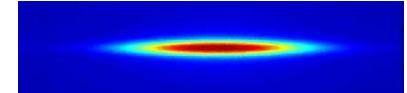


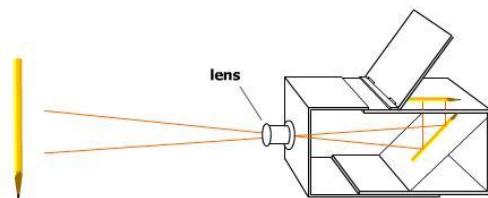
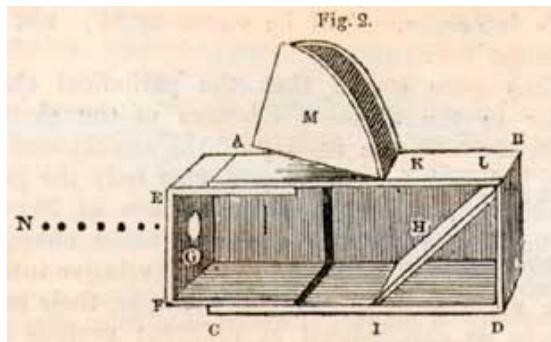
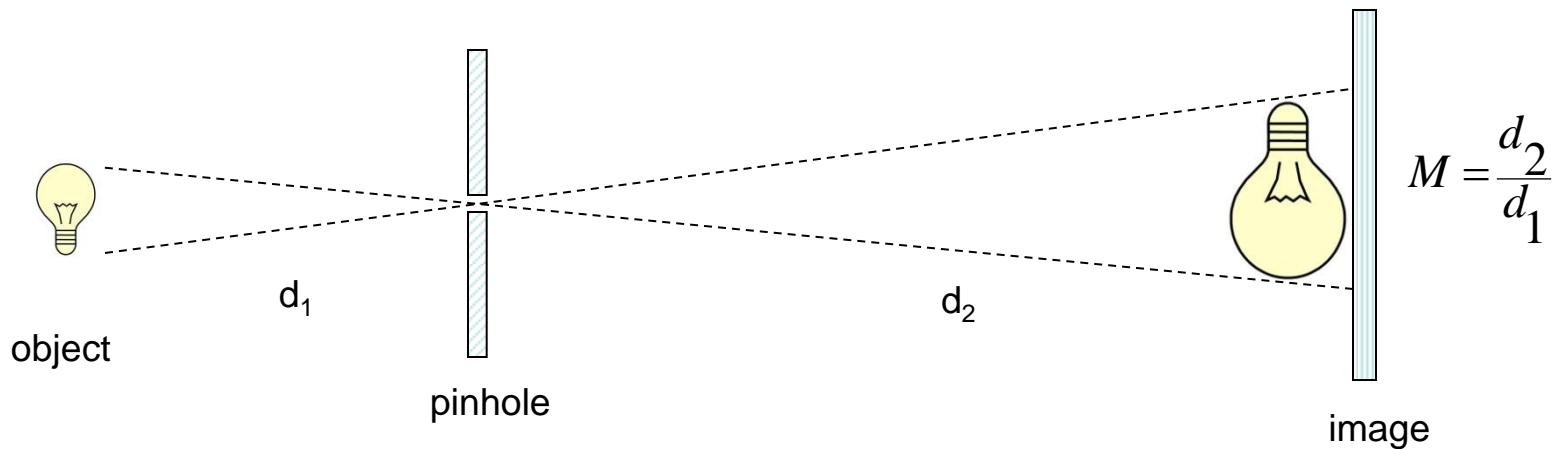
Pinhole Cameras - Operation and Analysis

US Particle Accelerator School
January 14-18, 2008



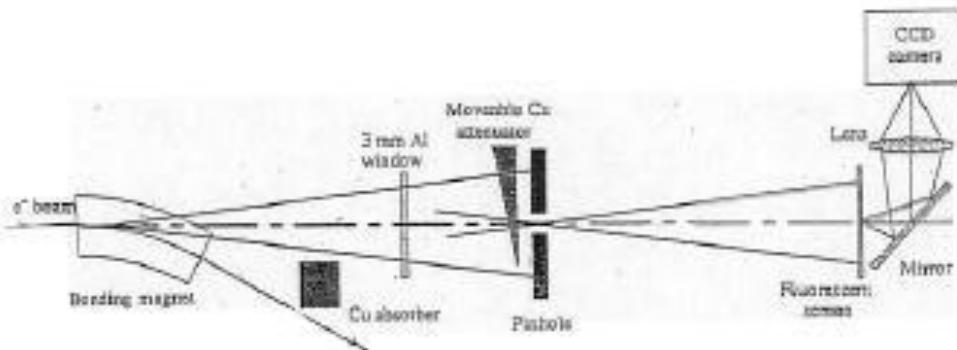
- Use x-rays to minimize diffraction effects
- Reflective/refractive optics not available
- Simple components

