

January 14-18 2013

Vacuum Science and Technology for Accelerator Vacuum Systems

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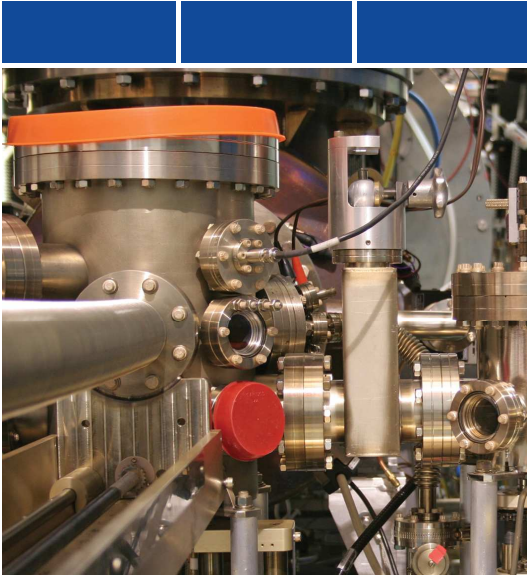


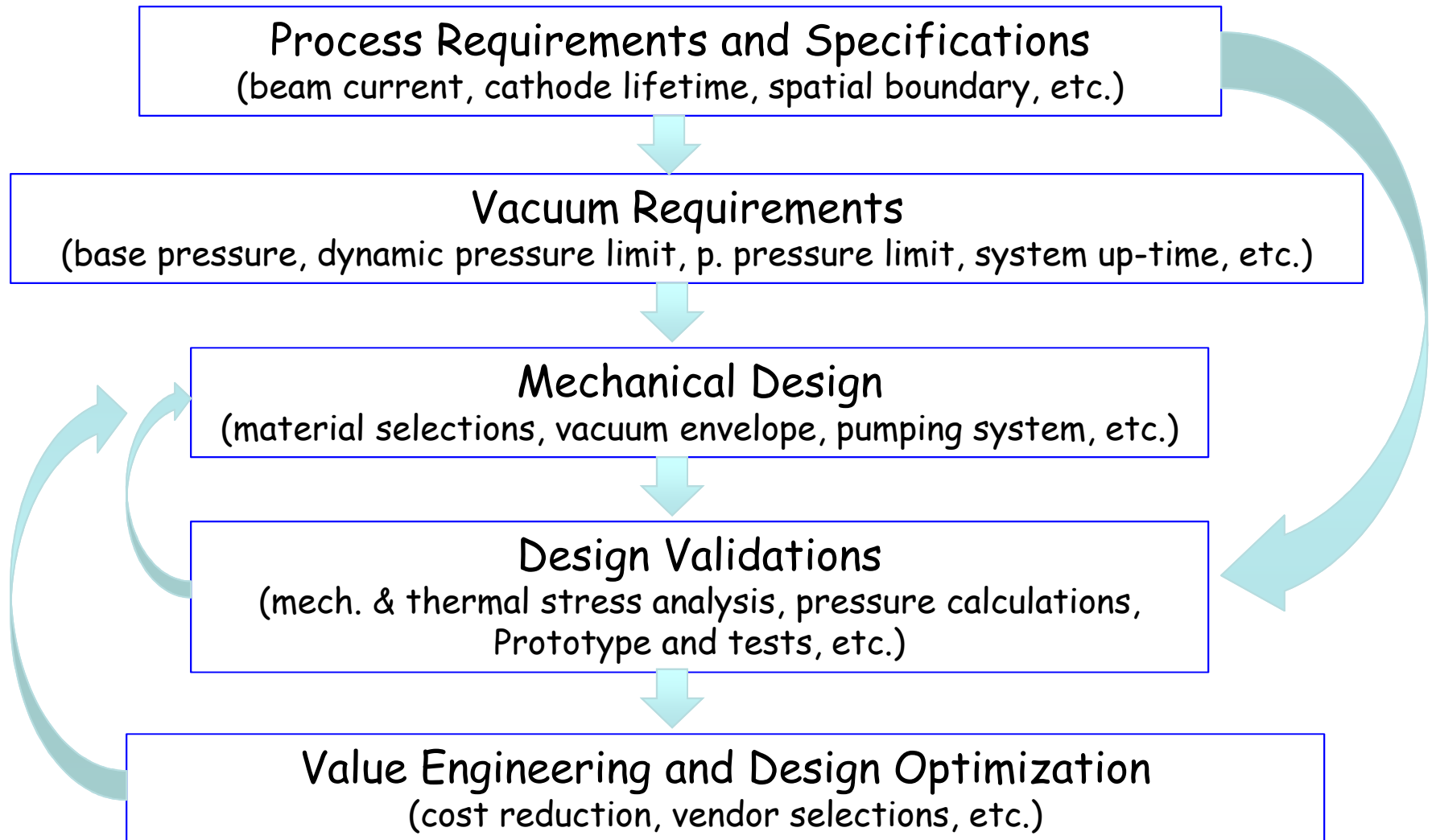
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SESSION 5: Vacuum System Engineering

- Typical vacuum system design/engineering flow
- High vacuum system design considerations
- Ultrahigh vacuum system design considerations
- Tools for vacuum system engineering
- Vacuum system integration

Typical Vacuum System Design Flow



Accelerator Vacuum Design Considerations



- ❑ Particle beam parameters
 - Type of particles: e^- , e^+ , p^+ , ions, etc.
 - Beam density
 - Beam temporal and spatial properties, etc.
 - ..., ...
- ❑ Magnets - Mainly spatial constraints
- ❑ Accelerating RF cavities
 - Particulate control - ultra-clean vacuum systems
 - 'Free' cryo-pumping for SRFs, but handling of warm-ups
 - Cryo related issues (insolation vacuum, etc.)
- ❑ Key functional accelerator components
 - SR generation insertion devices - in-vacuum and/or ex-vacuum
 - Particle sources - electron and positron, protons, ions,
 - Beam instrumentations - BPMs, beam size monitors, etc.



Vacuum Pressure Considerations



1. Base pressure

- For e^-/e^+ storage rings, base pressure usually an order of magnitude below beam induced dynamic pressure, typically in the low 10^{-10} torr range
- For high intensity proton and heavy ion machines, there are more demanding requirements on the base pressure, as beam-gas interaction is much sensitive
- For some special devices, such as photo-cathode electron sources, XHV environment is essential for the cathode lifetime

2. Dynamic pressure

- For e^-/e^+ storage rings, the dominating dynamic pressure is due to photon-induced desorption from intense SR. The maximum pressure must be controlled to a level such that the beam-loss from beam-gas interaction is below the other factors.
- For p^+ and ion machines, SR usually negligible. The dynamic pressure rise is primarily due to lost particles. Though beam loss is small, proton/ion induced desorption is much higher than PSD.
- Other collective effects (such as electron cloud, HOM heating, etc.) may also induce (usually nonlinear) pressure rises.



High Vacuum Systems



- ❑ *High vacuum system is dynamic pressure in range of 10^{-6} to 10^{-9} torr*
- ❑ *Examples of accelerator high vacuum systems:*
 - *Low beam intensity LINACs*
 - *Low beam intensity energy booster rings for storage rings*
 - *Insolation vacuum for cryo-modules*
- ❑ *For these systems, often discrete pumps are sufficient. Typical pumps used are ion pumps, diffusion pumps, cryo-pumps and turbo-molecular pumps.*
- ❑ *For cryo-module insolation vacuum, though with 'build-in' cryo-pumping from cryogenic surfaces, sufficient contingency pumping system must always included to deal with possible internal helium leaks.*
- ❑ *Material selection for high vacuum systems is usually dictated by cost and easiness of fabrications. Though cleanness is not as critical, a clean system will reduce cost of pumping system.*



Ultra-High Vacuum Systems



- ❑ *UHV system is dynamic pressure in range below 10^{-9} torr*
- ❑ *Examples of accelerator UHV systems:*
 - *Electron storage rings for light sources and colliders*
 - *High intensity proton and ion machines*
 - *High intensity LINACs*
- ❑ *For these systems, often distributed pumps are needed with gas conductance limited beam chambers, and distributed dynamic gas load. Only UHV-compatible pumps should be used, including ion pumps, NEGs and TiSPs.*
- ❑ *In most cases, only UHV compatible metals should be used for these systems. Stringent cleaning and UHV-compatible handling is paramount. Only all-metal joints are permitted.*
- ❑ *UHV ion gauges must be included in the UHV system. RGAs are strongly recommended for vacuum diagnostics.*
- ❑ *UHV system roughing and venting needs significant cares.*





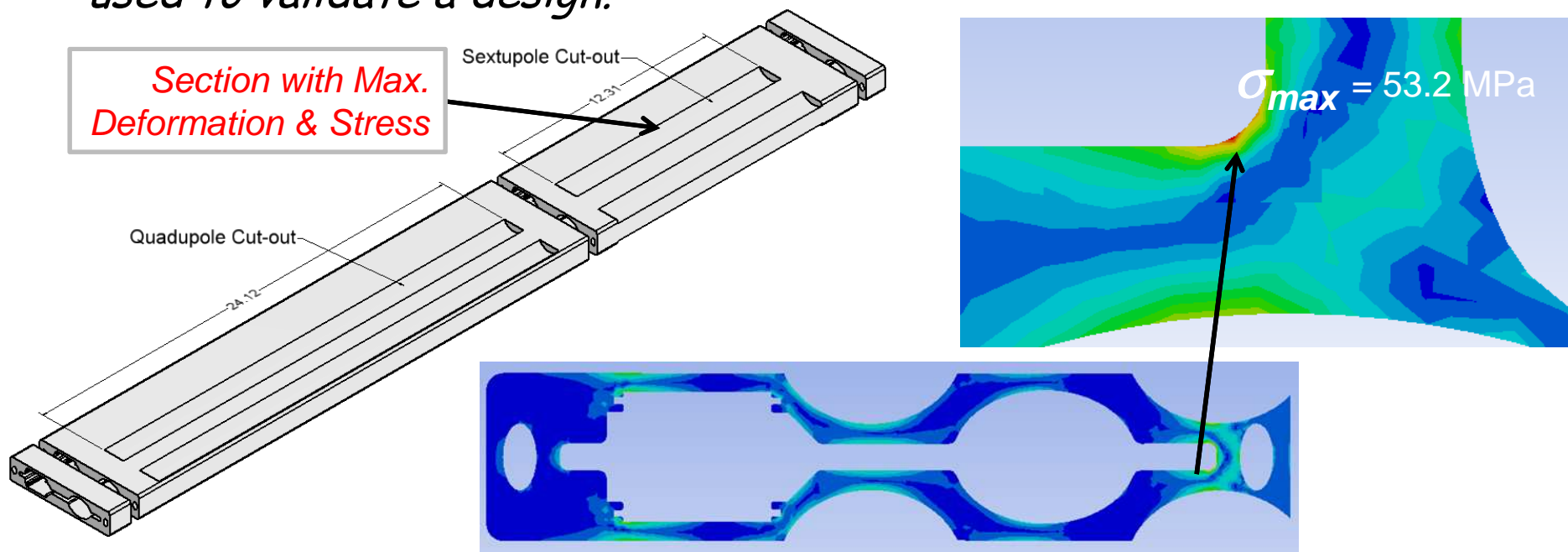
- ❑ *For high beam intensity accelerators, beam pipe material with high electric conductivity must be used for carrying image wall current.*
- ❑ *For beam chambers not subject to direct power deposition from synchrotron radiation or particle bombardment, stainless steel with copper coating/plating/lining is an option. The thickness of the copper coating only need to be a few factor of skin-depth at fundamental beam RF frequency.*
- ❑ *For beam chambers intercept SR power, or intense particle impingement, material with good bulk electric and thermal conductivities must be used. Aluminum alloys, copper or copper alloys are usually used.*



Chamber Design – Mechanical Consideration



- ❑ *In many beam chamber designs, there are often competing requirements to provide adequate beam aperture, while to bring magnet poles close to particle beam.*
- ❑ *These requirements may lead to minimizing chamber wall thickness and complex chamber shapes. Thorough mechanical analysis of chamber stress under atmospheric pressure must be carried out. Commercial finite-element analysis (FEA) tools, such as ANSYS, are used to validate a design.*



Mechanical Consideration Cont.



FEA results are not always the final word, if the material property inputs are incorrect (or not available). A copper beam chamber deformed severely during a 150°C bakeout, though FEA results predicted a 'healthy' safety margin at the temperature!



Distorted copper chamber during a bakeout



The chamber was saved by pressurizing and stiffening



Synchrotron Radiation in e^-/e^+ Storage Rings



- ❑ *For high beam current electron storage rings, SR power deposited on vacuum walls must be calculated.*
- ❑ *The calculated SR power distribution will be used to evaluate vacuum chamber design, to ensure*
 - (1) adequate cooling is provided to keep heating and thermal stress below a safe level;*
 - (2) no part of wall is subject to higher SR power that cannot handle by the wall materials;*
 - (3) proper 'masks' are in place to shadow components that may be damaged or affected by SR.*
- ❑ *For simple wall profiles, one can use the following formula for linear power density. The area power density can be calculated with a vertical SR angular spread of $\alpha_v = 1/\gamma$, where $\gamma = E_{\text{beam}}/E_{\text{rest}}$.*

$$P(W / mA) = 88.5 \frac{E^4 (GeV)}{R(m)} \frac{\Delta\alpha}{2\pi}$$



Synchrotron Radiation Calculations – SYNRAD



- ❑ *For more complex accelerator vacuum wall profile and SR-generating magnet arrangement, computing program is usually employed for SR calculations.*
- ❑ *In CESR, a program, SYNRAD, integrated into Bmad (A Relativistic Charged Particle Simulation Library^{REF}), is widely used for SR calculations.*
- ❑ *In SYNRAD, accelerator is divided into element along the curvilinear coordinates:*
 - *Photons are generated along the length of any element where SR are produced, using standard SR formulas for dipoles, quadrupoles and wigglers.*
 - *The generated photons are tracked to the vacuum chamber wall, horizontally, both inside and outside walls, also divided into elements.*
 - *SR power and photon flux along the walls are calculated.*

REF: [D. Sagan \(dcs16@cornell.edu\)](mailto:dcs16@cornell.edu), Synrad Information, October 1, 2010



SYNRAD Input files



```
&synrad_params
sr_param%lat_file = "lat.bmad"    ! Input lattice.
sr_param%i_beam = 0.1             ! Single-beam current.
sr_param%epsilon_y = 10e-12       ! Vertical emittance.
sr_param%n_slice = 20            ! # of slices per element or wiggler period
seg_len = 0.1                    ! Segment length for calculation.
beam_direction = 0                ! -1 = track backwards only,
                                ! 0 = track both directions, 1 = forward.

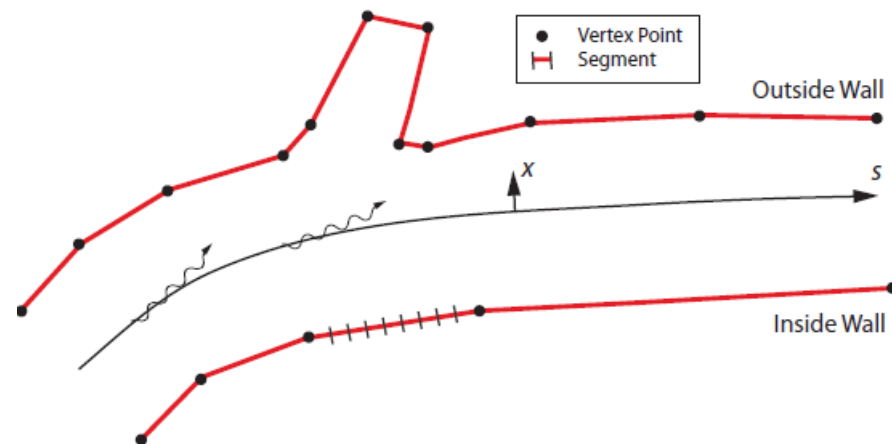
wall_file = "wall.dat"           ! "NONE" => Use a wall with a fixed offset from the beam
wall_offset = 0.045              ! Used when wall_file is set to "NONE"
forward_beam = "POSITRON"        ! "POSITRON" or "ELECTRON"
backward_beam = "ELECTRON"       ! This is important if there are elsep elements.
```

Main Input

Wall Definition

! Note: x_inside should be negative.
! Note: First s_position should be 0.
!

!s_position	x_inside	x_outside
0	-0.025	0.025
10	-0.025	0.025
10.3	-0.025	0.037
... etc ...		



SYNRAD Generated Five Output files



➤ element_power.dat

List of all elements where radiation is produced showing the power radiated and the power that hit the walls. These two numbers should be the same.

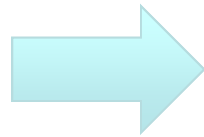
➤ synch_power_negative_x_side.dat & synch_power_positive_x_side.dat

List of all wall segments showing such things as power deposited, power per unit length, photons per second impinging, etc.

➤ synrad_negative_x_side.txt & synrad_positive_x_side.txt

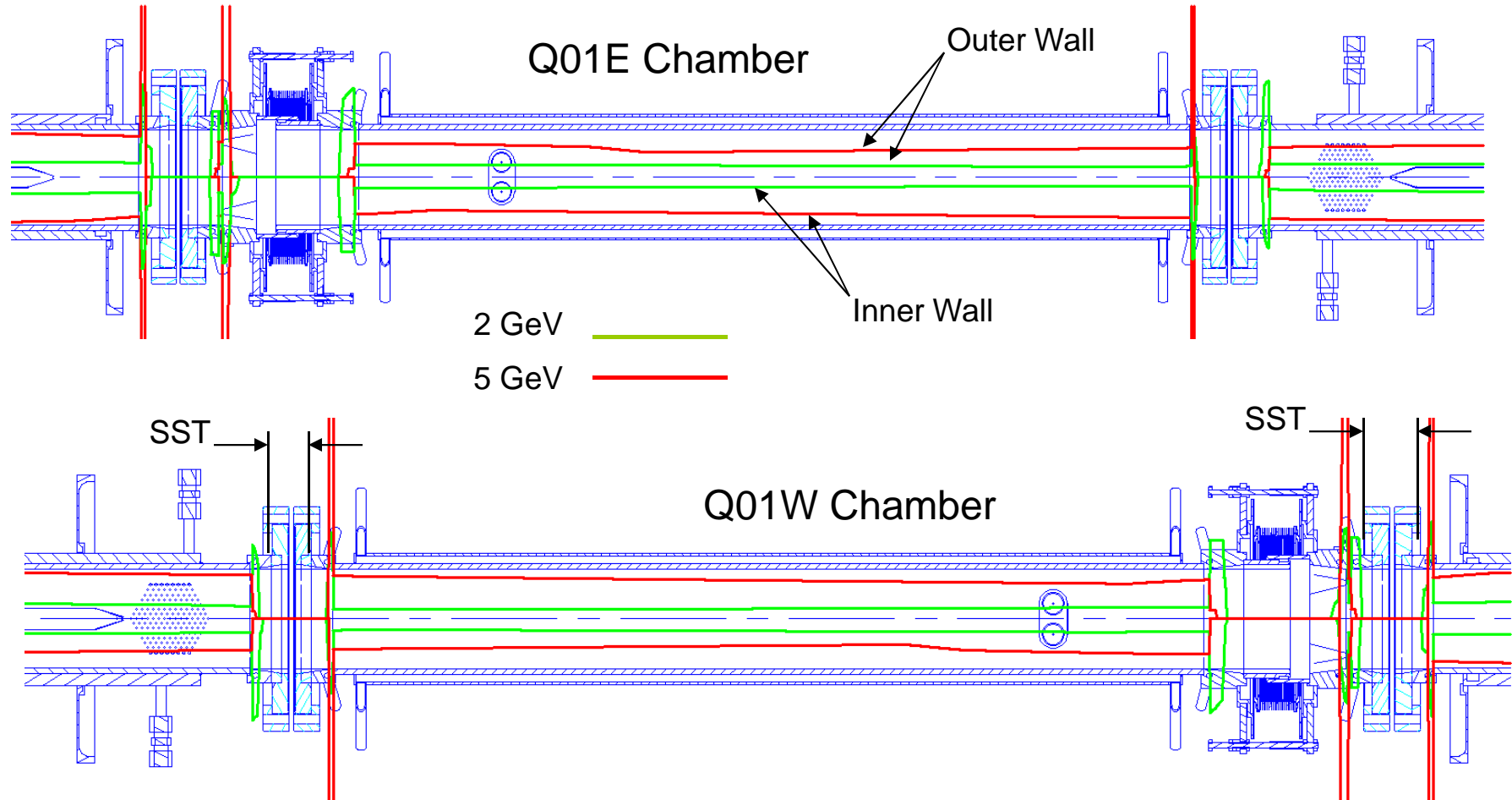
Similar to above, only in different format

**Example
output file**



synch_power_Outside.dat							
Lattice: cer1/trunk/model/lat.bmad							
I_beam = 0.100000001490116 ! Amps/beam							
Epsilon_y = 2.999999901276418E-011 ! Vertical emittance							
Segment							
Ix	Name	S_seg (m)	X_seg (m)	P/len (w/m)	P/Area (kw/m^2)	P_tot (w)	Phot/sec (1/s)
1	OUTSIDE	0.100	0.030	0.00E+00	0.0000E+00	0.0000E+00	0.0000E+00
2	OUTSIDE	0.200	0.030	0.00E+00	0.0000E+00	0.0000E+00	0.0000E+00
3	OUTSIDE	0.300	0.030	0.00E+00	0.0000E+00	0.0000E+00	0.0000E+00
4	OUTSIDE	0.400	0.030	0.00E+00	0.0000E+00	0.0000E+00	0.0000E+00
5	OUTSIDE	0.500	0.030	0.00E+00	0.0000E+00	0.0000E+00	0.0000E+00
4124	OUTSIDE	412.386	0.030	0.00E+00	0.0000E+00	0.0000E+00	0.0000E+00
4125	OUTSIDE	412.486	0.030	0.00E+00	0.0000E+00	0.0000E+00	0.0000E+00
4126	OUTSIDE	412.586	0.030	0.94E+02	0.2907E+04	0.9418E+01	0.1116E+18
4127	OUTSIDE	412.686	0.030	0.13E+03	0.4255E+04	0.1336E+02	0.1583E+18
4128	OUTSIDE	412.786	0.030	0.13E+03	0.4181E+04	0.1331E+02	0.1577E+18
4129	OUTSIDE	412.886	0.030	0.13E+03	0.4132E+04	0.1336E+02	0.1583E+18
4130	OUTSIDE	412.986	0.030	0.13E+03	0.4058E+04	0.1331E+02	0.1577E+18
22889	OUTSIDE	2288.823	0.030	0.00E+00	0.0000E+00	0.0000E+00	0.0000E+00
22890	OUTSIDE	2288.923	0.030	0.00E+00	0.0000E+00	0.0000E+00	0.0000E+00
22891	OUTSIDE	2289.023	0.030	0.00E+00	0.0000E+00	0.0000E+00	0.0000E+00
22892	OUTSIDE	2289.123	0.030	0.00E+00	0.0000E+00	0.0000E+00	0.0000E+00
22893	OUTSIDE	2289.223	0.030	0.00E+00	0.0000E+00	0.0000E+00	0.0000E+00
22894	OUTSIDE	2289.323	0.030	0.00E+00	0.0000E+00	0.0000E+00	0.0000E+00
22895	OUTSIDE	2289.423	0.030	0.00E+00	0.0000E+00	0.0000E+00	0.0000E+00
22896	OUTSIDE	2289.523	0.030	0.00E+00	0.0000E+00	0.0000E+00	0.0000E+00
22897	OUTSIDE	2289.623	0.030	0.00E+00	0.0000E+00	0.0000E+00	0.0000E+00
22898	OUTSIDE	2289.723	0.030	0.00E+00	0.0000E+00	0.0000E+00	0.0000E+00

SYNRAD Results – CesrTA Modification Example

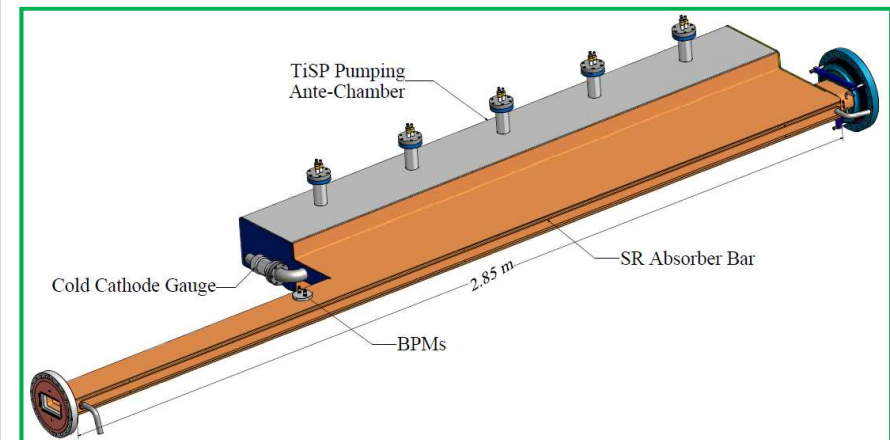
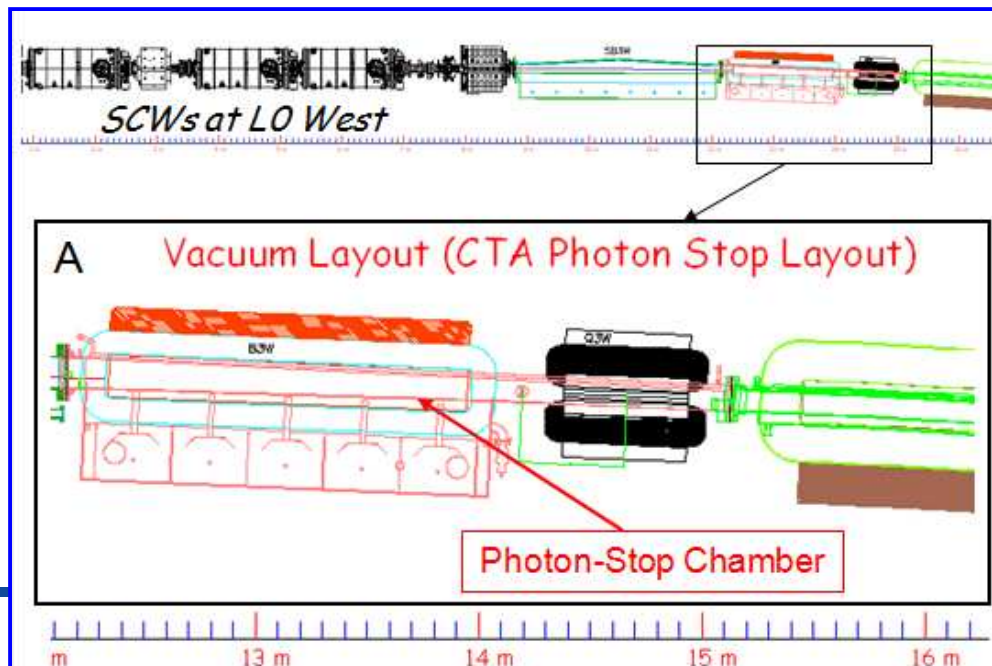
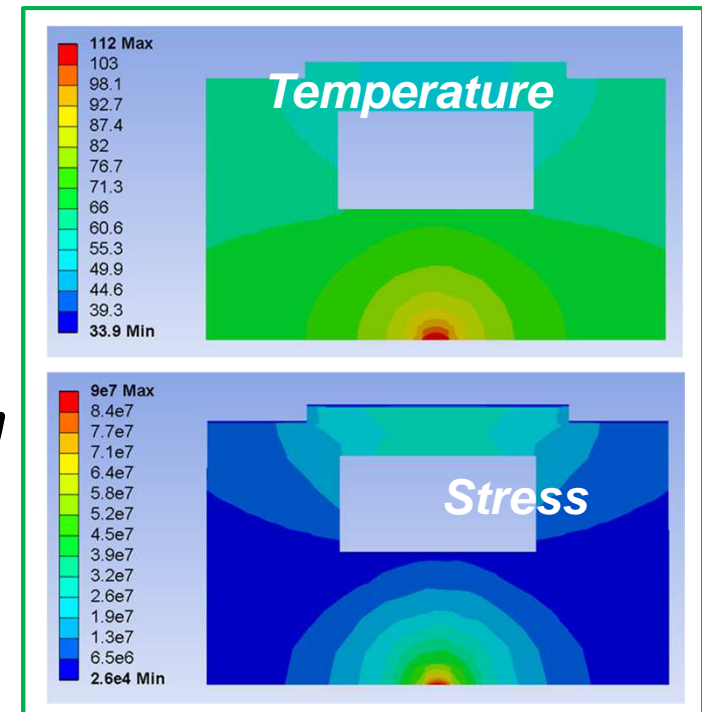


*SYNRAD used to ensure proper SR Masks
were designed to shadow non-cooled components*

Thermal Stress Analysis – Example



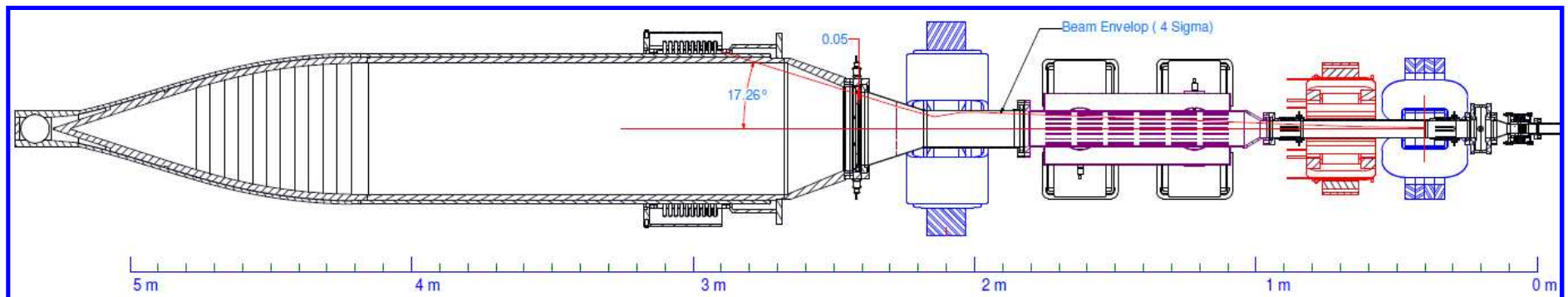
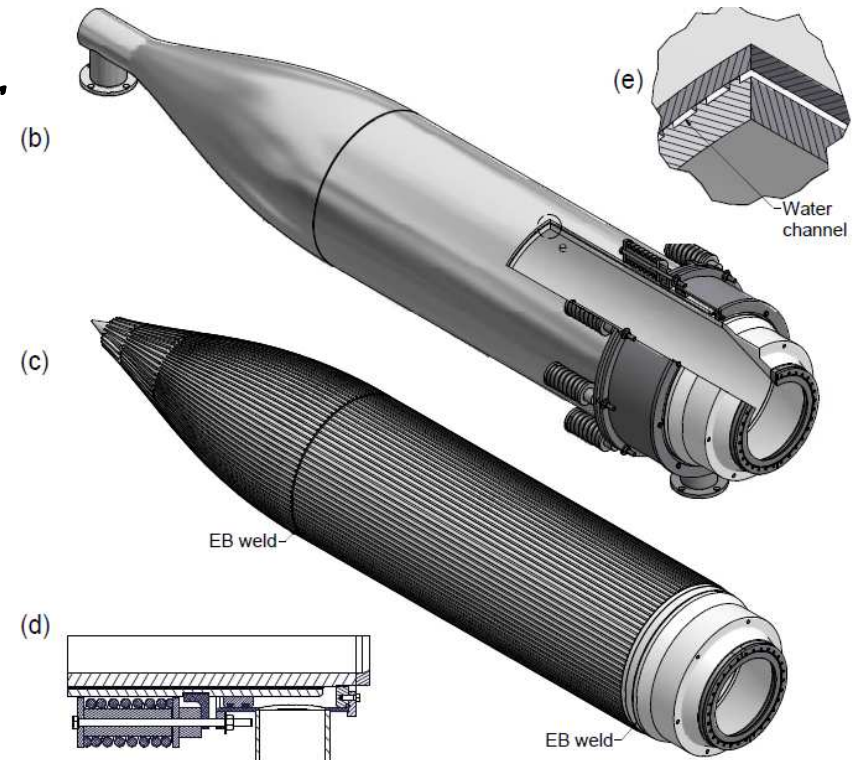
- During CestrA vacuum system conversion, a photon stopper chamber had to be designed to handle 40 kW of SR power generated from a string of six superconducting wigglers.
- ANSYS was used to calculate temperature rises and stress, at maximum power density of 6 W/mm², to verify safe operation of the chamber.



Electron Beam Dump – Another Example



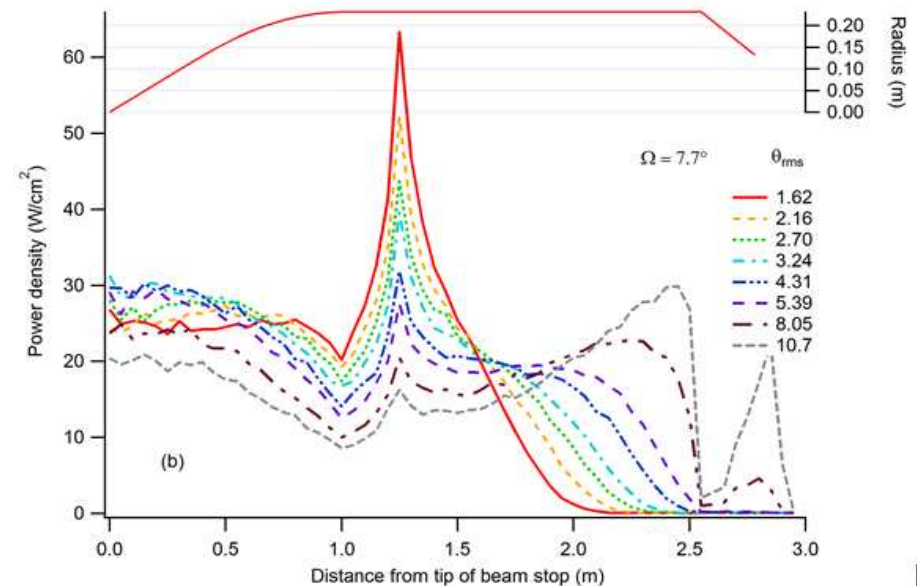
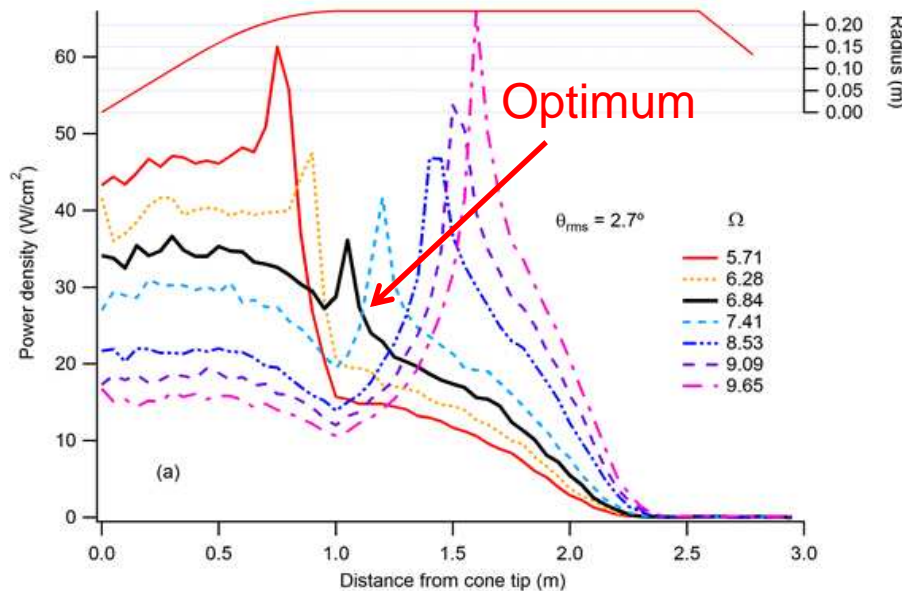
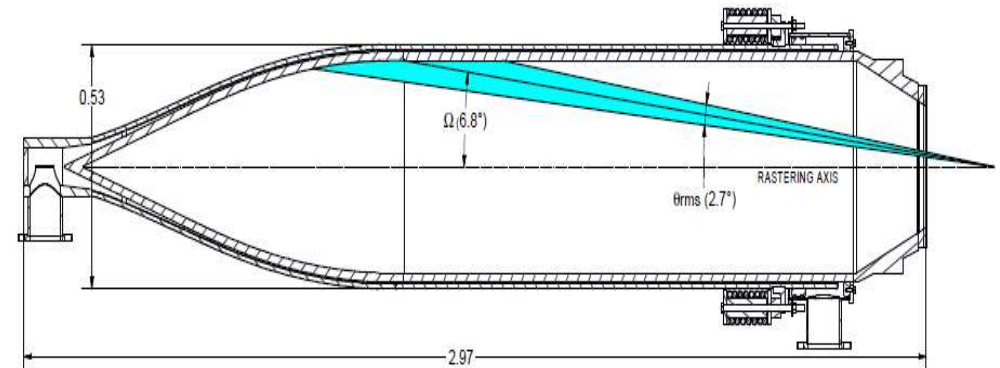
- ❑ In Cornell's ERL prototype inject project, an 600-kW electron dump was designed and constructed.
- ❑ Aluminum (6062-T6) was chosen over copper due to its higher neutron generation threshold.
- ❑ A pair of quads used to enlarge the beam sized, and a modified Sectupole used to raster centroid of the beam.
- ❑ Cooling water channeled through small channels to enhance heat exchange.



Simulate & optimize power deposition

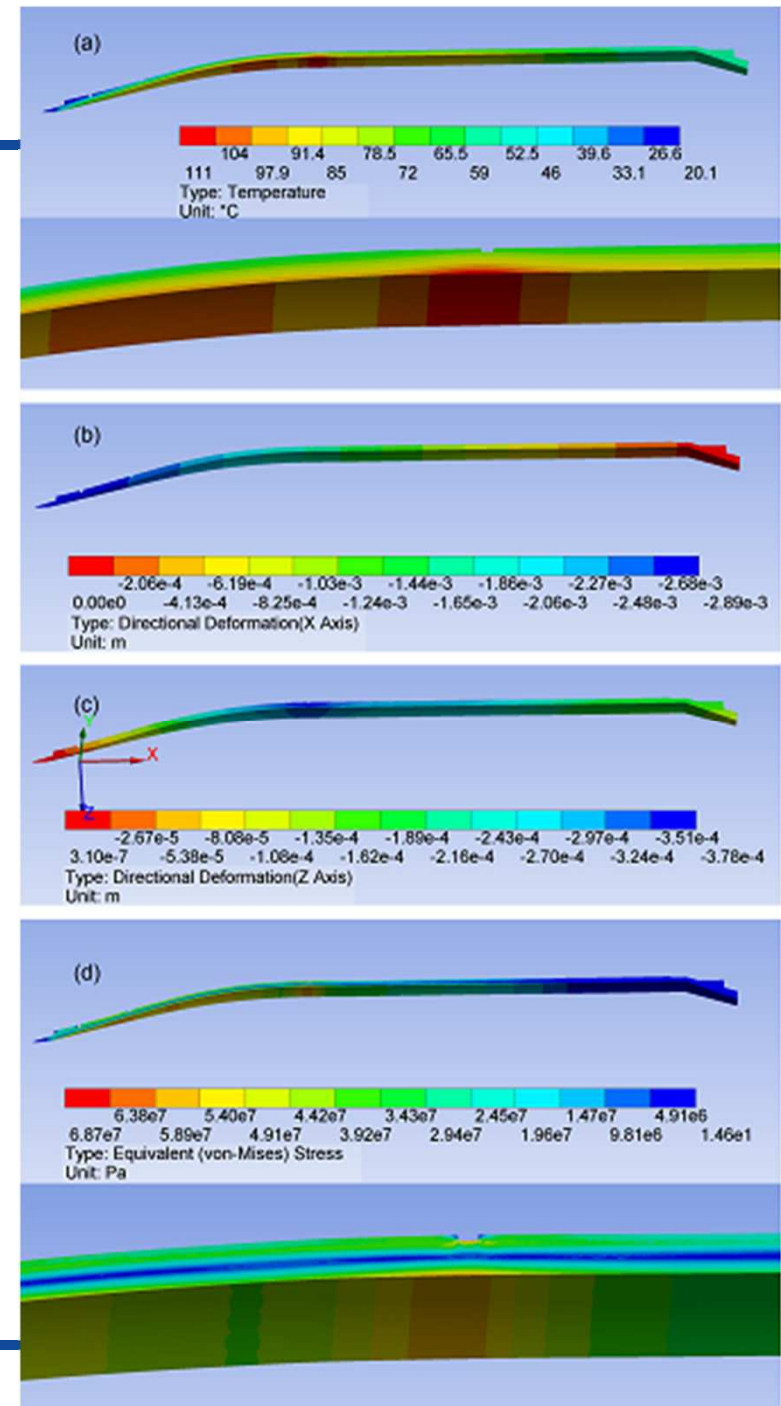
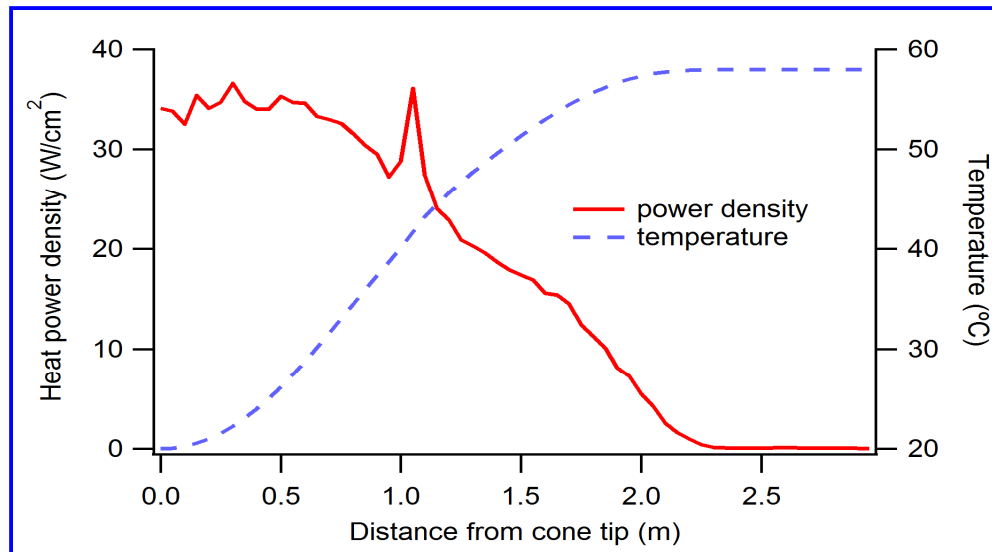


- Geant4 (a toolkit for the simulation of the passage of particles through matter) was used to simulate electron beam interaction with dump body, and to optimize beam setup for even power deposition



Dump Thermal Analysis

- After optimizing electron beam setting, ANSYS was used to calculate temperature distribution and analysis thermal stress, to ensure operational safety at design power level.
- Taking symmetry advantage, only one slice (16.4°) of the dump body needs to be modeled, to save computing time.