Camera Obscura

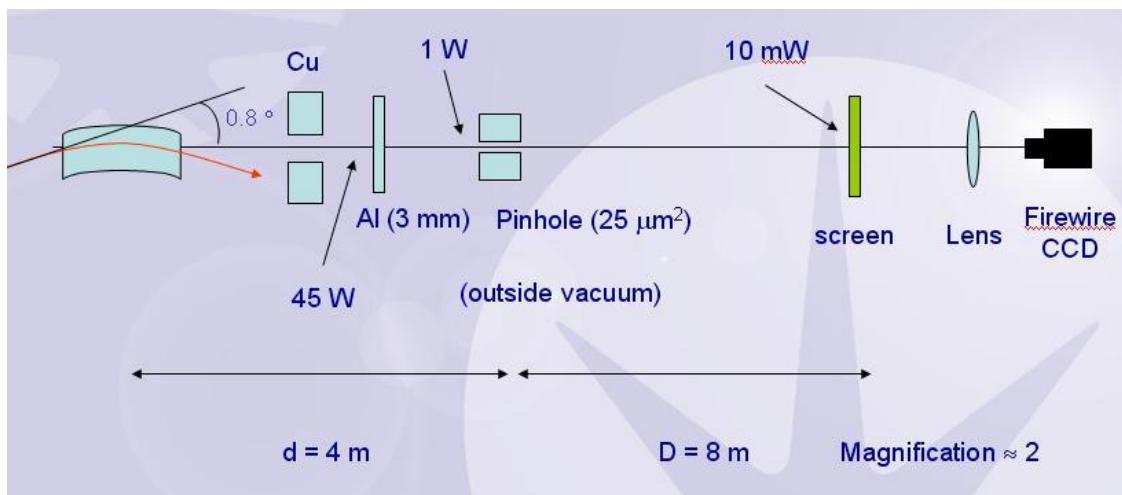


X-ray Pinhole Camera - Schematic

CARTOON of PINHOLE CAMERA

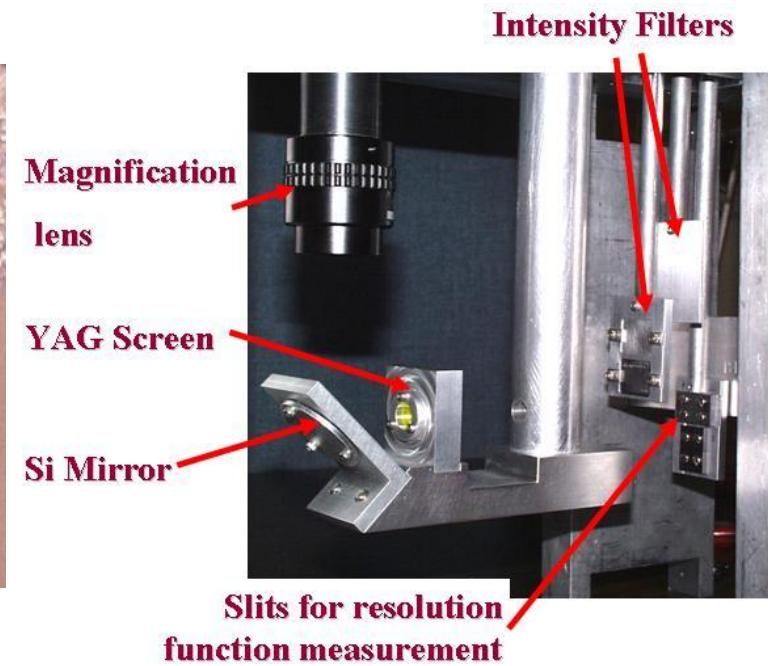
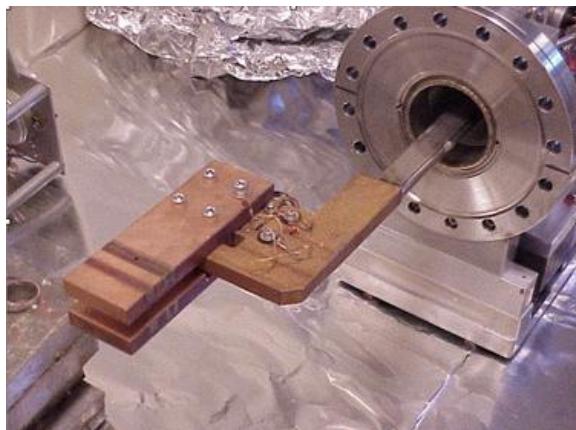


SPEAR circa 1975



DIAMOND circa 2005

SPEAR3 Pinhole, Filters, YAG Screen and Camera



What does the Pinhole Camera See?