Pressure Profile Calculations/Simulations



- *In accelerator vacuum system design, or/and in accelerator operations, knowledge of vacuum pressure distribution (or profile) is often needed for the following reasons:*
 - *Optimizing pumping speed and capacity installed to keep average pressure and peak pressure under desirable level*
 - *Understand impact of regional conductance limitation and local high gas load to the accelerator operations (such as beam lifetime, background to HEP detector, X-ray users)*
- *For almost all accelerator vacuum systems, molecular flow condition prevail.*
- *Though analytical method may work for very simple systems (such as round tubes), numerical approaches are usually used in simulating the pressure profile, with defined geometry, known pumping and calculated gas loads.*



One-Dimensional Pressure Profiles



- *Since most accelerators and components have one dimension which is much bigger than the two others (length of the beamlines vs cross-section of the beam pipe), one-dimensional mass-balance equation may be used:*

$$V \frac{dP(x,t)}{dt} = Q(x,t) - S(x,t) \cdot P(x,t) + c(x,t) \cdot \frac{d^2 P(x,t)}{dx^2}$$

- *At static states (which apply to most accelerator operation condition, where beam current varies slowly):*

$$S(x) \cdot P(x) - c(x) \cdot \frac{d^2 P(x)}{dx^2} = Q(x)$$

where $S(x)$, $Q(x)$ are pumping speed and gas load, $c(x)$ is specific gas conductance

- *In the literature, it is solutions to this equation that are found most often. Some of them are obtained analytically, others numerically.*



Analytical Solution – Periodic System



- Consider a simple vacuum system of uniform cross section, with lumped pumps installed every L meters apart, no distributed pumping.
- Let A be the specific surface of the vacuum chamber, in cm^2/m , and an uniform thermal outgassing rate, q in $\text{mbar}\cdot\text{l}/\text{s}\cdot\text{cm}^2$, we have

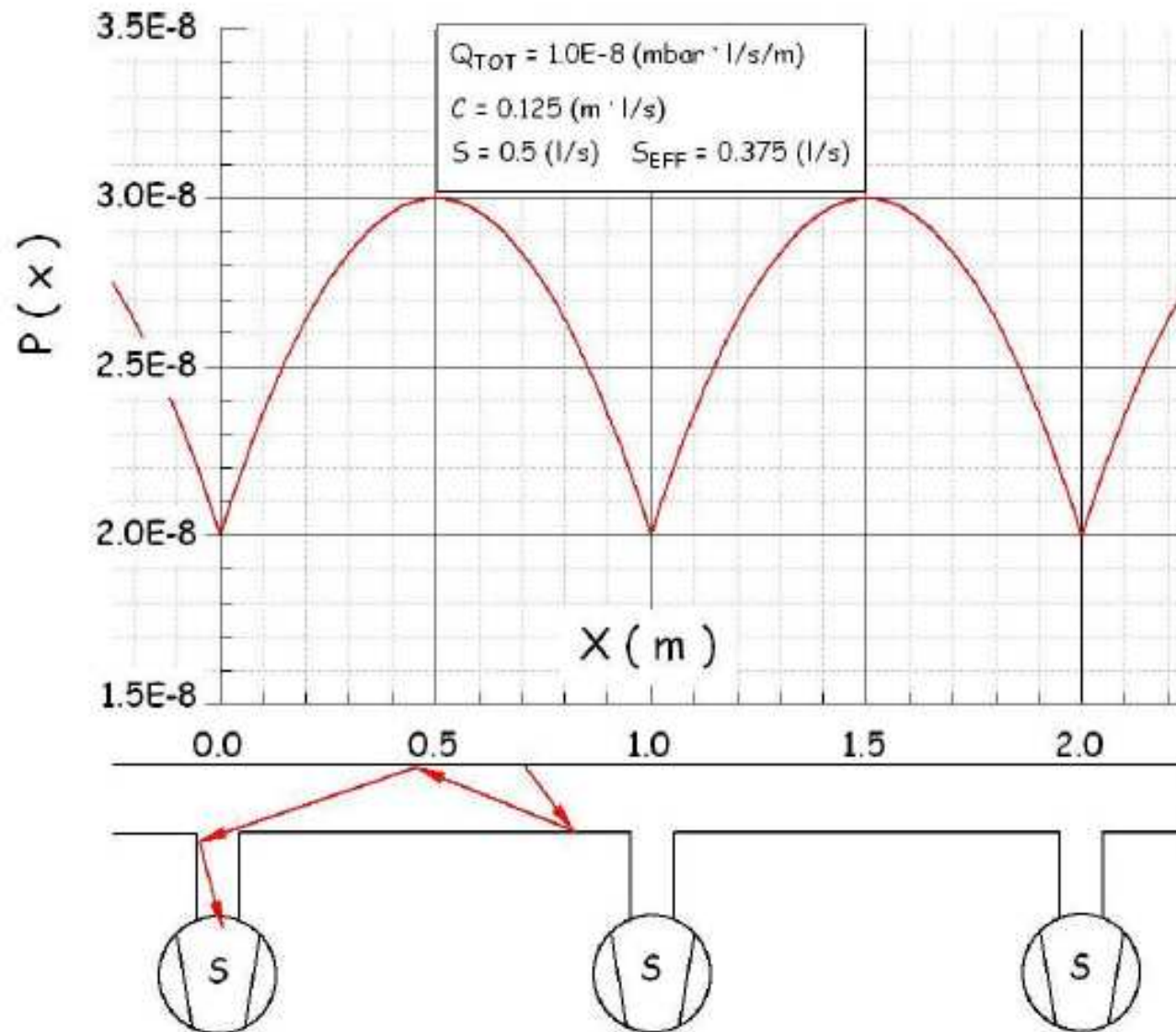
$$c \frac{d^2 P(x)}{dx^2} = -Aq \quad \text{and by symmetry:} \quad \begin{cases} \frac{dP}{dx}(x = L/2) = 0 \\ P(x = 0) = AqL/S \end{cases}$$

- The solution is:

$$P(x) = \frac{Aq}{2c} (Lx - x^2) + \frac{AqL}{S}$$



Analytical Solution – Periodic System Cont.

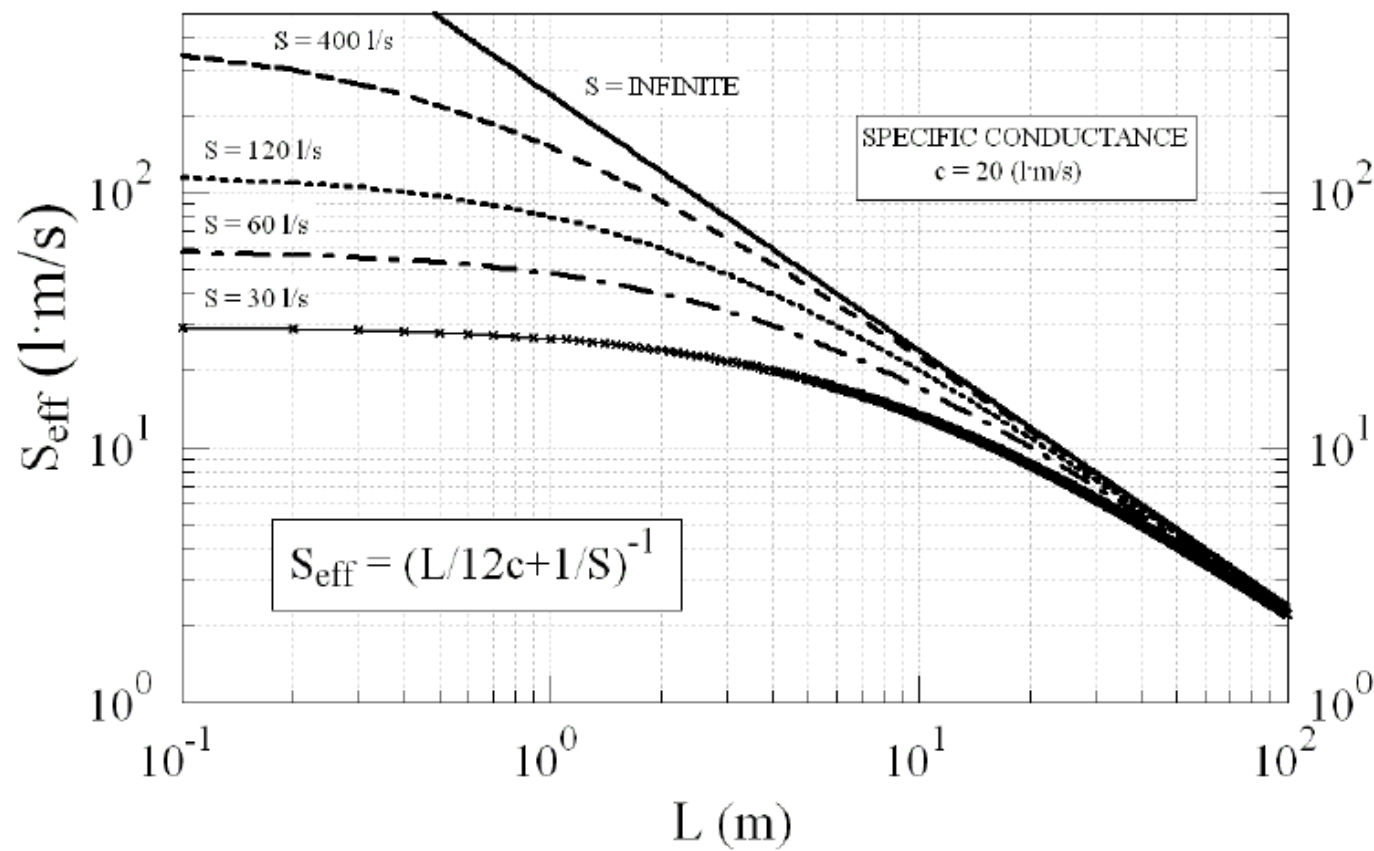


Analytical Solution – Periodic System Cont.



Average and maximum pressures are:

$$P_{avg} = AqL \left(\frac{L}{12c} + \frac{1}{S} \right) \equiv AqL \cdot \frac{1}{S_{eff}} \quad \text{AND} \quad P_{max} = AqL \left(\frac{L}{8c} + \frac{1}{S} \right)$$



VACCALC: A Numerical Implementation



This solving technique is based on the finite-difference method, by 'slicing' vacuum system into N elements of equal length, Δx

$$S(x) \cdot P(x) - c(x) \cdot \frac{d^2 P(x)}{dx^2} = Q(x) \quad \Rightarrow \quad \frac{d}{dx} \left(c_i \frac{dP_i}{dx} \right) - S_i \cdot P_i + Q_i = 0$$

AND:

$$\frac{d}{dx} \left(c_i \frac{dP}{dx} \right) = \frac{(c_{i+1} - c_i)P_{i+1} + (c_i - c_{i-1})P_{i-1} - (c_{i+1} - c_{i-1} + 2c_i)P_i}{2\Delta x^2}$$

$$\frac{c_i + c_{i-1}}{2} P_{i-1} + \left\{ \frac{-(c_{i+1} + c_{i-1} + 2c_i)}{2} - s_i \Delta x^2 \right\} P_i + \frac{c_{i+1} + c_{i+1}}{2} P_{i+1} = q_i \Delta x^2$$

With proper boundary conditions, these linear equations can be solved for the pressure profile, P_i

Ref. "A Method for Calculating Pressure Profiles in Vacuum Pipes", Sullivan, SLAC, 1993



VACCALC Input



- *Each beampipe element is described by the following characteristics:*
 - *Lumped or distributed values.*
 - *Length (m)*
 - *Axial conductance (liters/sec)*
 - *Outgassing rate (nTorr-liters/sec)*
 - *Pumping speed (liters/sec)*
- *Segment length (Δx) is specified for all elements*
- *10,000 segments max. per pipe*



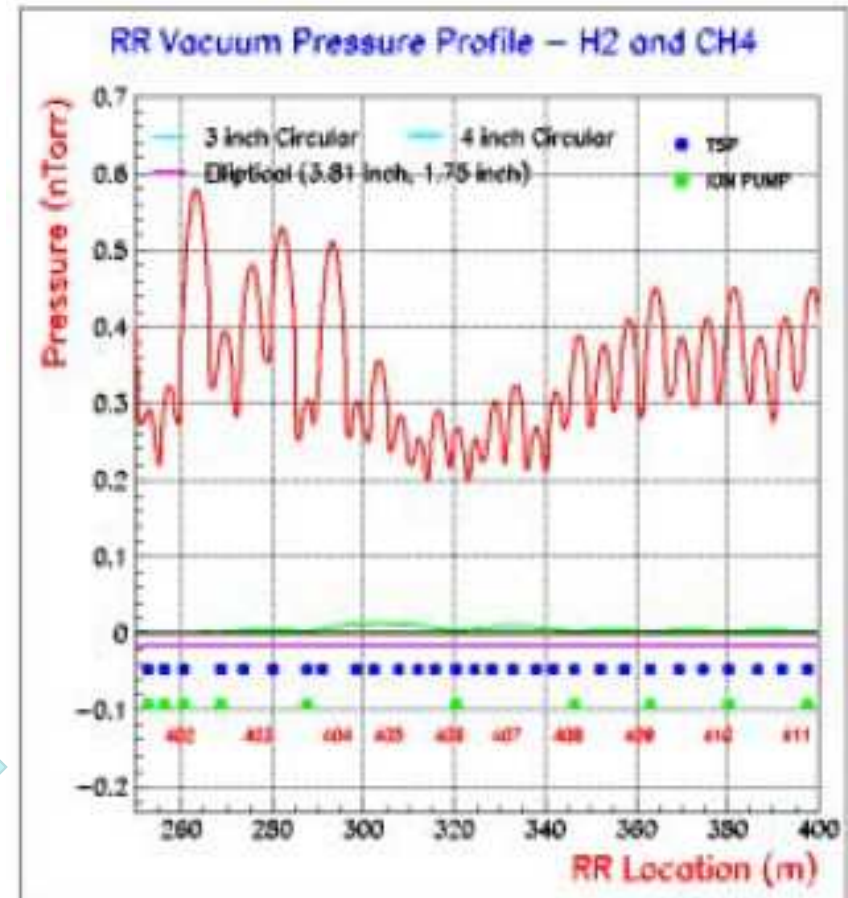
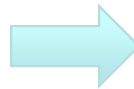
VACCALC Output



➤ *VACCALC produces an Excel Spreadsheet output file called "VACCALC.tsv" which includes the following:*

1. *Pressure (nTorr) vs. Z (meters)*
2. *Average Pressure along piping segment (nTorr)*
3. *Axial Conductance (liters/sec-m) vs. Z (meters)*
4. *Gas load (nTorr-liters/sec-m) vs. Z (meters)*
5. *Pumping Speed (liters/sec-m) vs. Z (meters)*

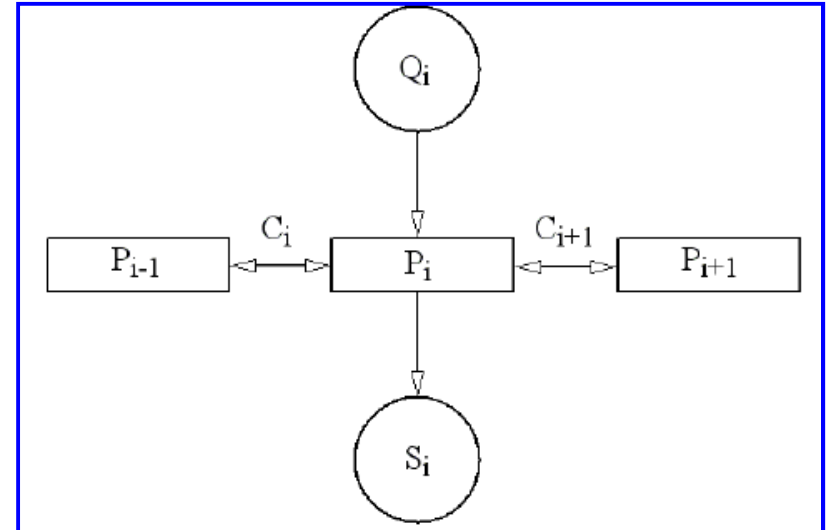
Example: K. Gounder, et al, "RESIDUAL GAS PRESSURE PROFILE IN THE RECYCLER RING", *Proceedings of the 2003 Particle Accelerator Conference*



The Continuity Principle of Gas Flow



- Another way of solving the mass-flow balance equation is the so-called Continuity Principle of Gas Flow*, which can be stated after discretization of the vacuum system as shown.
- Each segment of the vacuum system is assigned its S_i , Q_i and C_i , and then its pressure P_i is obtained by solving the set of equations:



$$C_i (P_{i-1} - P_i) + C_{i+1} (P_{i+1} - P_i) + Q_i = S_i P_i$$

- Three boundary conditions (BCs) were discussed in the reference(*):

1) Periodic BC; (2) Smooth BC; (3) Fixed BC

* Y. Li *et al.*, Calculation of pressure profiles in the CESR hardbend and IR regions, Proc. Int. Workshop on Performance and Improvement of e-e+ Collider Particle Factories, Tsukuba, 1999



The Continuity Principle of Gas Flow Cont.



Periodic BC:

$$\begin{cases} P_0 = P_n \\ P_{n+1} = P_0 \end{cases} \quad \text{then} \quad \begin{cases} C_1(P_n - P_1) + C_2(P_2 - P_1) + Q_1 = S_1 P_1 \\ C_i(P_{i-1} - P_i) + C_{i+1}(P_{i+1} - P_i) + Q_i = S_i P_i \\ C_n(P_{n-1} - P_n) + C_1(P_1 - P_n) + Q_n = S_n P_n \end{cases}$$

Smooth BC:

$$\begin{cases} P_0 = P_1 \\ P_{n+1} = P_n \end{cases} \quad \text{then} \quad \begin{cases} C_2(P_2 - P_1) + Q_1 = S_1 P_1 \\ C_i(P_{i-1} - P_i) + C_{i+1}(P_{i+1} - P_i) + Q_i = S_i P_i \\ C_n(P_{n-1} - P_n) + Q_n = S_n P_n \end{cases}$$

Fixed BC:

$$\begin{cases} P_0 = \text{known} \\ P_{n+1} = \text{known} \end{cases} \quad \text{then} \quad \begin{cases} -C_1 P_1 + C_2(P_2 - P_1) + (Q_1 + C_1 P_0) = S_1 P_1 \\ C_i(P_{i-1} - P_i) + C_{i+1}(P_{i+1} - P_i) + Q_i = S_i P_i \\ C_n(P_{n-1} - P_n) - C_1 P_n + (C_{n+1} P_{n+1} + Q_n) = S_n P_n \end{cases}$$

All these linear equations can be easily solved to obtain pressure profile, via so-called *Substitute-Forward & Chase-Backward* method, as described in the reference.

Arithmetic for Smooth BC



Continuity Principle of Gas Flow equations can be rewrite as:

$$a_i P_{i-1} + P_i + b_i P_{i+1} = d_i \quad (i=1,2,\dots,n) \quad \textbf{(A)}$$

$$\begin{cases} a_i = -C_i / (C_i + C_{i+1} + S_i) \\ b_i = -C_{i+1} / (C_i + C_{i+1} + S_i) \\ d_i = Q_i / (C_i + C_{i+1} + S_i) \end{cases} \quad \begin{cases} a_1 = 0 \\ b_1 = -C_2 / (C_2 + S_1) \\ d_1 = Q_1 / (C_2 + S_1) \end{cases} \quad \begin{cases} a_n = -C_n / (C_n + S_n) \\ b_n = 0 \\ d_n = Q_n / (C_n + S_n) \end{cases}$$

***Forward-Substitute** (solving for P_i in i th equation in equations (A) and then substituting solved P_i into $(i+1)$ th equation in equations (A), an so forth, from $i=1$ to $i=n$)*

$$\begin{cases} P_i = d_i^* - b_i^* P_{i+1} & (i=1,2,\dots,n-1) \\ P_n = d_n^* \end{cases} \quad \textbf{(B)}$$

$$\begin{cases} b_1^* = b_1 \\ d_1^* = d_1 \end{cases} \quad \& \quad \begin{cases} b_i^* = b_i / (1 - a_i b_{i-1}^*) \\ d_i^* = (d_i - a_i d_{i-1}^*) / (1 - a_i b_{i-1}^*) \end{cases} \quad (i=2,3,\dots,n-1) \quad \& \quad d_n^* = (d_n - a_n d_{n-1}^*) / (1 - a_n b_{n-1}^*)$$

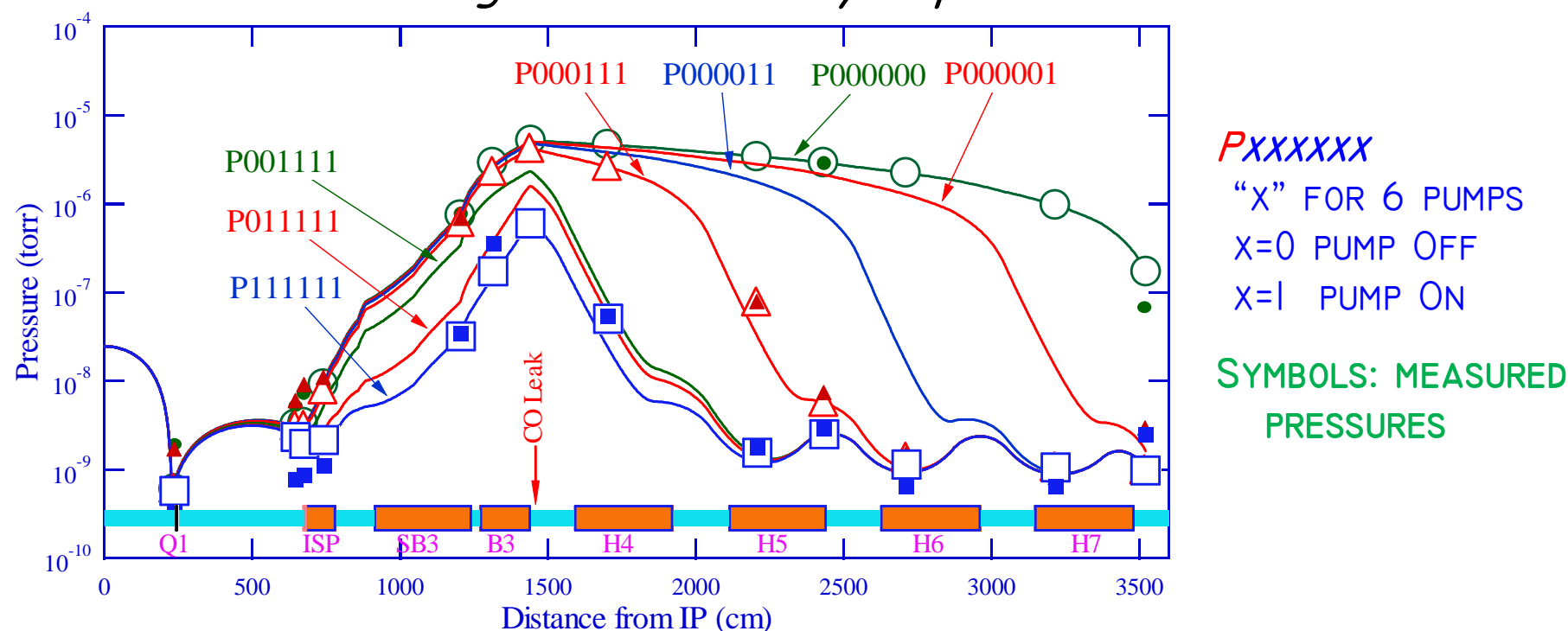
The pressure profile is now easily obtained by 'chase-back' of equation (B)

Implementation in IGOR Pro. (ICM Prototype Beamline Pressure Profile)

Application – Background of HEP Detector



In CESR/CLEO HEP II operations, an experiment was conducted to probe the HEP detector background sensitivity to pressure distribution



- *In the experiment, a CO gas was introduced to create a 'pressure bump', and ion pumps (2 LPs, 4 DIPs) were turned off sequentially to spread the bump. A probe electron beam was sent through the bump to measure detector background.*
- *Pressure profiles were calculated and compared to the measured pressures, with ion pump speed's pressure dependence taking into account.*
- *The results helped design of background masks for the CESR/CLEO III upgrade.*

Application – Background of HEP Detector 2



* Gas load Q -- dominated by the CO leak, 1.6×10^{-5} torr·liter/s

* Conductance -- calculated using MOLFLOW

* Pumping Speed

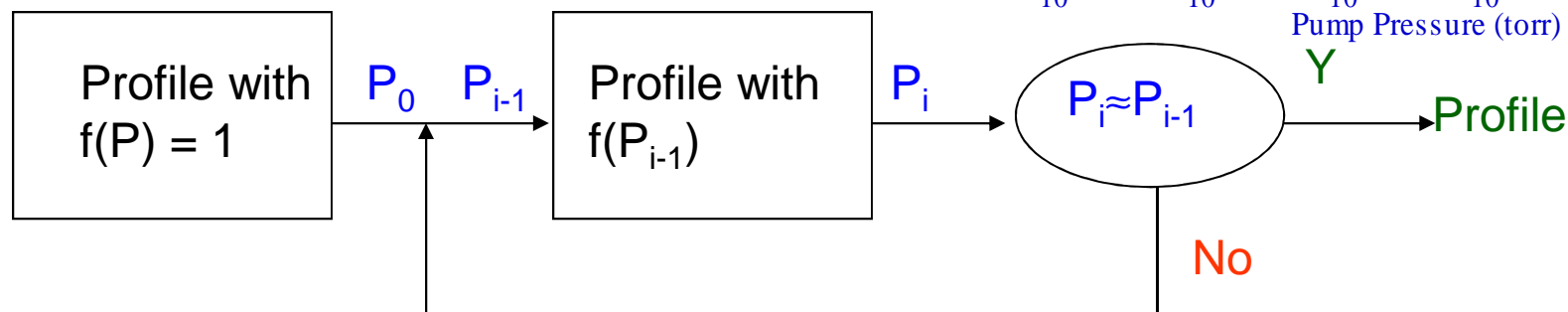
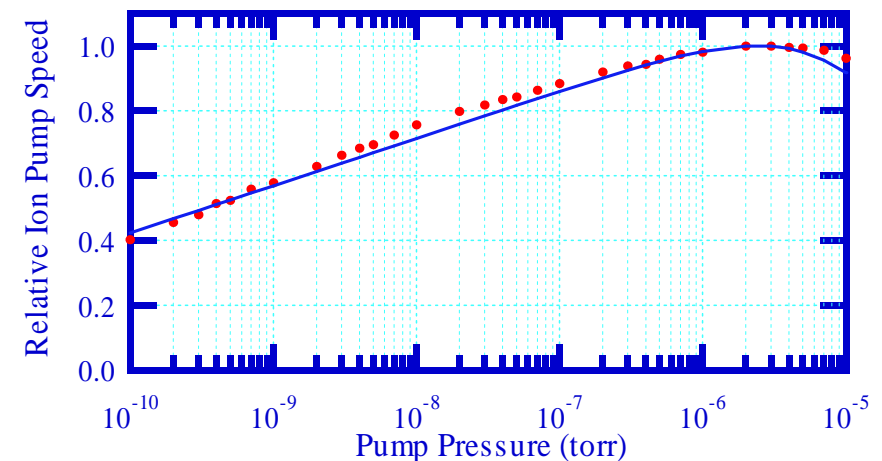
TiSPs -- $S_{\max} \cdot F_{\text{sat}}$; S_{\max} - Plenum Conductance,
 F_{sat} - Saturation factor

DIPs -- $S_{\max} \cdot f(P)$, Pressure dependent
 pumping speed

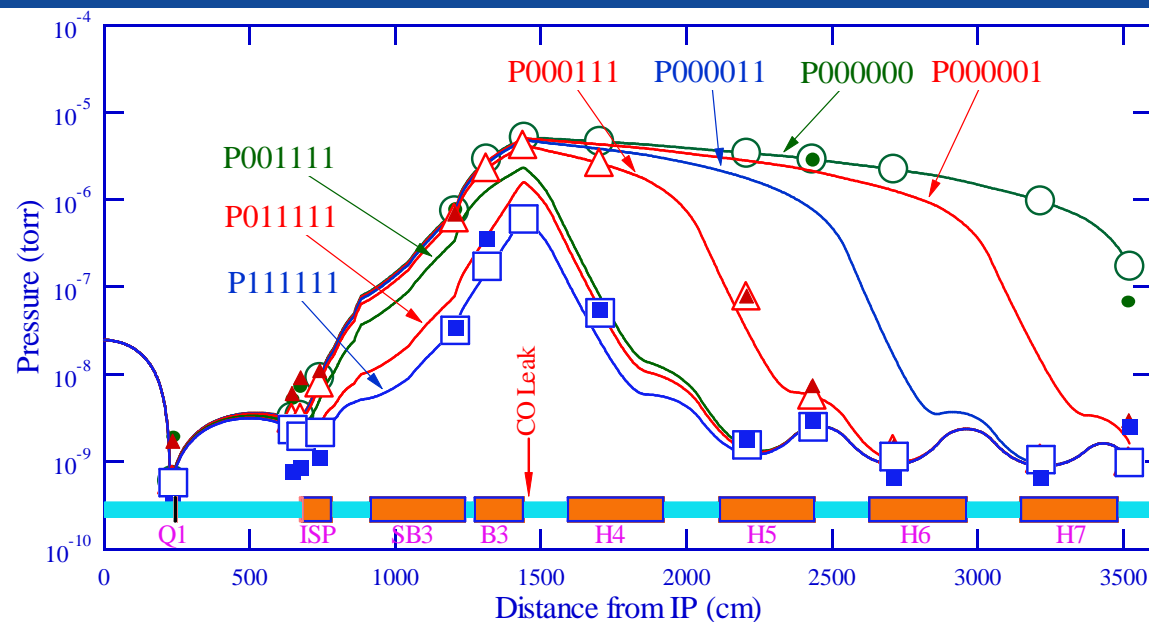
* Self-consistent iteration

Table 3. DIP Pumping Speed Parameters

DIP Name	Max. Pumping Speed, l/s/m
B3E	55
H4E	85
H5E	100
H6E	120
H7E	120

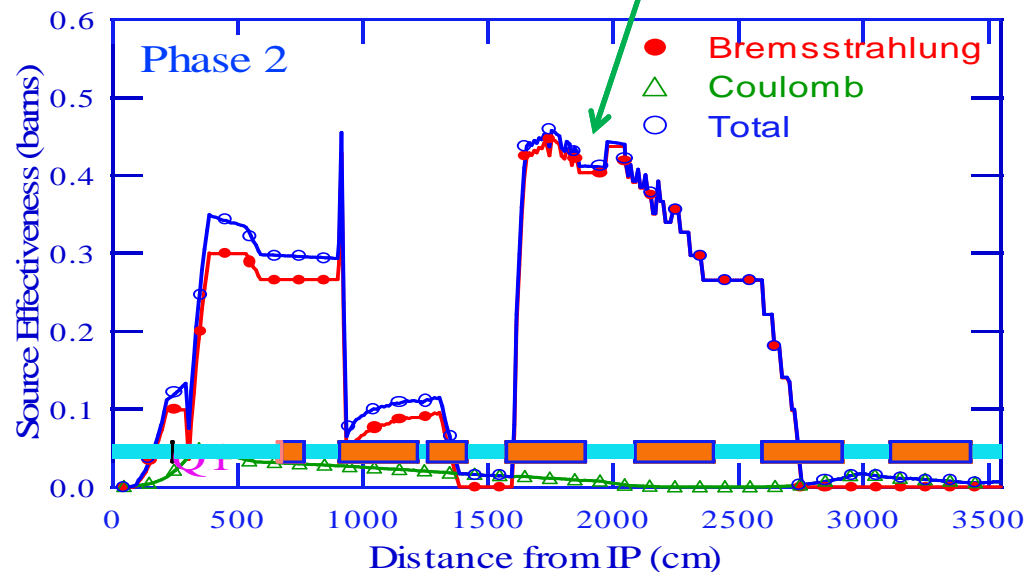


Pressure Manipulations and Calculations



This was a surprise

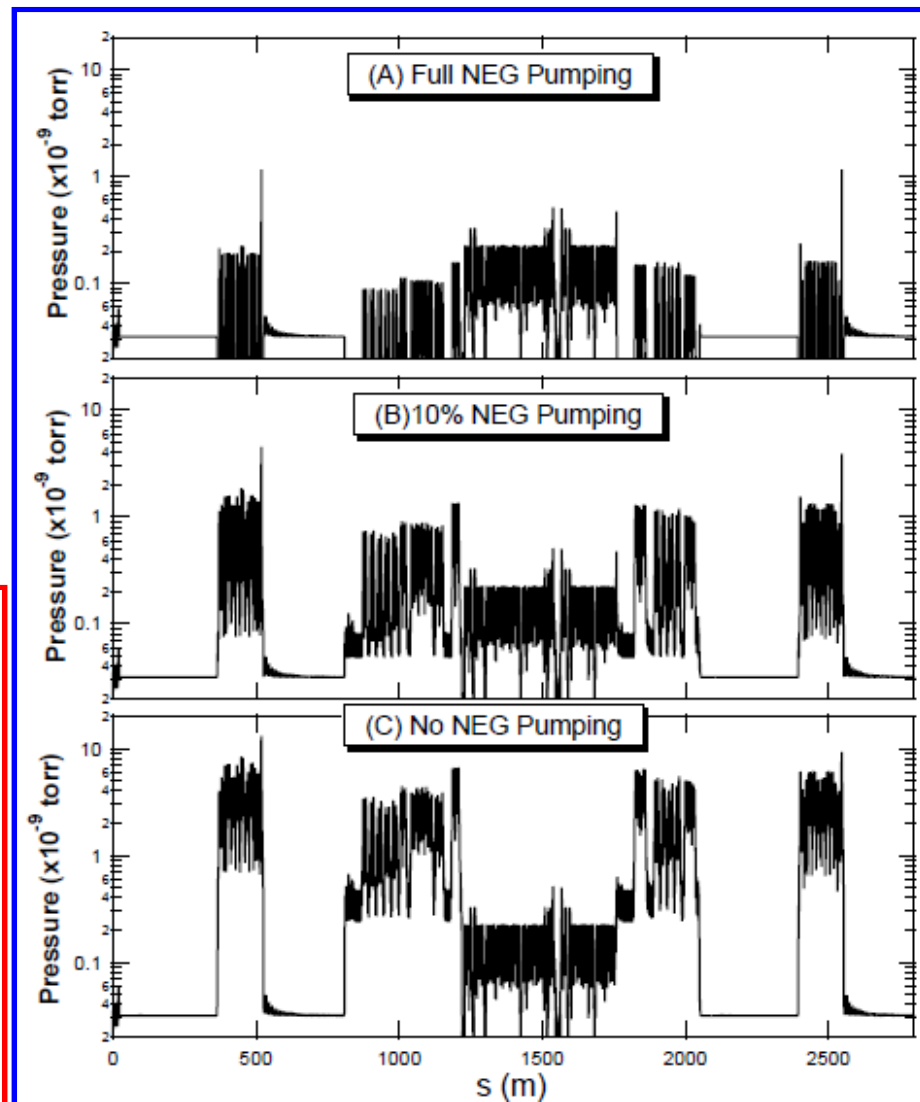
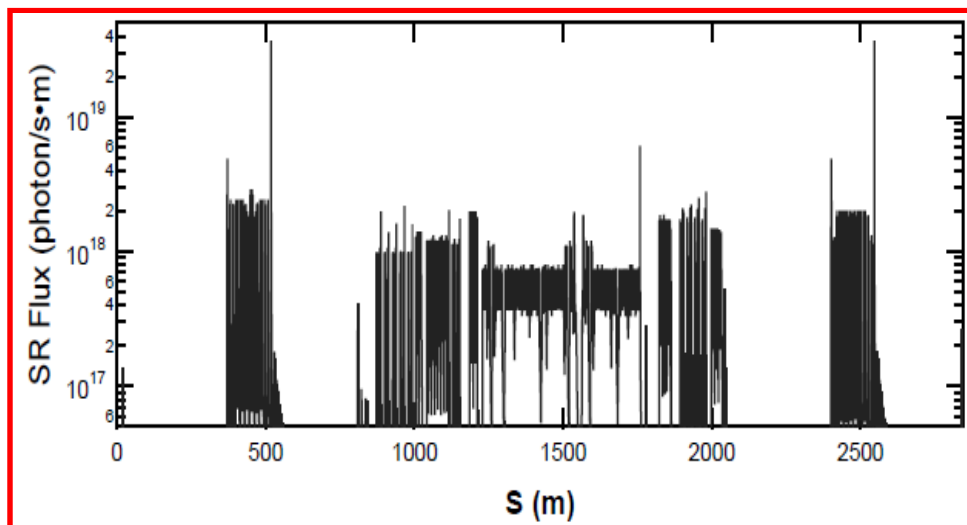
'Pin-out' sources of gas-induced detector radiation



Application – Cornell ERL Vacuum Design



- In conceptual design of Cornell ERL-based light sources, pressure profile calculations were carried out to ensure adequate vacuum pumping (Ion pumps and NEG strips.).
- SYNRAD provided SR flux for 100 mA electron beam at 5 GeV.
- Thermal outgassing and SR-induced gas-load (SR yield of 10^{-6} mol/ph) included in calculation.



Pressure Profile Calculation – Limitations



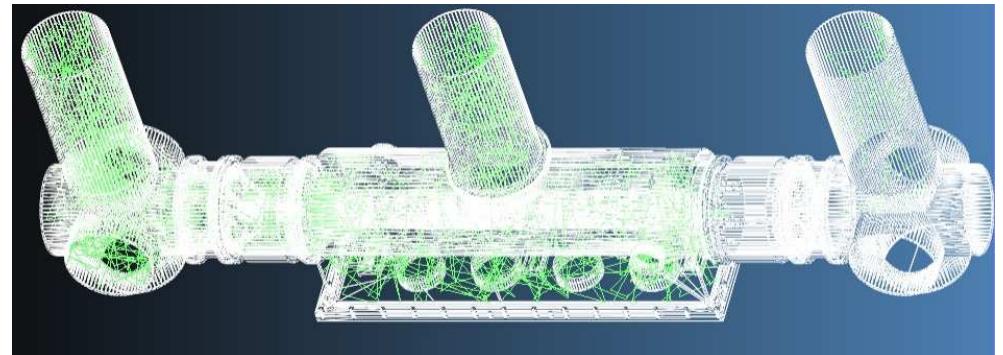
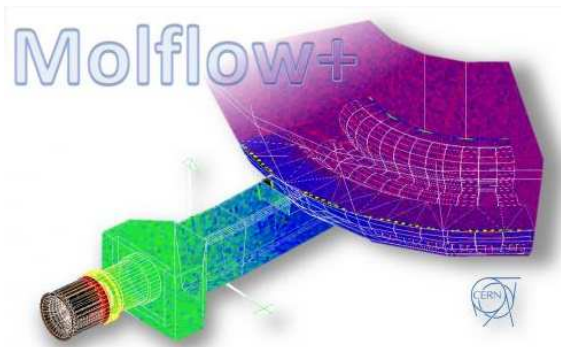
- ❑ *Results from one dimensional pressure profile calculations should be used with caution, though they are valuable design tools. It is most suitable for vacuum system with true uniform cross-section.*
- ❑ *The accuracy of the results heavily depends on the calculation of the specific gas conductance. Even for simple cross sections (such as round and rectangular), often the used conductance is over-estimated, as the 'beaming' effect of continuous 'slices' of 'elements' is not considered.*
- ❑ *For complex beam pipe cross sections, Monte-Carlo methods are used to compute gas conductance.*
- ❑ *Another source of errors is in the estimation of gas loads, particularly the dynamic gas load, such as SR-induced desorption. Though it is relatively straight forward in calculating SR flux impinging on walls, the desorption yield is 'history' and spatially dependent.*



MOLFLOW+ – Test Particle Monte-Carlo

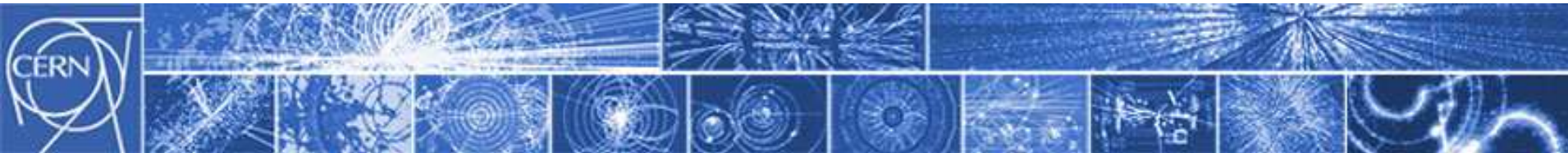


- *The TPMC method consists of calculating a large number of molecular trajectories in order to get a picture of a rarefied gas flow.*
- *Walls of a vacuum system are divided into planar facets. Test particles 'bounce' off facets with a cosine distributions, and continue be tracked until they exit the system, or into pumps. The facets can be assigned as pumps (with a sticking coefficient) or as gas sources.*
- *TPMC is best for computation of molecular flow conductance, but it can also generate 3D pressure profiles.*
- *Though the author (Roberto Kersevan) continues to improve the user-interface, MOLFLOW+ is still very difficult to use, and extremely time-consuming in initial setup.*



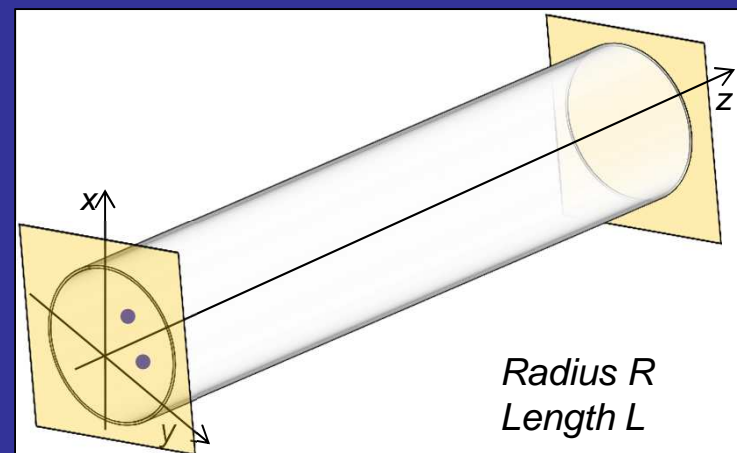
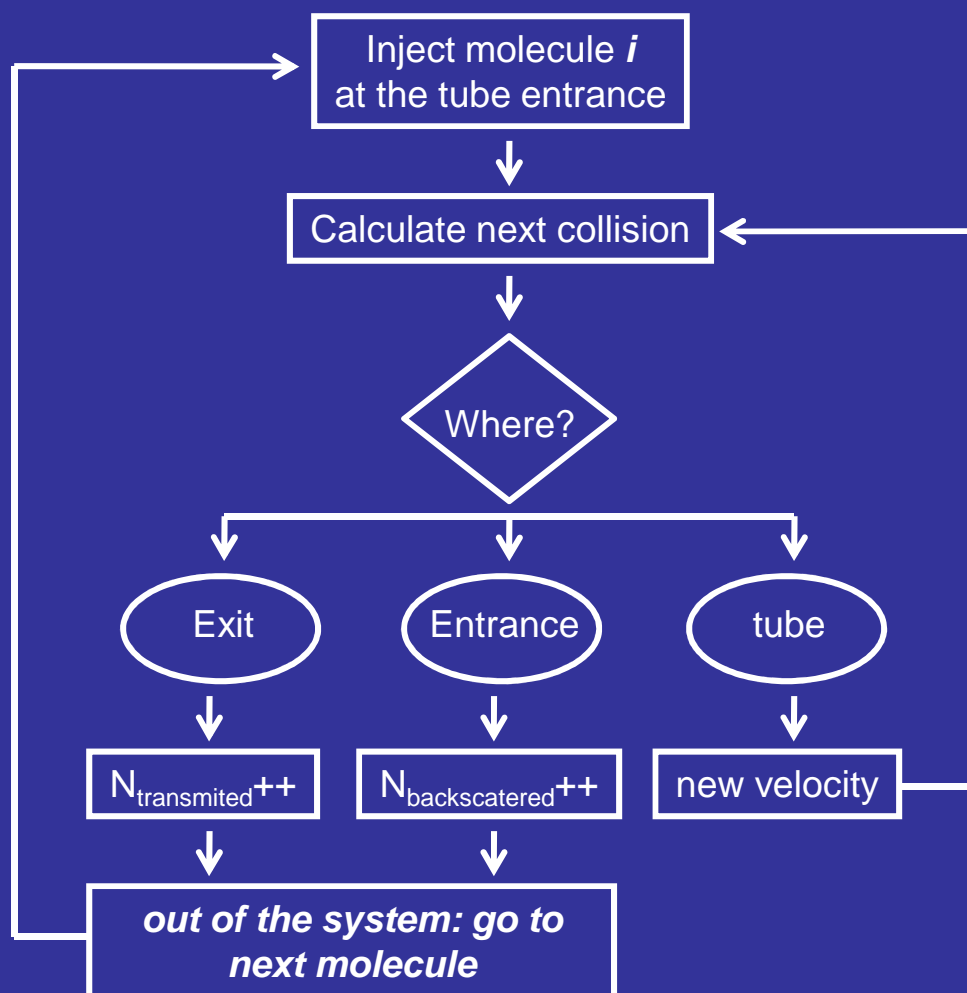
REF: R. Kersevan and J.-L. Pons, JVST A 27(4) 2009, p1017

*The Following Slides are Courtesies of
Roberto Kersevan of CERN,
the Author and the developer of
MOLFLOW and MOLFLOW⁺*



The Test Particle Monte Carlo: how does it work?

Calculate the molecular transmission probability of a tube.