1. Horizontal Plane

➤ Electron beam distribution

$$\rho(x, x') = \frac{1}{2\pi\varepsilon_o} e^{-(\gamma_o x^2 + 2\alpha_o xx' + \beta_o x'^2)/2\varepsilon_o}$$

➤ Photon beam distribution

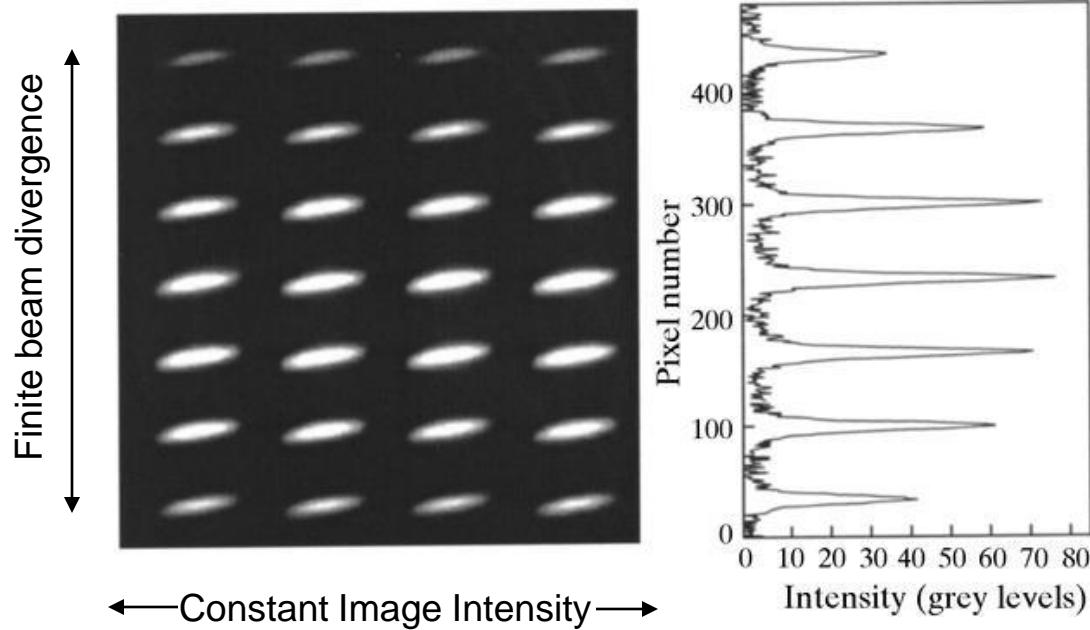
$$\rho(x, x') = \frac{1}{2\pi\varepsilon} e^{-(\gamma x^2 + 2\alpha xx' + \beta x'^2)/2\varepsilon} \quad (\text{new Twiss, new ellipse})$$

Searchlight sweeping across pinhole integrates over x'