Transmission probability:

$$\alpha = \frac{N_{transmited}}{N_{total}}$$

backscattering probability:

$$\beta = \frac{N_{backscattered}}{N_{total}}$$

Standard deviation:

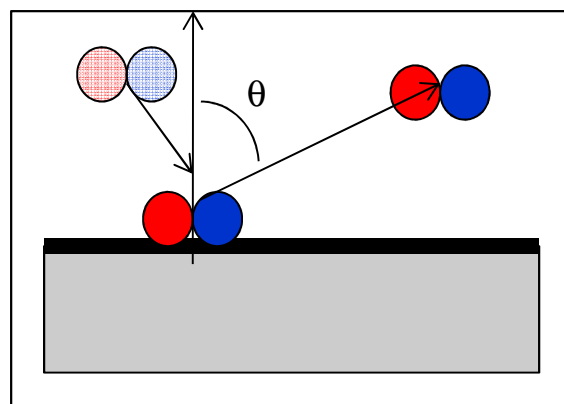
$$\sigma_{\alpha} = \sqrt{\frac{\alpha \cdot (1 - \alpha)}{N_{total}}}$$

How Molecules Interact with a Wall



Adsorption

If adsorption time is long the molecule is pumped (getters, cold surfaces)



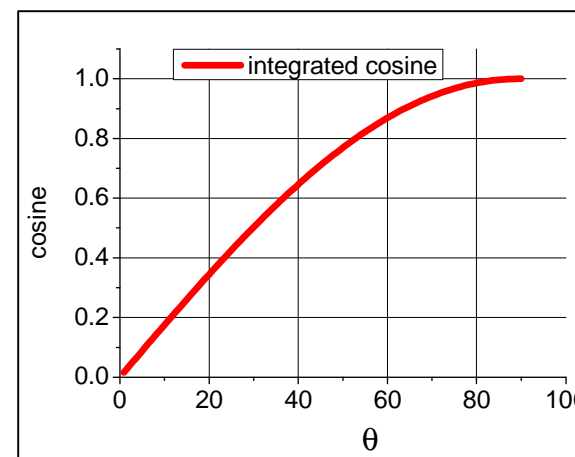
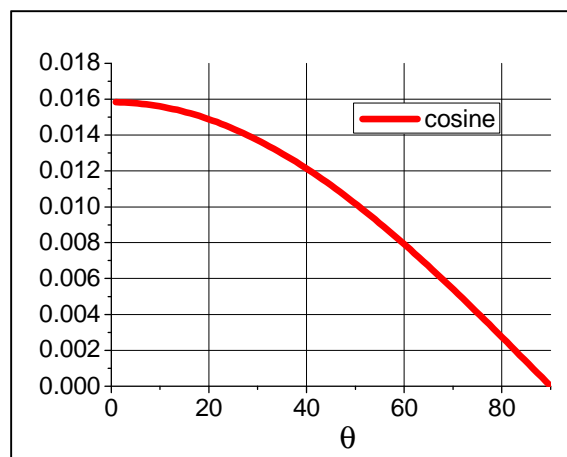
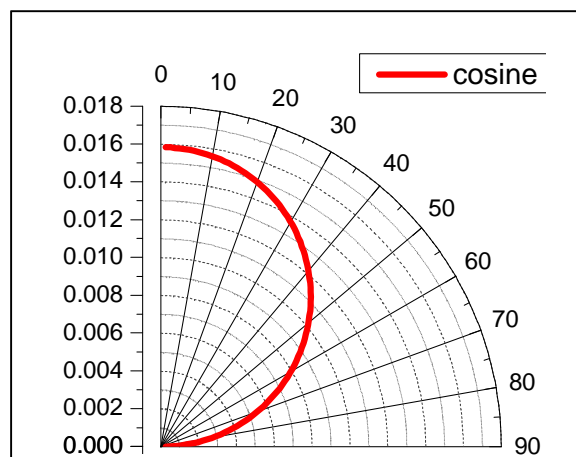
Desorption

If adsorption time is short ($\sim 10^{-11}$ s for physisorbed CO, N₂, O₂).

The angle of desorption, θ , is independent of the incident angle.

The “desorbed flux” follow the cosine law:

$$I(\theta) = I_0 \cos^n \theta \quad n \geq 1$$

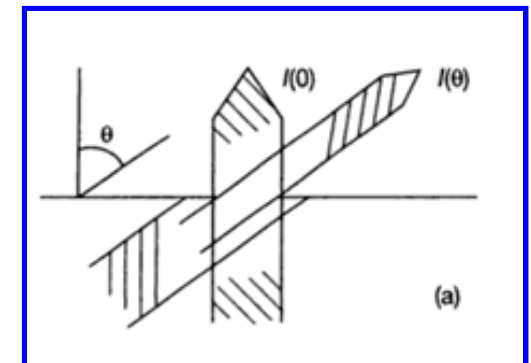
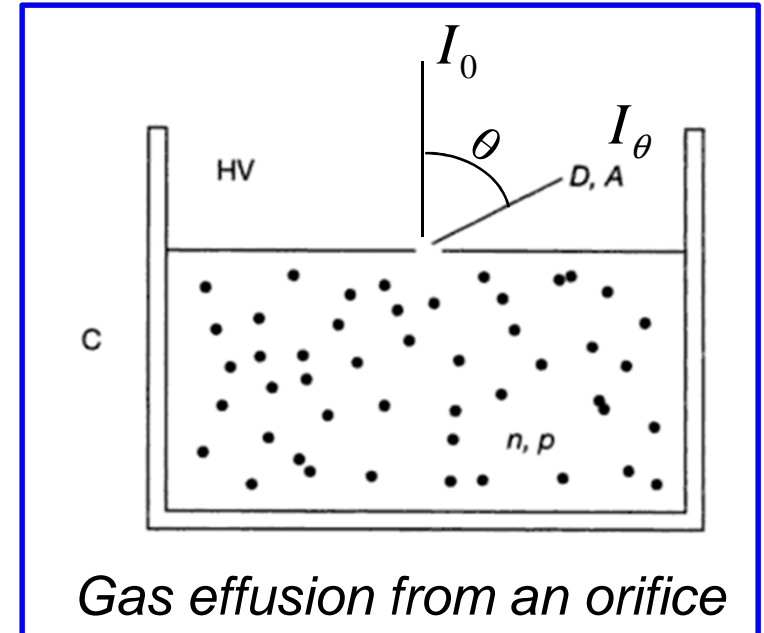


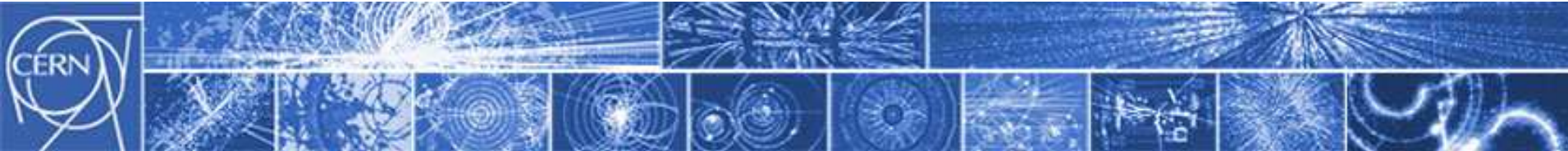
Knudsen's Cosine Law – Effusion



- ❑ Considering gas molecules exiting from a thin orifice (with area A). Assuming a much better vacuum above the orifice and a gas density below is in molecular flow region.
- ❑ The molecular flux (I_0) in the direction normal to the orifice is proportional to the density and the orifice area A .
- ❑ Assume that molecules exit the orifice isotropically, the flux (I_θ) at angle θ is also proportional to the density and a projected orifice area $A \cdot \cos\theta$. Thus, we have the Knudsen's cosine law of effusion:

$$I_\theta = I_0 \cos \theta$$





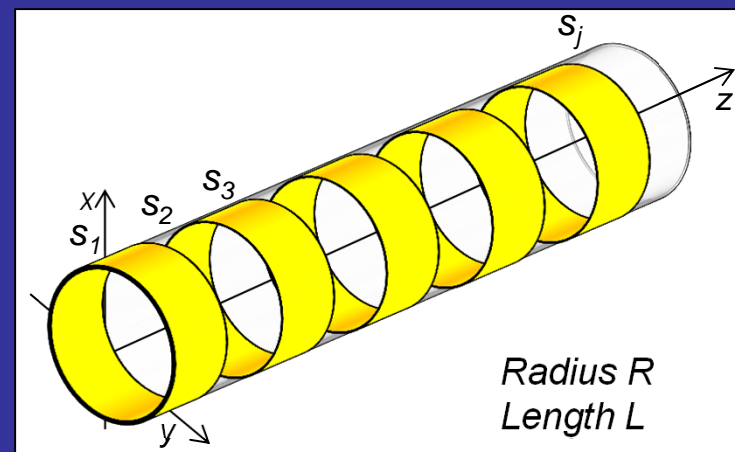
The Test Particle Monte Carlo: how does it work?

Calculate the transient pressure profile in a tube.

Define the sectors where the pressure must be computed (pressure counters);

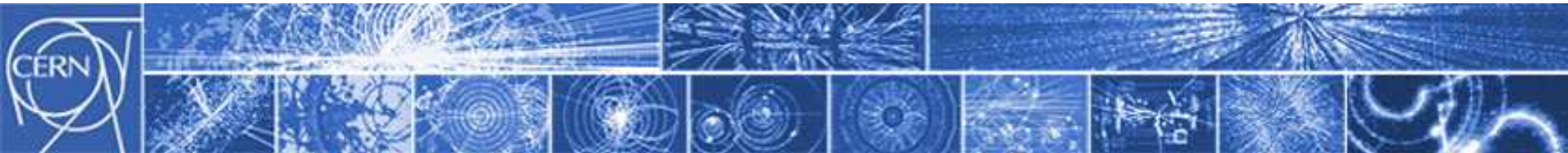
Define sampling time (time for which we want to get the pressure profiles) :

$$t_{\text{sampling}}[] = \{t_1, t_2, \dots, t_k\}.$$



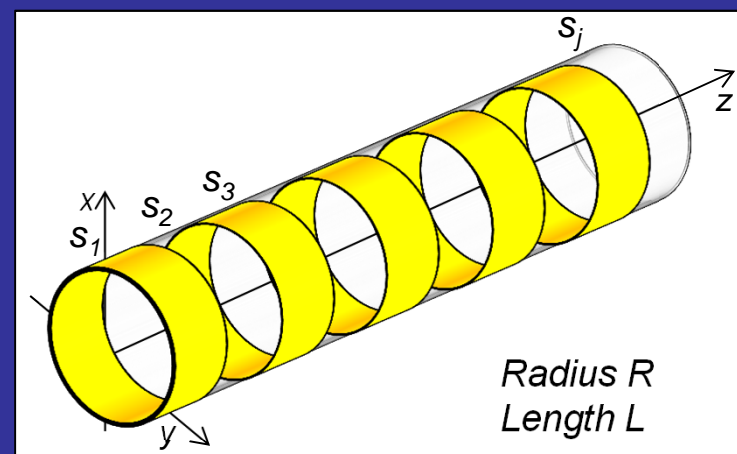
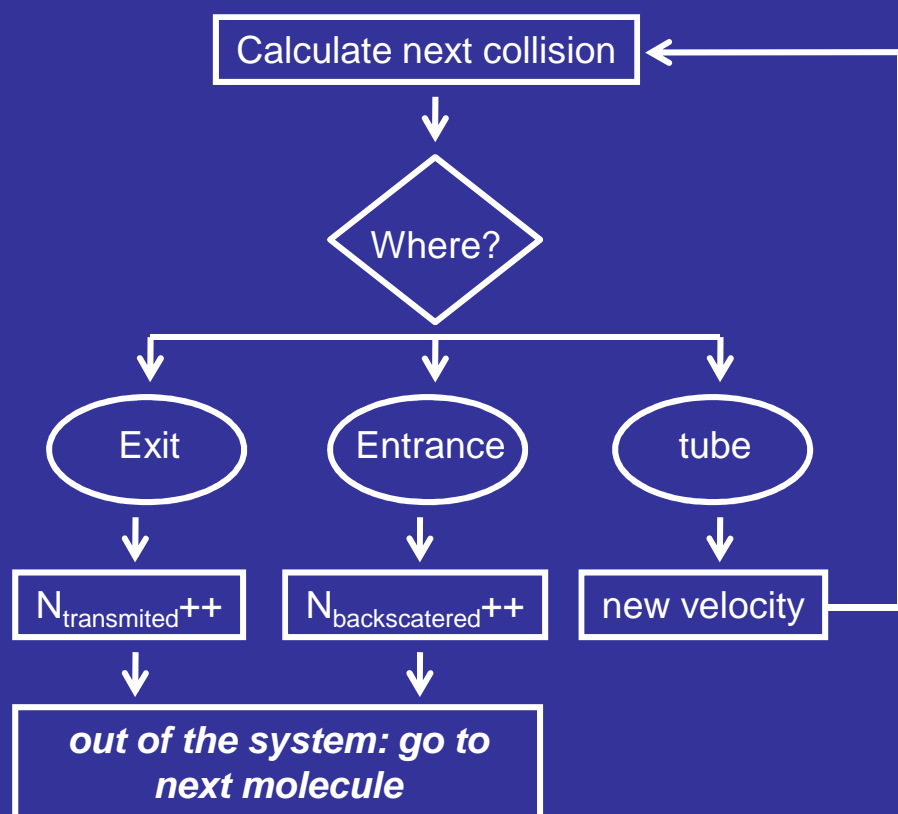
Inject molecules, calculate next interaction, (as for the transmission probability case), and for each time $t_{\text{sampling}}[]$ update pressure counters.

$$p_i = \frac{N_{\text{sim},i} f}{V_i} k_b T, \quad f \text{ is the scaling factor } f = \frac{N_{\text{real}}}{N_{\text{sim,total}}}$$



The Test Particle Monte Carlo: how does it work?

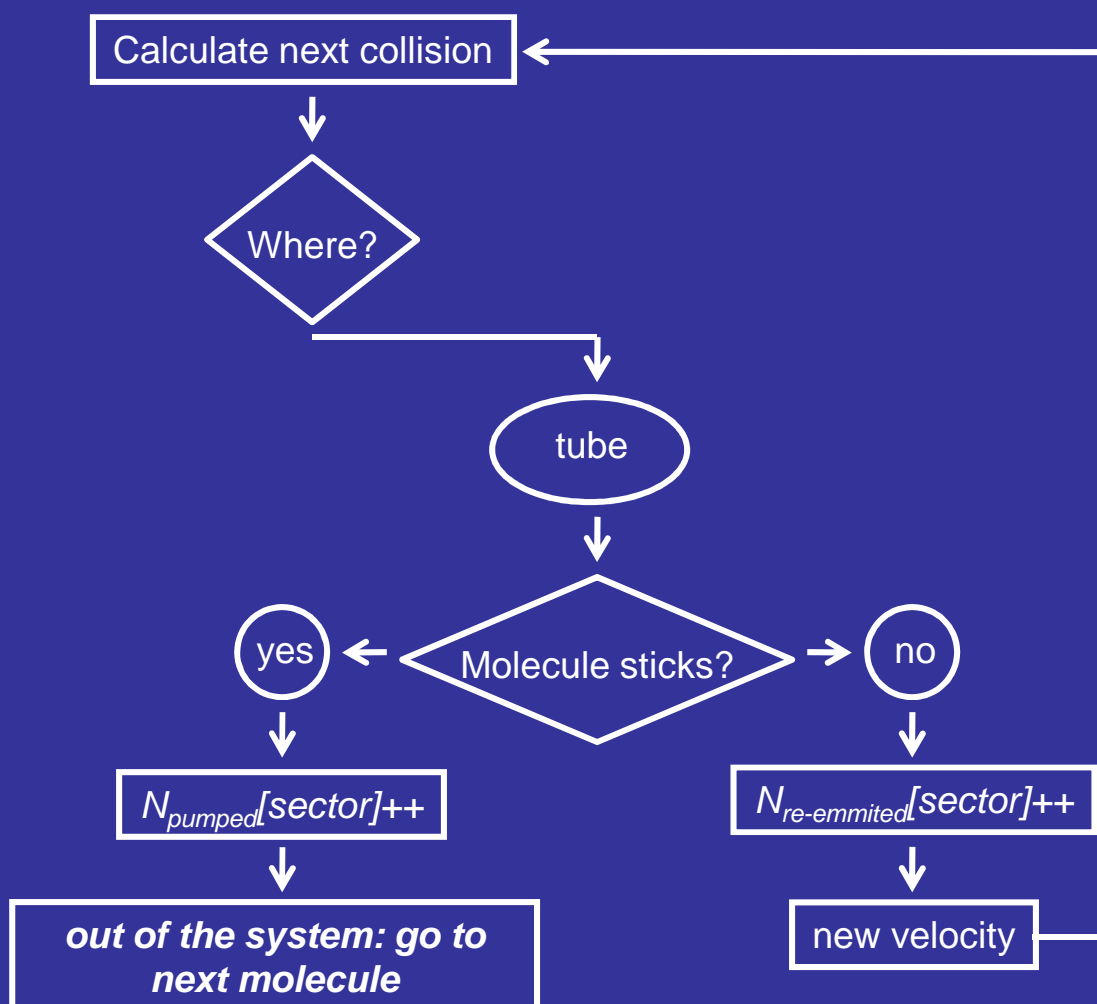
If surfaces have sticking probability? (getters, cold surfaces)





The Test Particle Monte Carlo: how does it work?

If surfaces have sticking probability? (getters, cold surfaces)



Molecule sticks?

If $Rnd() < s$ the molecule sticks
Else re-emitted

($Rnd()$ is a function to generate random numbers uniformly distributed in $[0, 1]$)

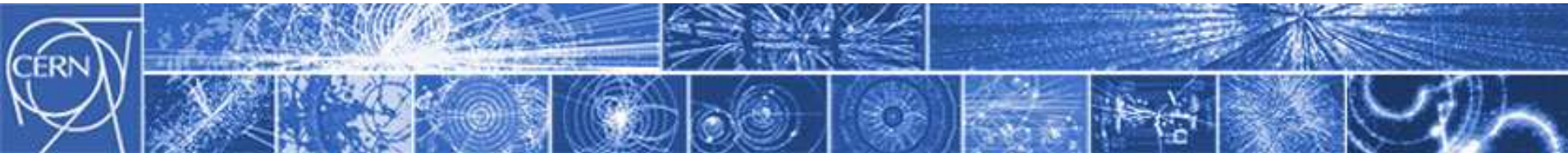
$N_{pumped}[sector]$ -> gives the distribution of the molecules pumped

$N_{re-emitted}[sector]$ -> gives the pressure profile (via the impingement rate)

$$v[sector] = \frac{N_{re-emitted}[sector]}{N_{total} \cdot A[sector]} \cdot \frac{Q}{kT}$$

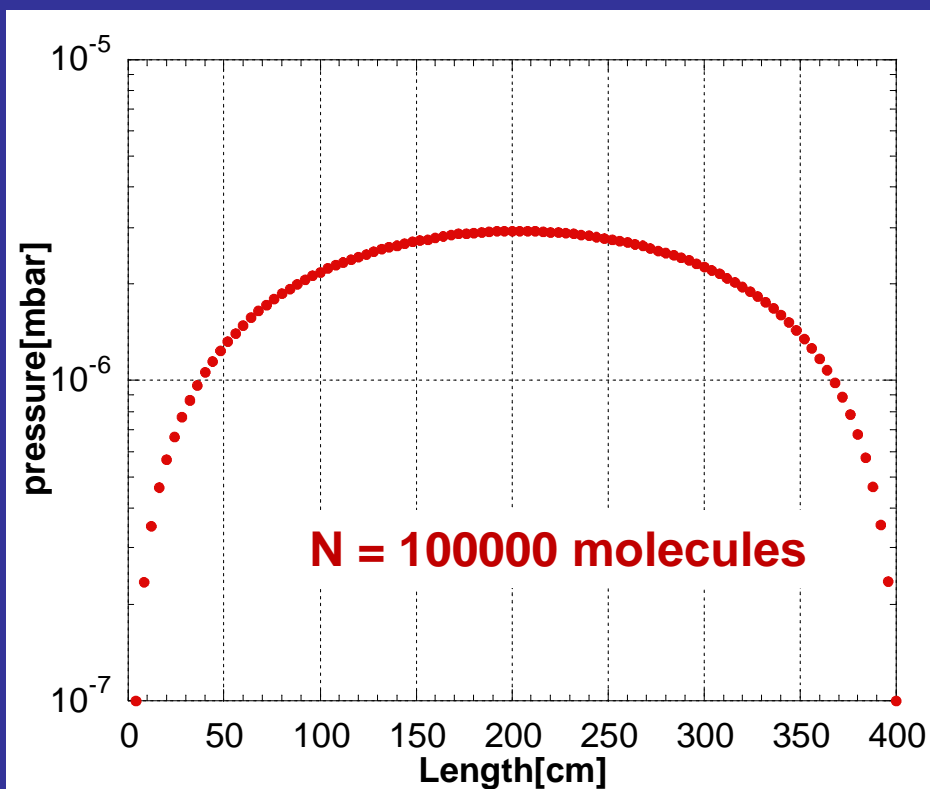
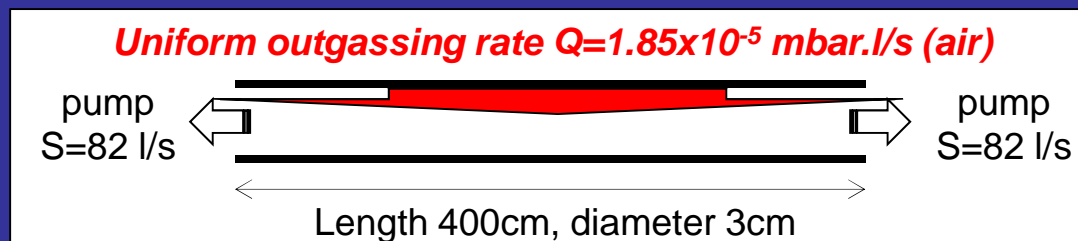
$$p[sector] = \frac{4kT}{v_a} v[sector]$$

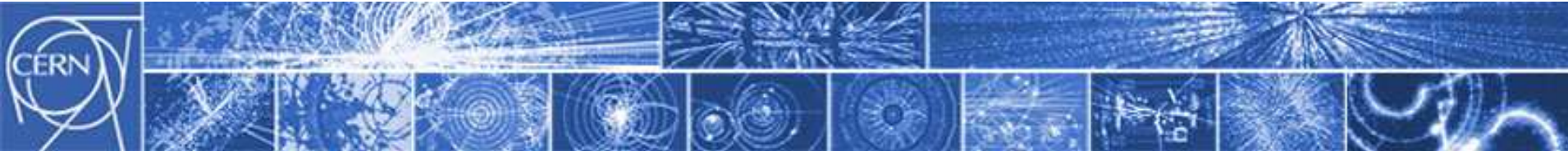
$$p[sector] = \frac{4Q}{v_a} \frac{N_{re-emitted}[sector]}{N_{total} \cdot A[sector]}$$



The Test Particle Monte Carlo: Examples.

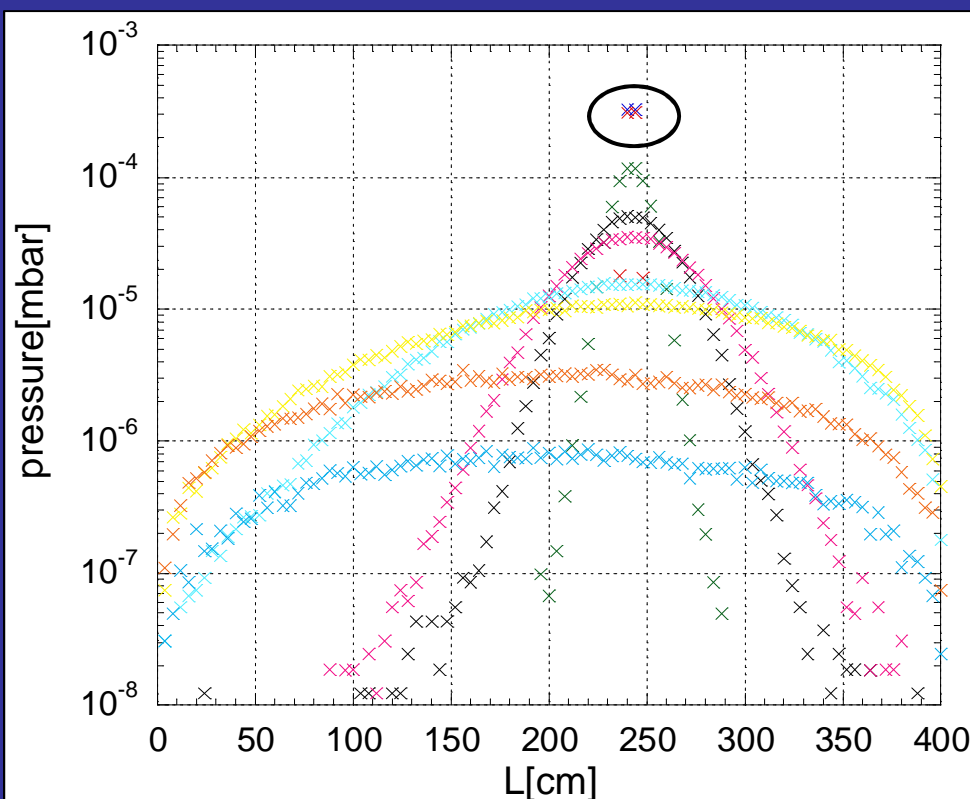
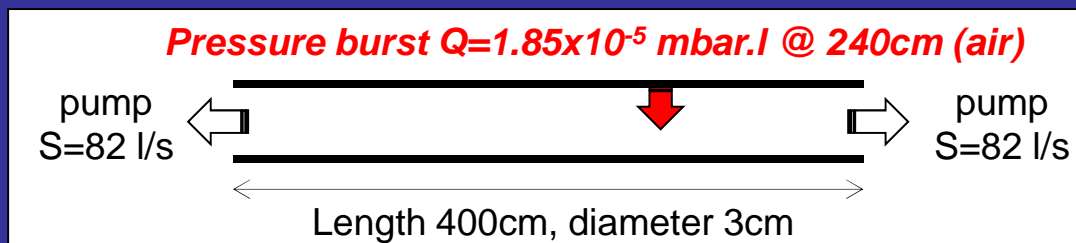
Steady state pressure profile in a tube





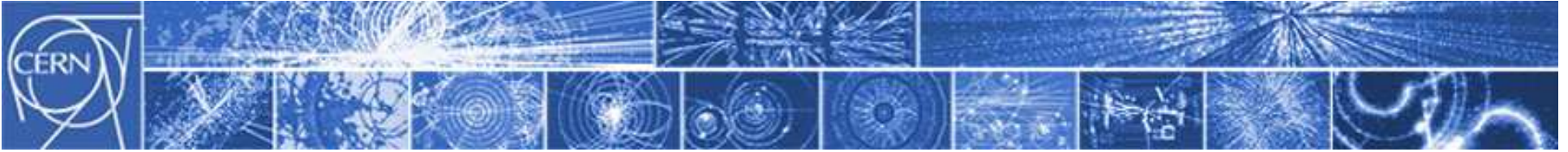
The Test Particle Monte Carlo: Examples.

Transient pressure profile after a pressure burst in a tube



1E-5s
 1E-4s
 1E-3s
 5E-3s
 1E-2s
 5E-2s
 1E-1s
 5E-1s
 1s

Length of sector = 4m/100
 Velocity air molecule at 25°C
 ~ 500 m/s
 Time to fly along a sector ~
 length / velocity = 8×10^{-5} s



The Test Particle Monte Carlo: if you don't want to write the code?.

MolFlow+

Written by **Roberto Kersevan** (former leader of the Vacuum group at ESRF; since July 2009 at ITER, now at CERN)

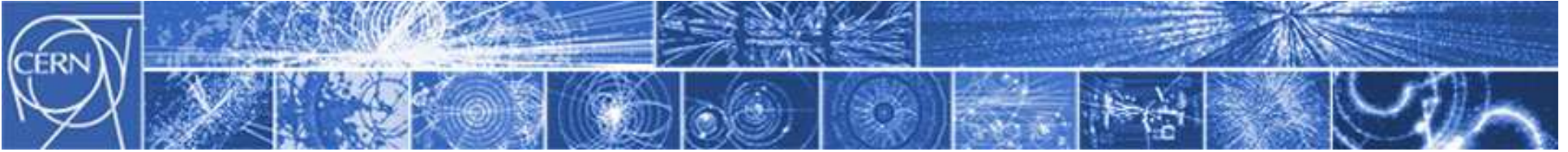
Developed since 1991, (started at CERN), in Turbo Pascal. used mainly in accelerators laboratories (Diamond Light Source, BNL, Elettra, Alba, Sesame, ASTeC, FermiLab, Cornell, and more). Old versions not very user friendly...

New version since 2008: written in C/C++ under Windows XP/ OpenGL, fast, optimized for **multi core CPUs** (parallelization)... **user friendly graphic interface**, but lacks a serious manual...

Geometries can be imported in 3D-CAD format (.STL, common to the main CAD programs)

The program can be obtained directly from the author:

Roberto Kersevan <roberto.kersevan@cern.ch>



The Test Particle Monte Carlo: if you don't want to write the code?.

MolFlow+

Procedure:

3D CAD drawing

**Import into Molflow+
(.STL)**

Attention: version 2.1 only accepts ASCII type .STL files

**Configure simulation
model:**

Define facets, desorption,
pumping, opacity, etc

Where the user spend more time: the .STL file loads surfaces built with triangles. The user must “collapse” some of this triangles by groups in order to define the usefull facets for the simulation. Less facets also means faster runs!

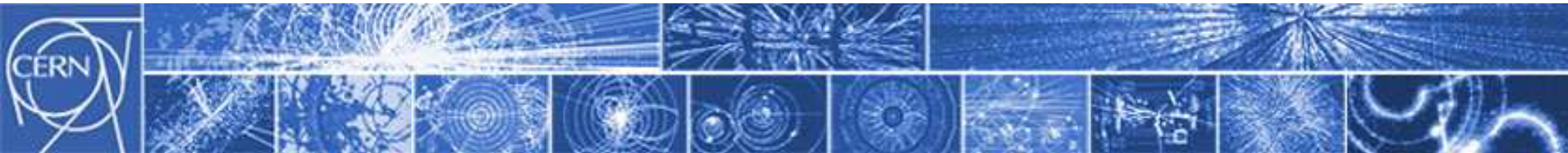
Define outputs:

Profiles: pressure, angular
distributions, formulas.

Pressure and angular profiles can be plotted for “real” facets or for “virtual” facets, (imposed to the model just for this purpose). For example, if we want to plot the pressure along the transversal plane of a tube.

RUN

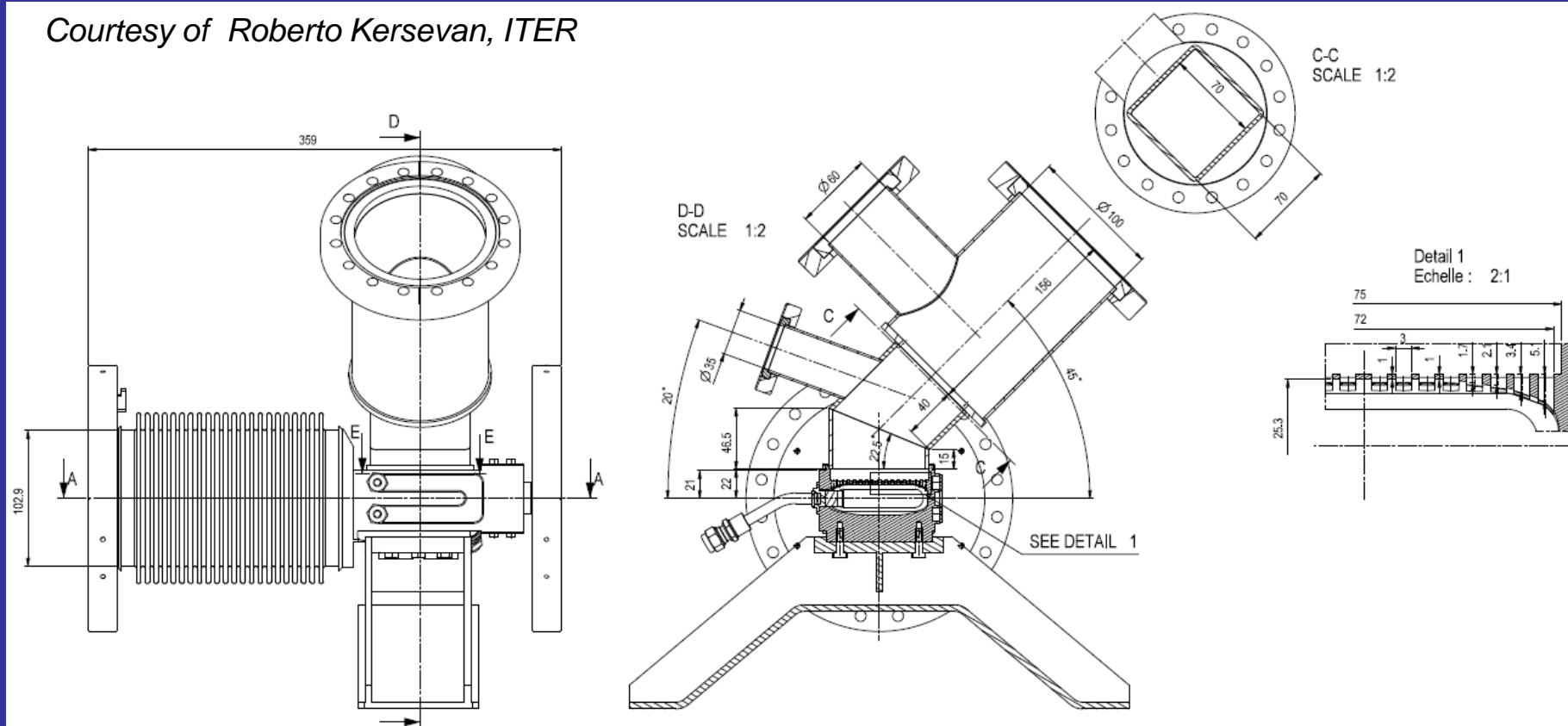
Practical results within a few seconds to hours, depending on geometry.
(1,550,000 hits/s in a 2.4GHz dual core CPU)

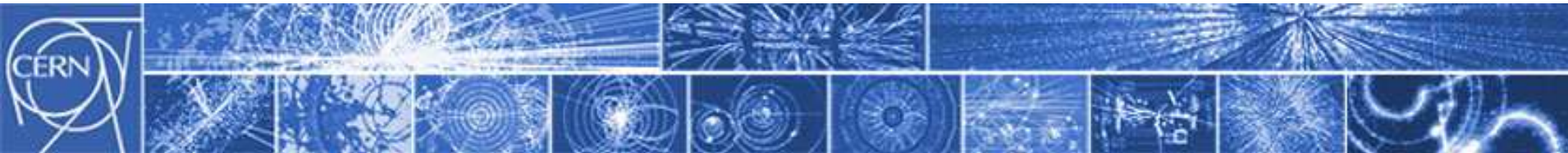


The Test Particle Monte Carlo: if you don't want to write the code?.

Example with **MolFlow+**: pumping port at ESRF

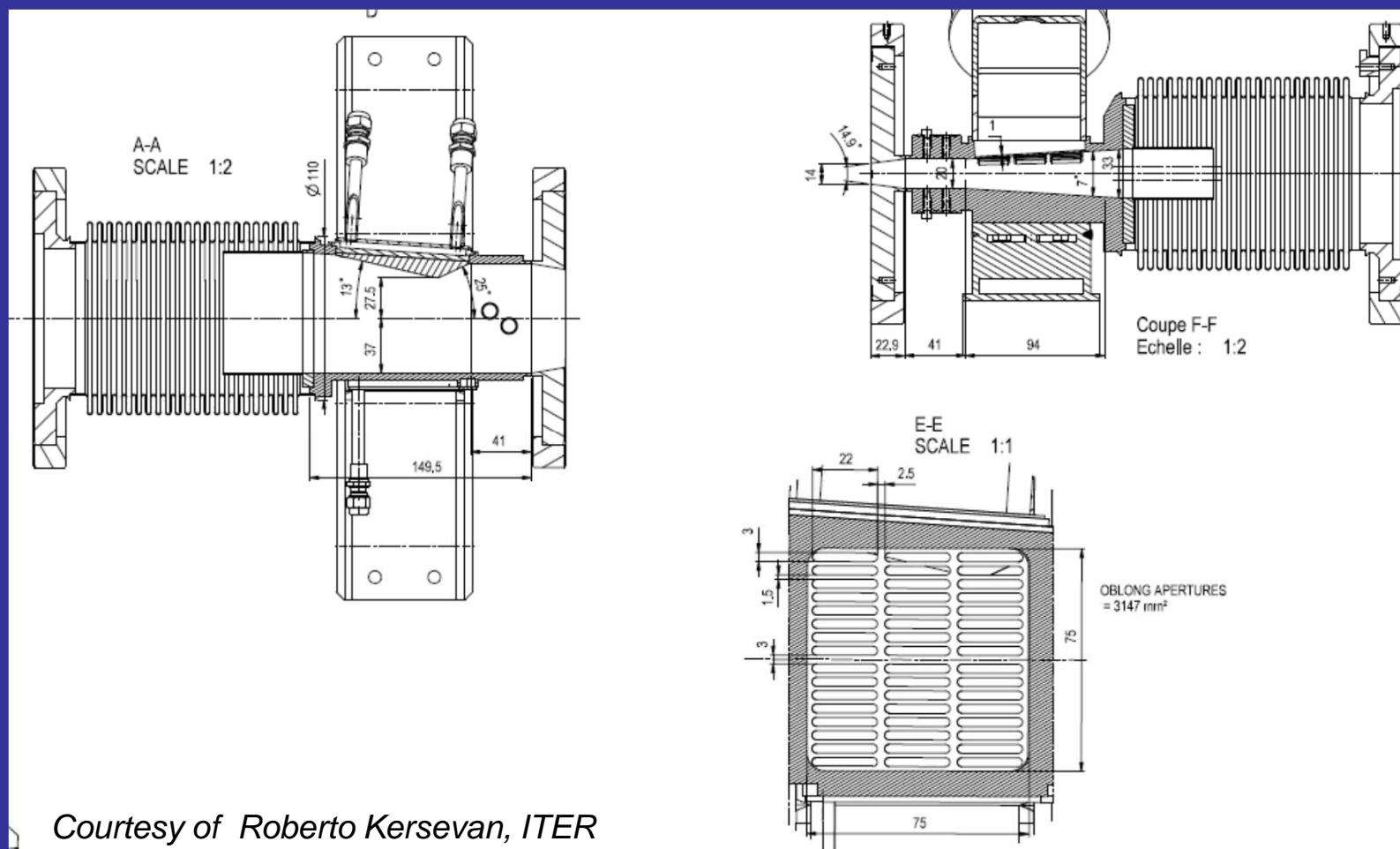
Courtesy of Roberto Kersevan, ITER



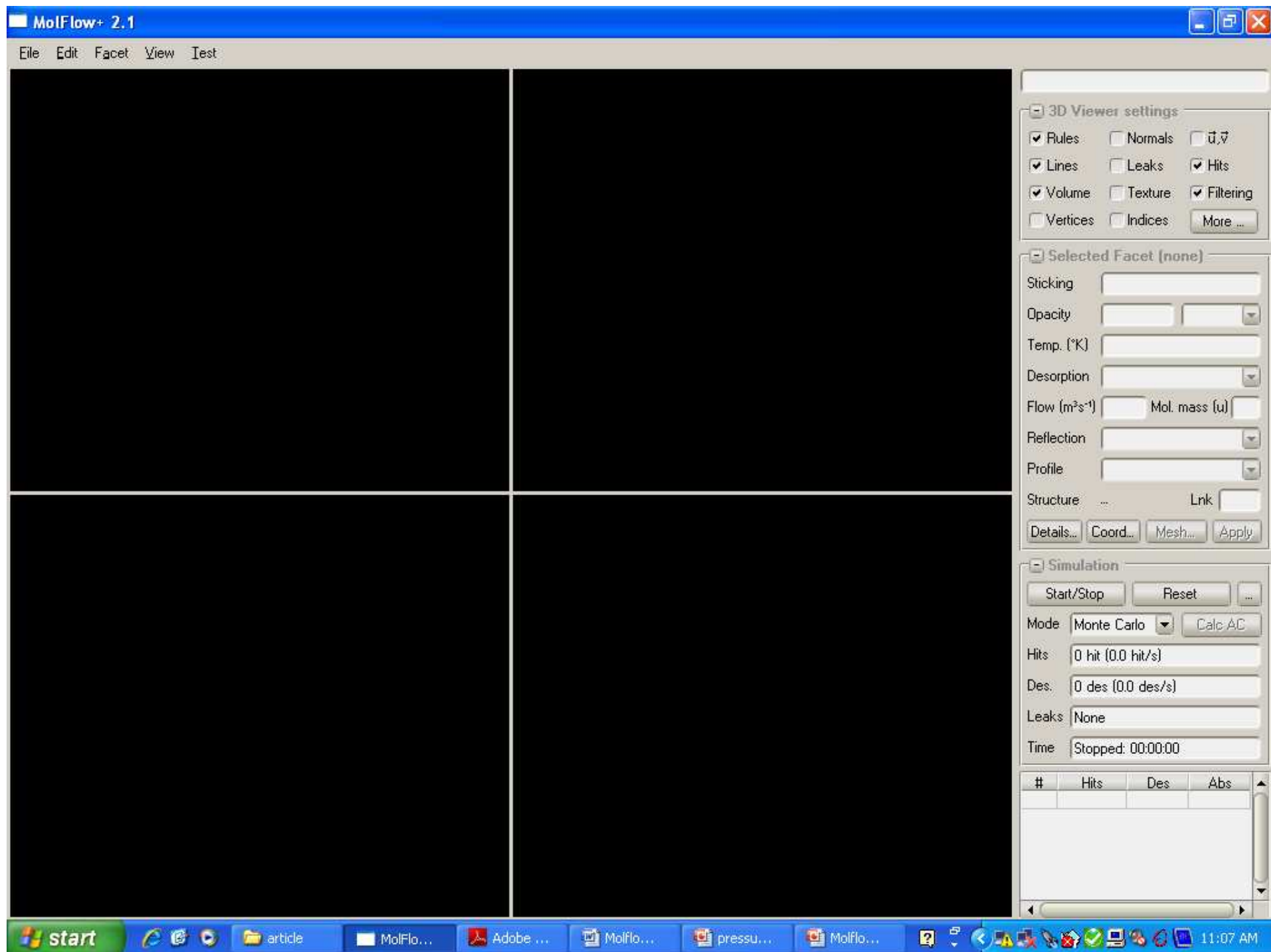


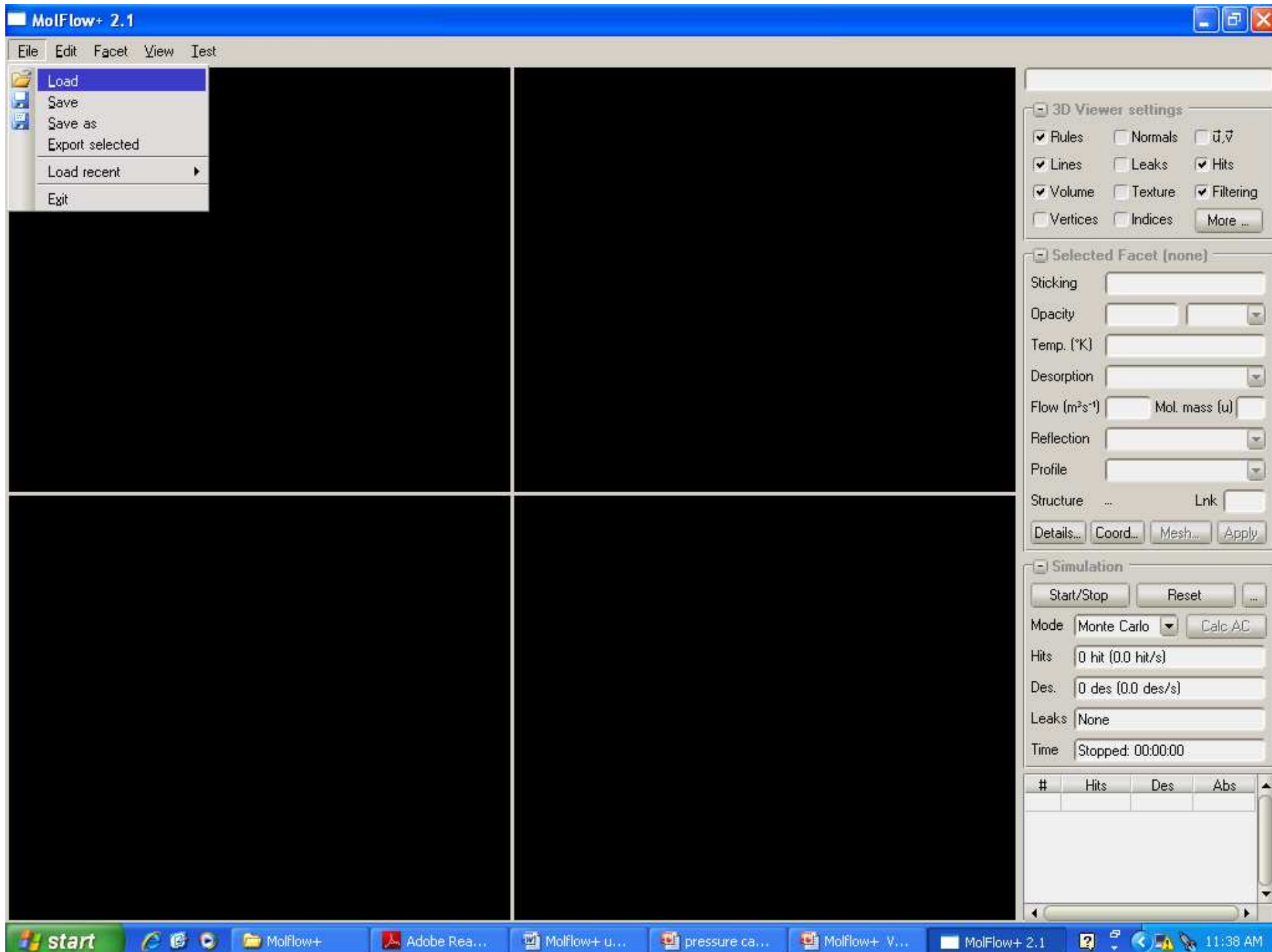
The Test Particle Monte Carlo: if you don't want to write the code?.

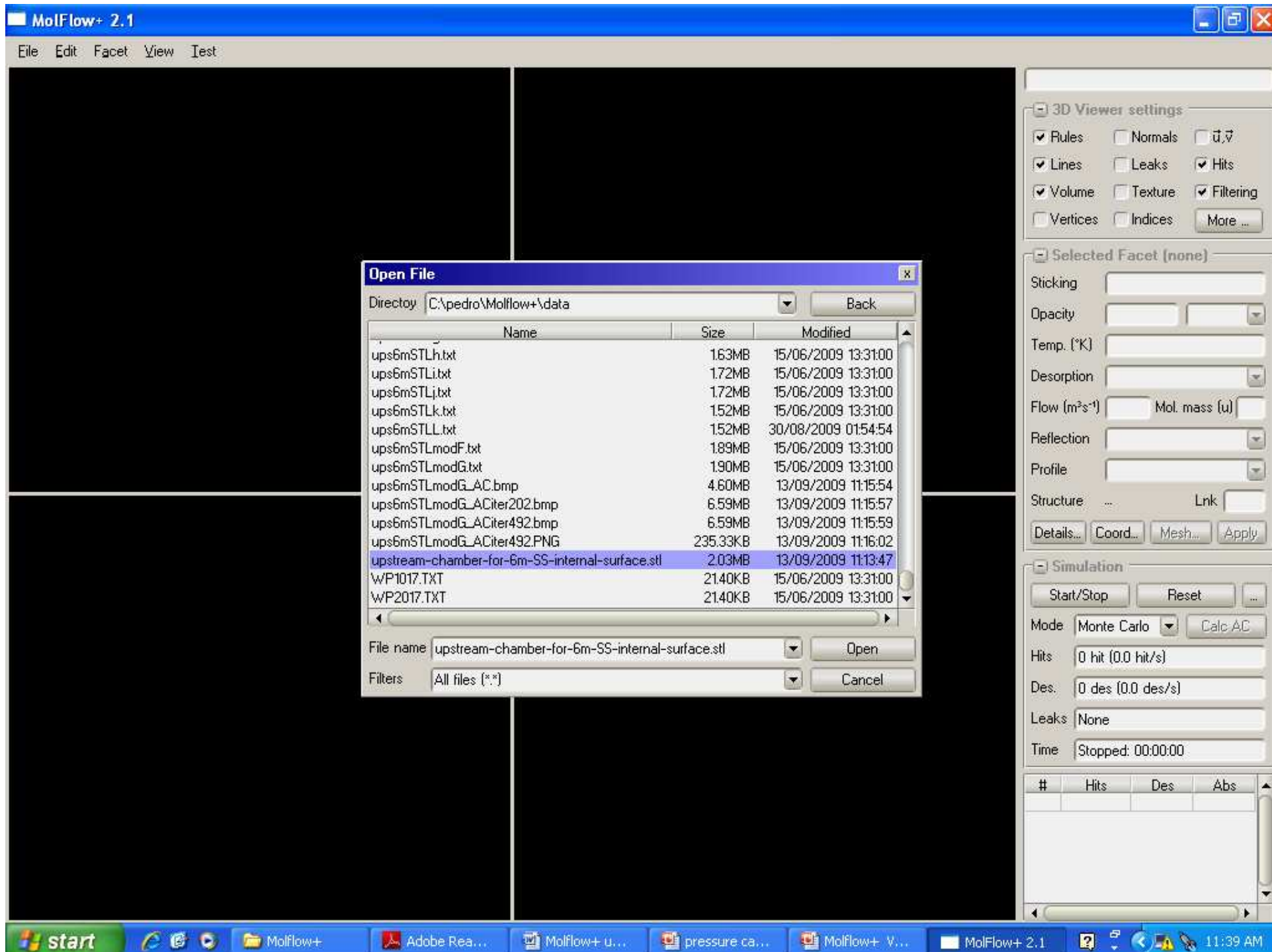
Example with **MolFlow+**: pumping port at ESRF

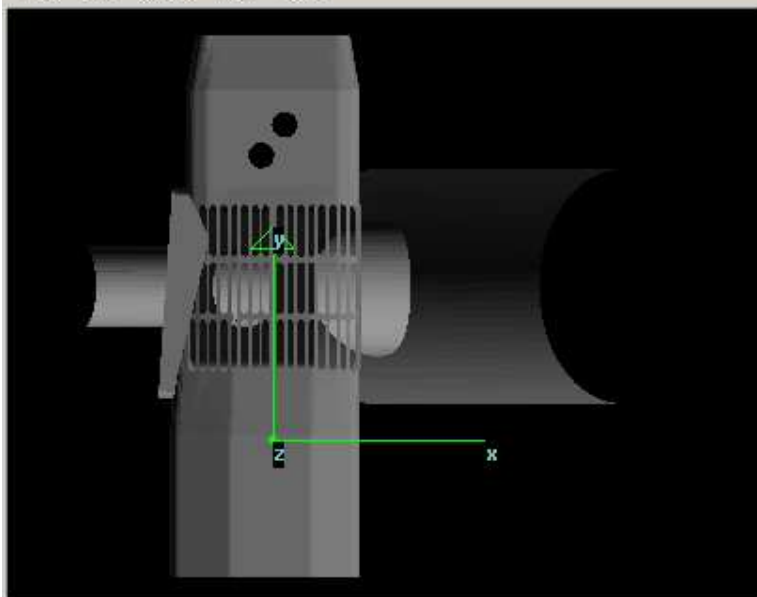


Courtesy of Roberto Kersevan, ITER

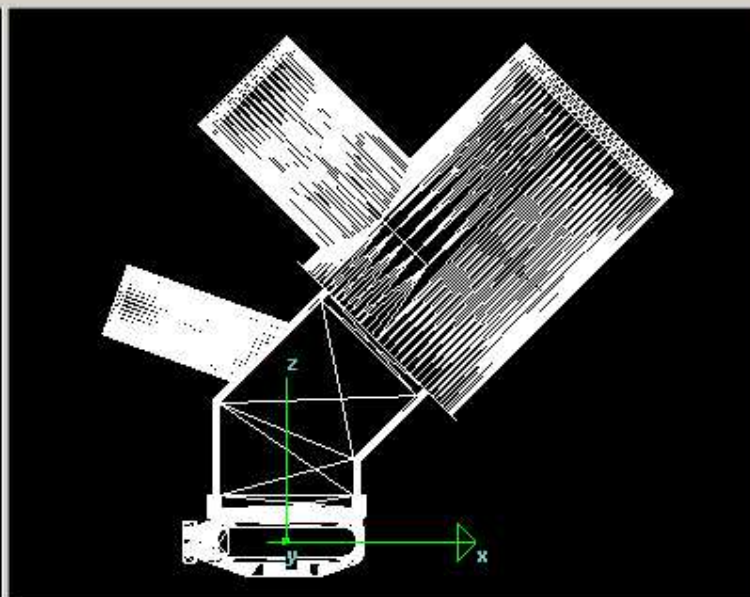




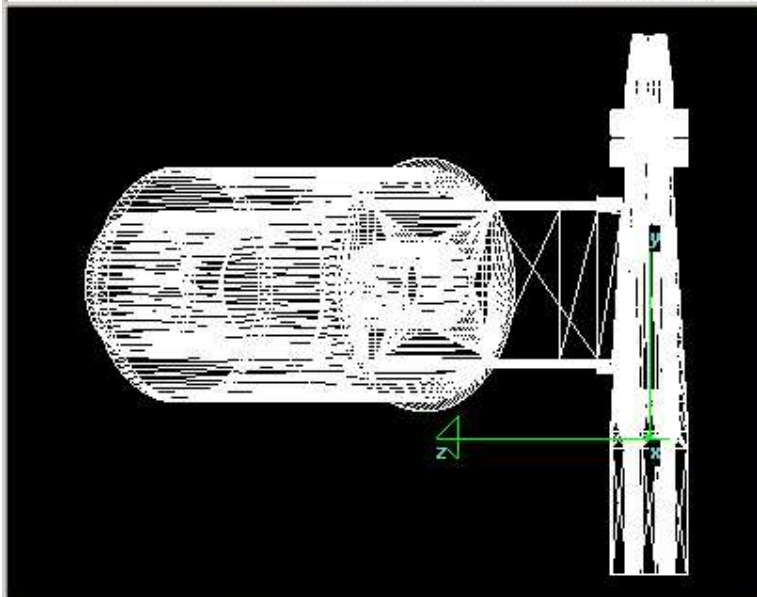




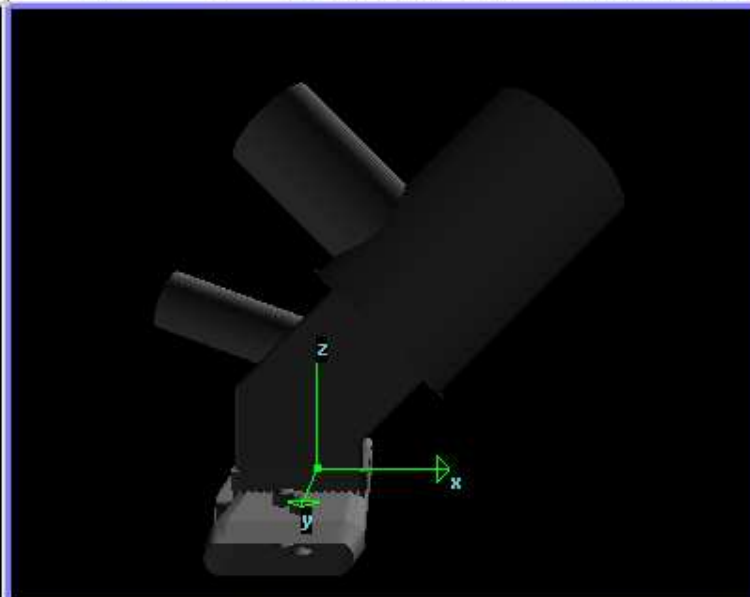
Front Top Side Ortho. X=154.134, Y=-55.3791



Front Top Side Ortho. X=-51.3888, Z=-14.138



Front Top Side Ortho. Z=-15.9289, Y=122.941



Front Top Side Persp.

V:22854 F:7618 Dim:(271.906,230.75,257.3)

3D Viewer settings

- ☒ Rules ☐ Normals ☐ \vec{u}, \vec{v}
☐ Lines ☐ Leaks ☒ Hits
☒ Volume ☐ Texture ☐ Filtering
☐ Vertices ☒ Indices

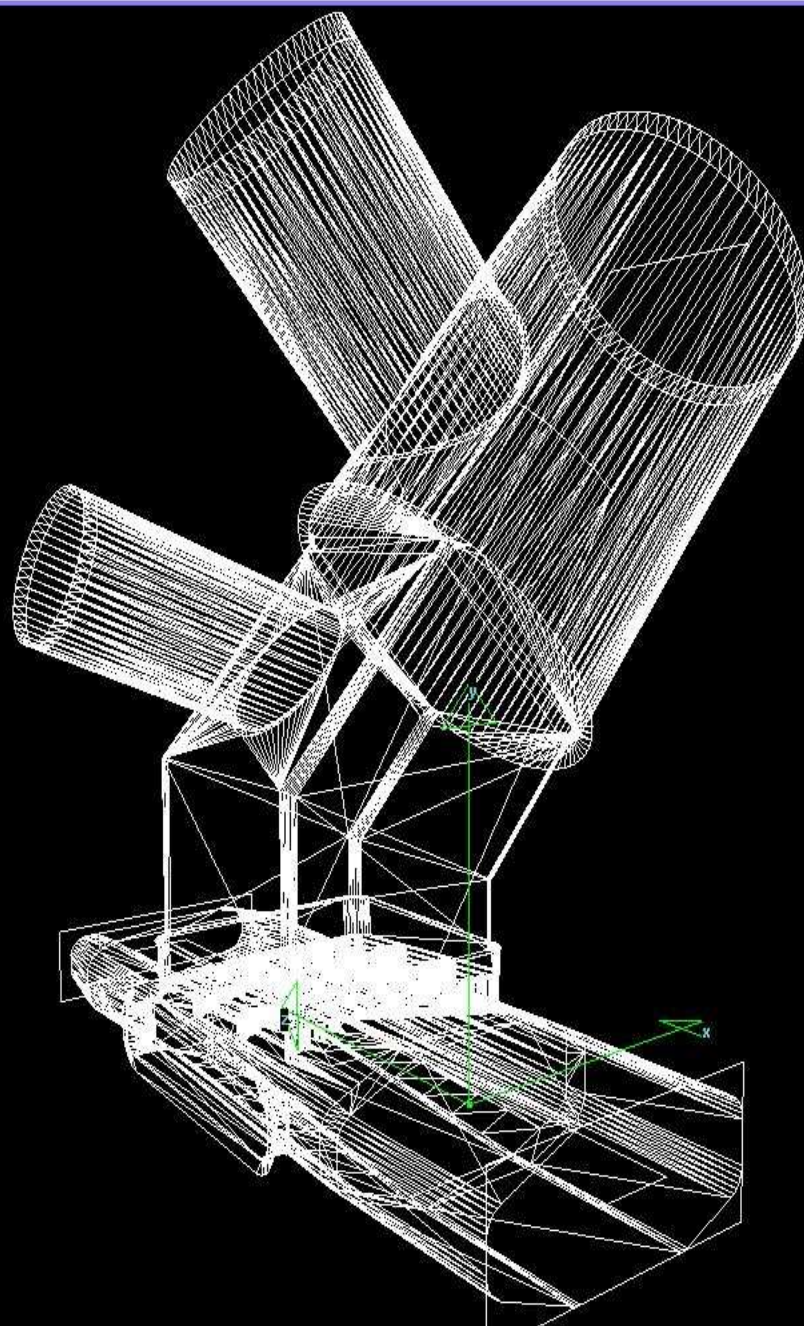
Selected Facet (none)

- Sticking
 Opacity
 Temp. (°K)
 Desorption
 Flow (m³s⁻¹) Mol. mass (u)
 Reflection
 Profile
 Structure ... Lnk

Simulation

- Mode
 Hits
 Des.
 Leaks
 Time

#	Hits	Des	Abs
341	U	U	U
342	0	0	0
343	0	0	0
344	0	0	0
345	0	0	0
346	0	0	0



V:4060 F:7295 Dim(271906,257,377,230)

3D Viewer settings

- ☒ Rules ☐ Normals ☐ U.V.
☒ Lines ☐ Leaks ☒ Hits
☐ Volume ☐ Texture ☐ Filtering
☐ Vertices ☐ Indices [More ...](#)

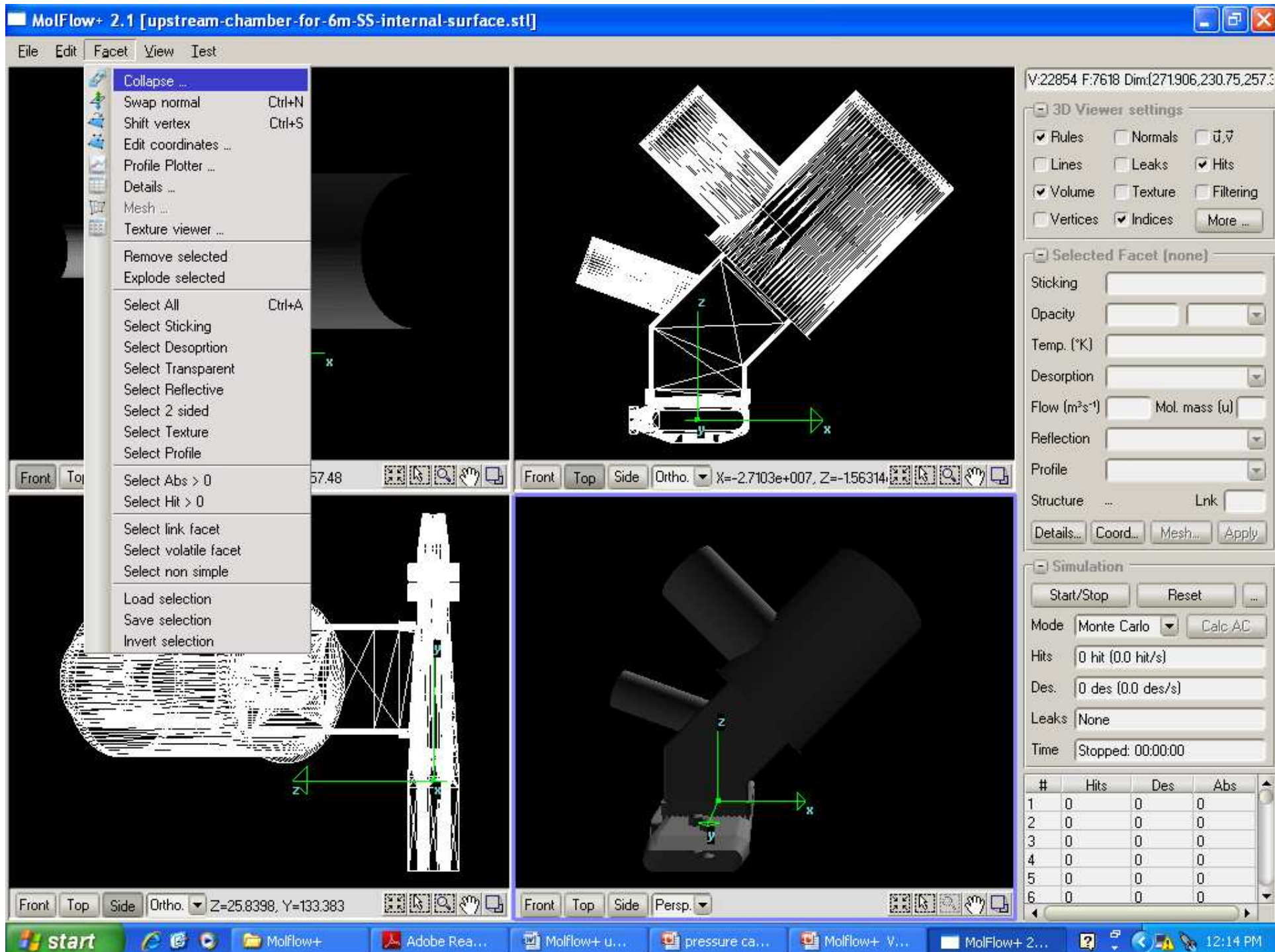
Selected Facet (none)

Sticking
Opacity
Structure ... Lnk ☐
Description
Reflection
Profile
[Details...](#) [Coord...](#) [Mesh...](#) [Apply](#)

Simulation

[Start/Stop](#) [Reset](#) ...
Mode: Monte Carlo
Hits: 3.75 Mhit (0.0 hit/s)
Des: 22.0 Kdes (0.0 des/s)
Leaks: None
Time: Stopped: 00:00:00

#	Hits	Des	Abs
3649	4628	0	0
3650	4918	0	0
3651	4588	0	0
3652	4931	0	0
3653	4689	0	0
3654	4873	0	0
3655	4663	0	0
3656	4884	0	0
3657	4602	0	0
3658	4701	0	0
3659	4707	0	0
3660	4838	0	0
3661	4683	0	0
3662	4935	0	0
3663	4666	0	0
3664	4934	0	0
3665	4644	0	0
3666	4839	0	0
3667	4691	0	0
3668	4865	0	0
3669	4638	0	0
3670	4862	0	0



MolFlow+ 2.1 [upstream-chamber-for-6m-SS-internal-surface.stl]

File Edit Facet View Test

3D Settings ... Ctrl+B
Texture scaling... Ctrl+D
Add formula ...

Front Top Side Ortho. X=-29.0053, Y=183.988

Front Top Side Ortho. X=-3.90434, Z=100.541

Front Top Side Ortho. Z=151.949, Y=183.988

Front Top Side Persp.

V:22854 F:7618 Dim(271906,230.75,257.3)

3D Viewer settings

☒ Rules ☐ Normals ☐ \vec{u}, \vec{v}
☐ Lines ☐ Leaks ☒ Hits
☒ Volume ☐ Texture ☐ Filtering
☐ Vertices ☒ Indices

Selected Facet (none)

Sticking
 Opacity
 Temp. (°K)
 Desorption
 Flow (m³s⁻¹) Mol. mass (u)
 Reflection
 Profile
 Structure ... Lnk

Simulation

...

Mode

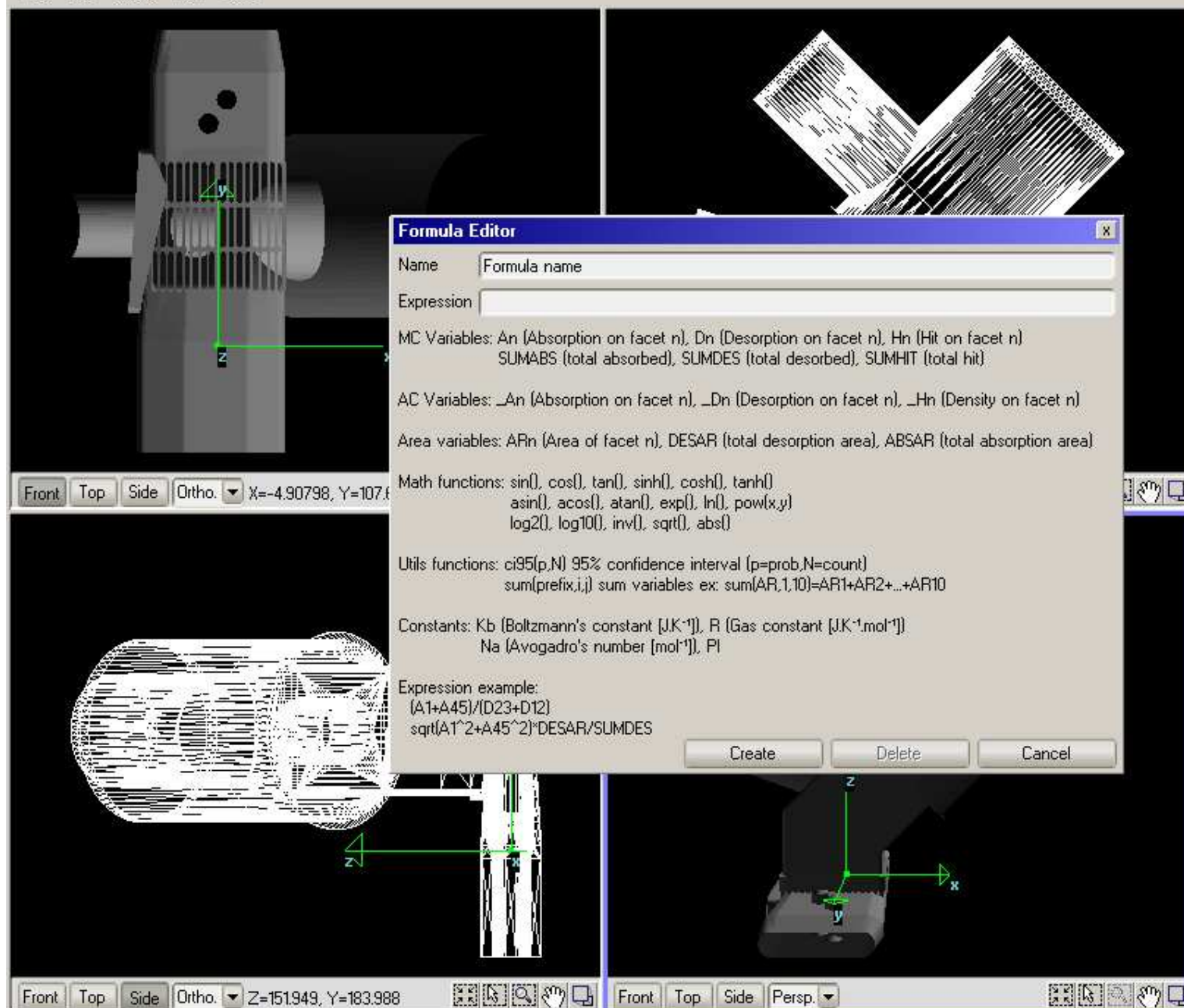
Hits
 Des.
 Leaks
 Time

#	Hits	Des	Abs
3498	0	0	0
3499	0	0	0
3500	0	0	0
3501	0	0	0
3502	0	0	0
3503	0	0	0

start

Molflow+ Adobe Rea... Molflow+ u... pressure ca... Molflow+ V... Molflow+ 2...

12:25 PM



V:22854 F:7618 Dim(271906,230.75,257.3

3D Viewer settings

☒ Rules ☐ Normals ☐ d.v

☐ Lines ☐ Leaks ☒ Hits

☒ Volume ☐ Texture ☐ Filtering

☐ Vertices ☒ Indices

Selected Facet (none)

Sticking:

Opacity:

Temp. (°K):

Desorption:

Flow (m³.s⁻¹): Mol. mass (u):

Reflection:

Profile:

Structure: ... Lnk:

Simulation

...

Mode: Monte Carlo

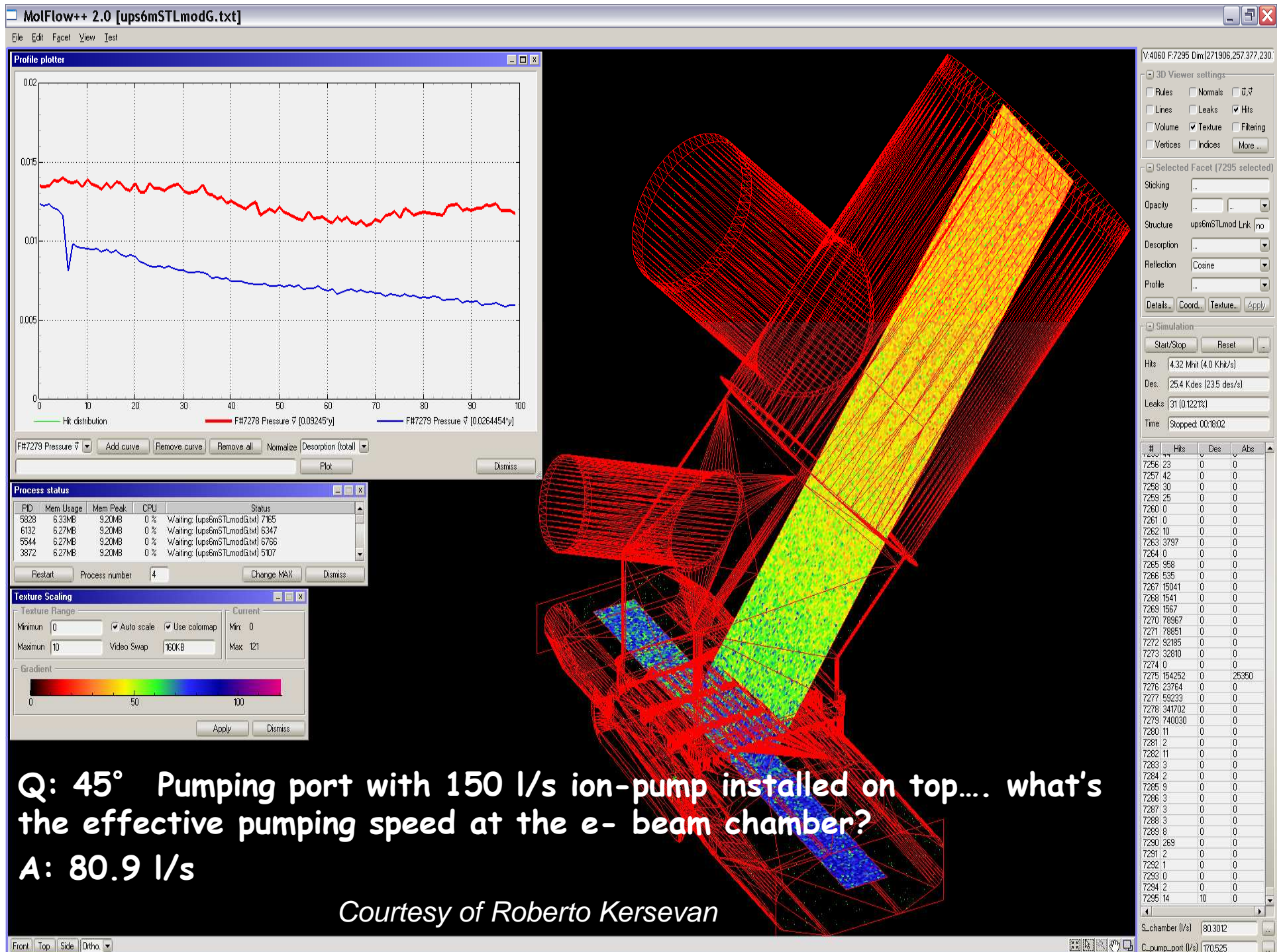
Hits: 0 hit (0.0 hit/s)

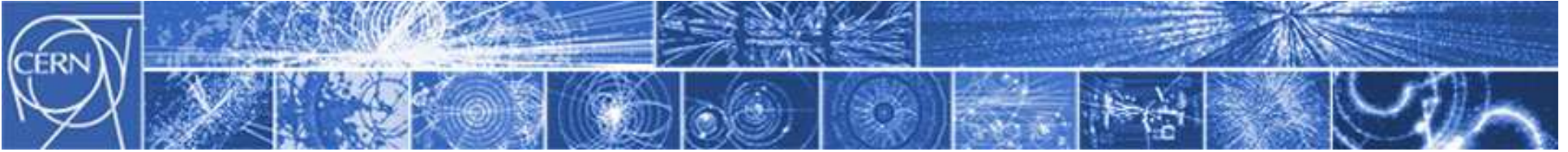
Des.: 0 des (0.0 des/s)

Leaks: None

Time: Stopped: 00:00:00

#	Hits	Des	Abs
3498	0	0	0
3499	0	0	0
3500	0	0	0
3501	0	0	0
3502	0	0	0
3503	0	0	0





The Test Particle Monte Carlo

Summary:

Simple physical basis: rectilinear movement of molecules in UHV, cosine like desorption, molecules move independently from each other.

Flow charts for the simulation are simple: do not require expert programmers to write a code for a dedicated simulation. (to work with 3D CAD files it's another story...)

Both steady state and transient regimes can be simulated with accuracy in 3D

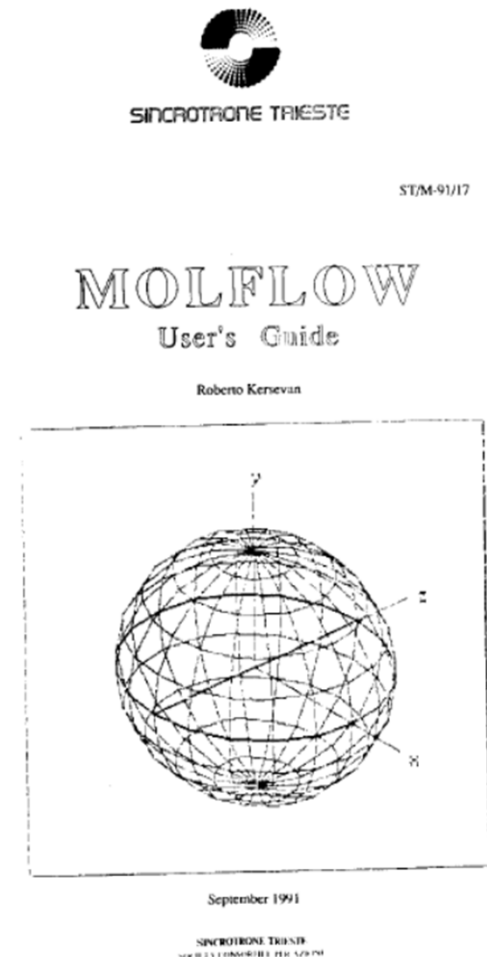
It is a statistical method: accuracy depends on the number of molecules tracked

Steady state simulation of 3D complex geometries, loaded from CAD files, can be done with **MolFlow+** in a user friendly environment.

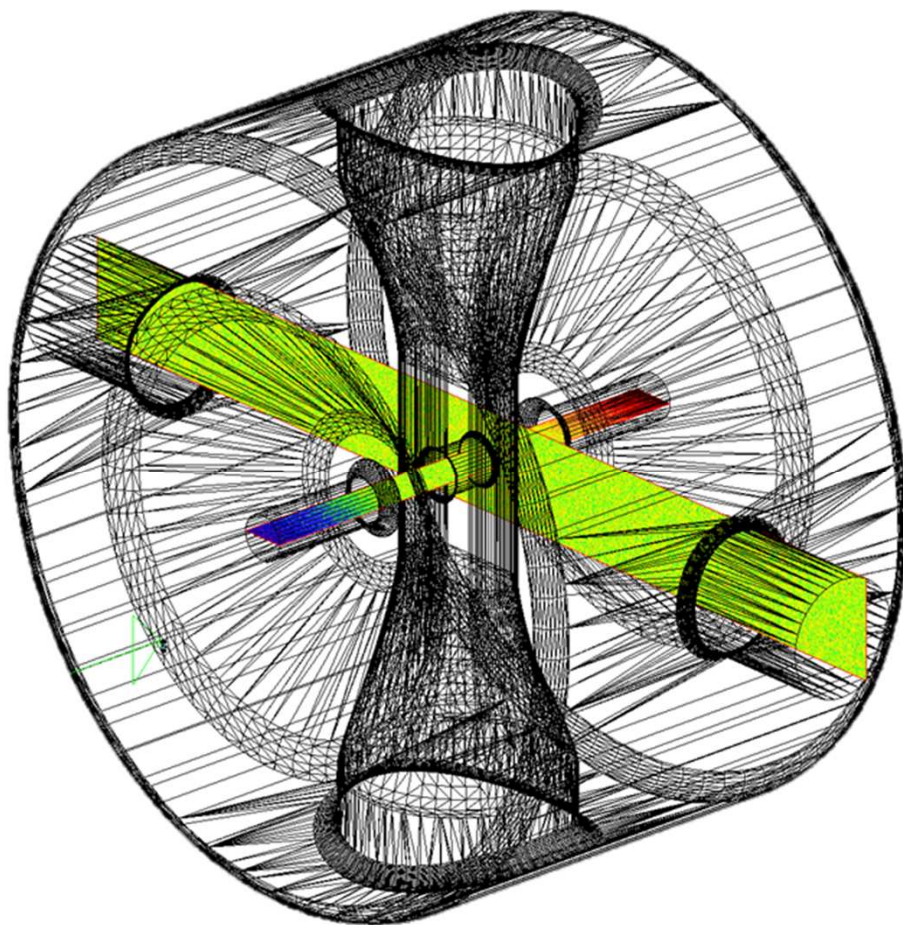
Transient simulation of 3D complex geometries, loaded from CAD files, can be done with FEM PROGRAMS, (slow), or with your own code...

Molflow 'History'

- Developed since 1991 (R. Kersevan)
- Turbo Pascal, 13.000 lines of code
- Used by:
 - Diamond Light Source
 - BNL
 - Elettra
 - Alba
 - Sesame
 - ASTeC
 - FermiLab
 - Cornell
 - ...
 - CERN

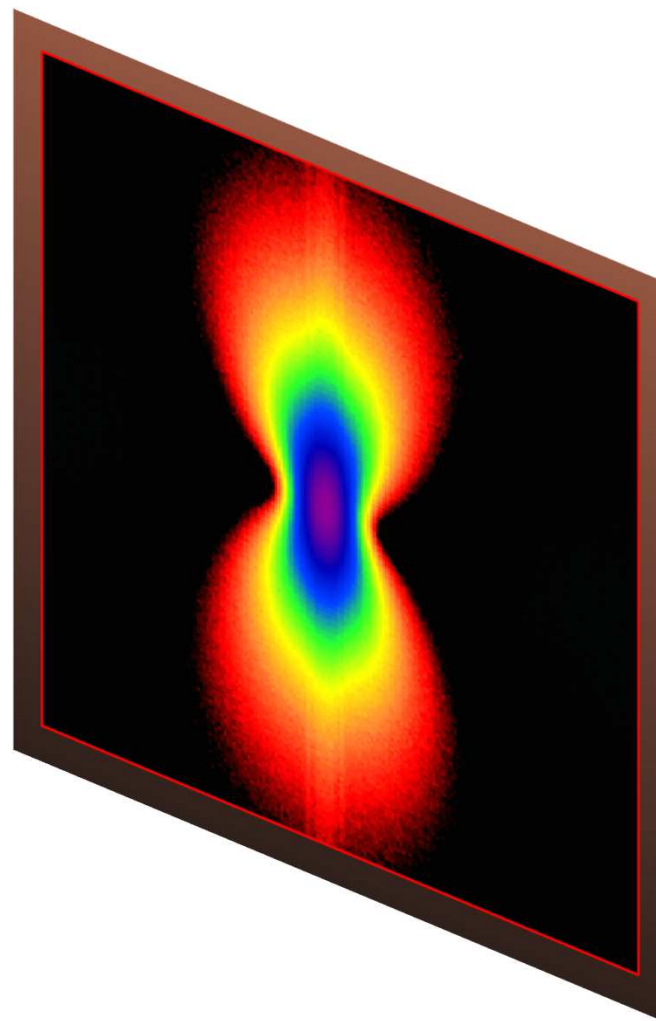


Molflow+



UHV

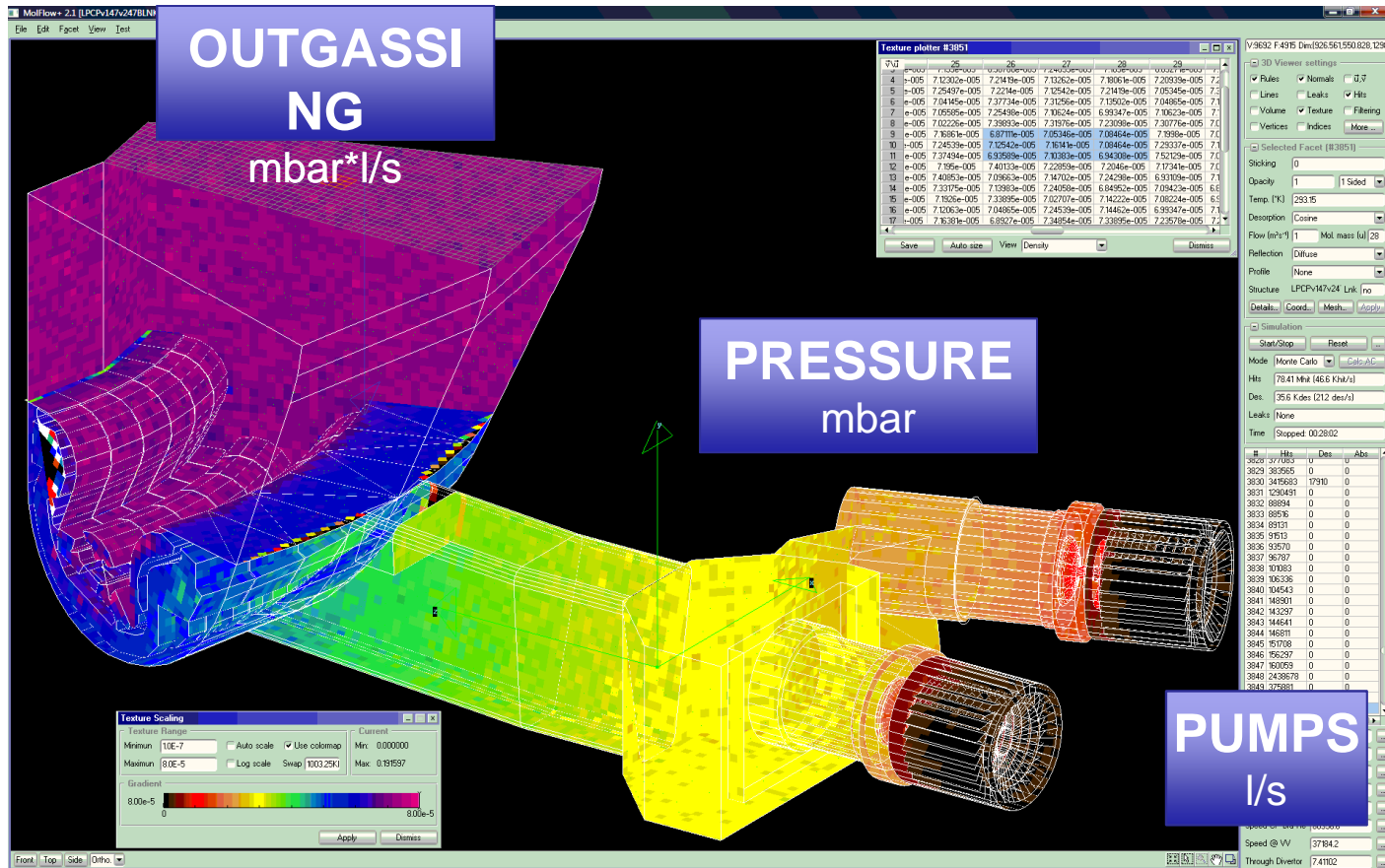
Synrad+



Synchrotron Radiation

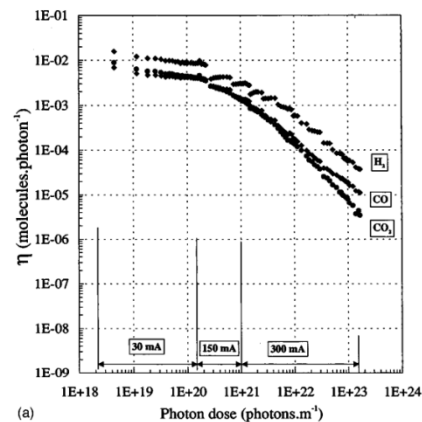
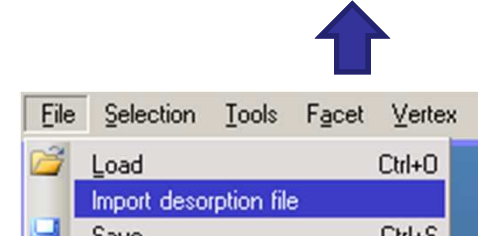
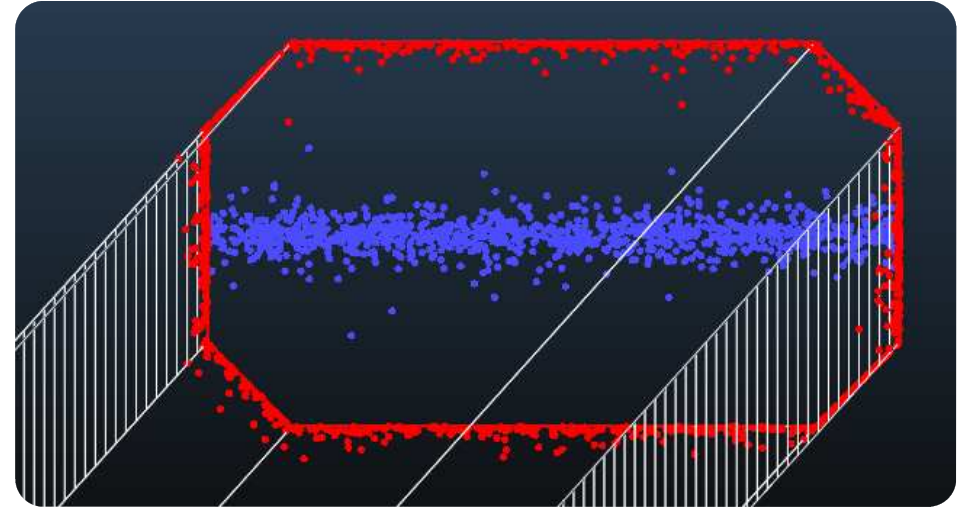
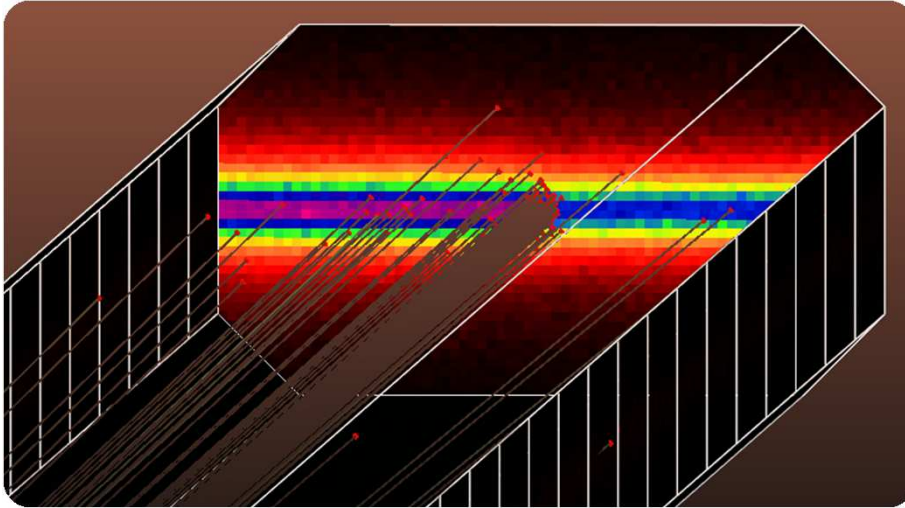
Molflow+

“Friendly units”



Multiple outgassing

Synrad+ AND Molflow+



(a)

Conversion