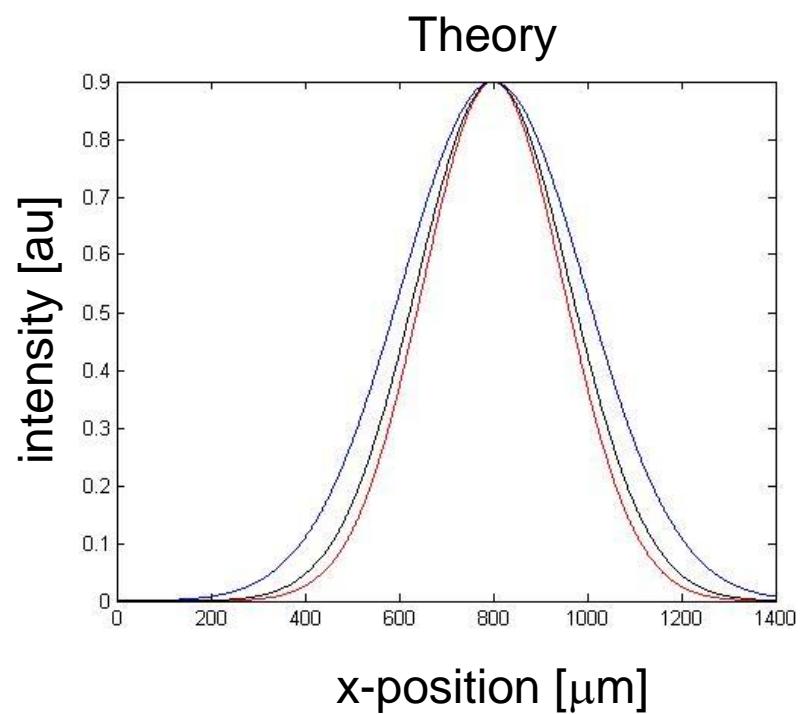
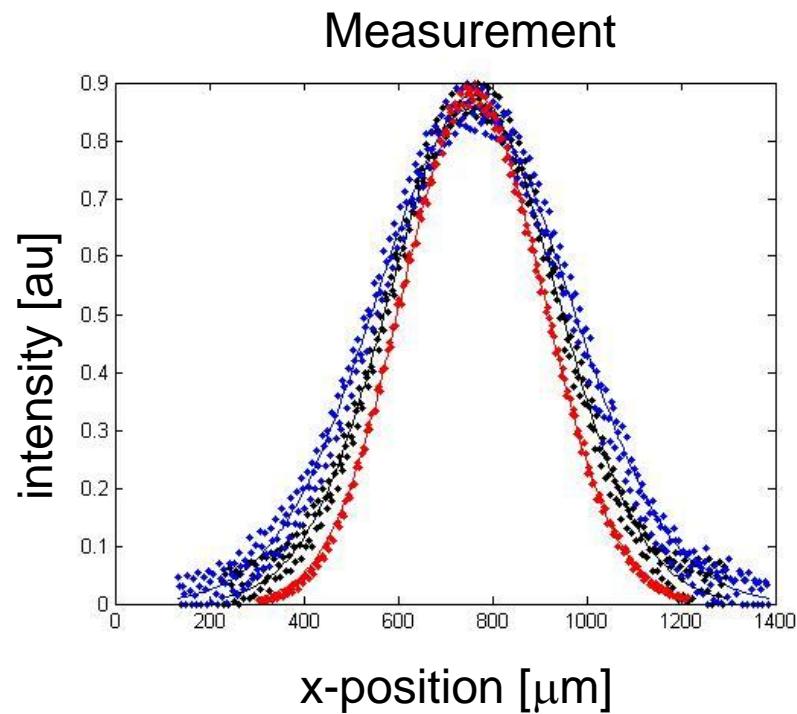
$$\rho(x) = \frac{1}{\sqrt{2\pi\beta\varepsilon}} e^{-x^2/2\beta\varepsilon} \quad (\text{simple result})$$

where $\beta\varepsilon = \beta_o\varepsilon_o + (\eta_o\delta)^2$ \longrightarrow fit to Gaussian, compute ε_o

BESSY-II Pinhole Array
(Peatmann and Holldack)



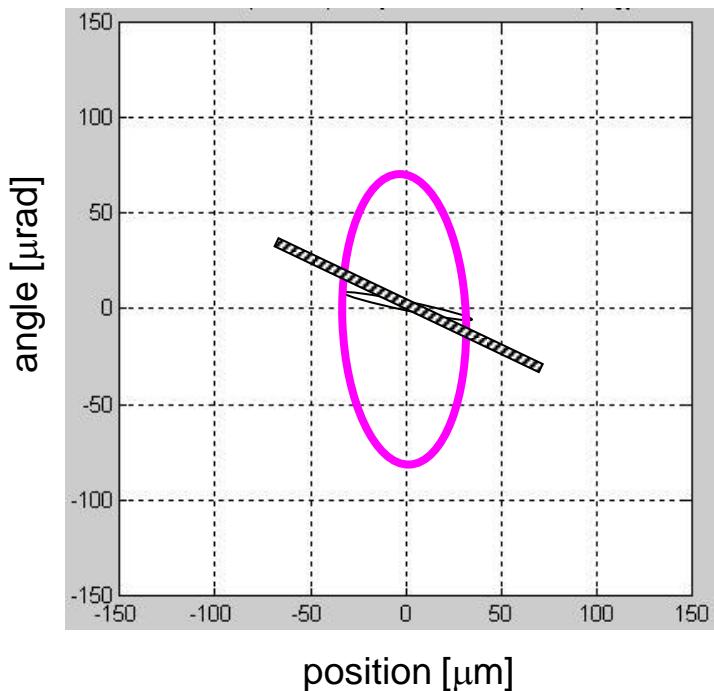
SPEAR3 Example – three different operational modes



What does the Pinhole Camera See?

2. Vertical Plane

- Sweeping searchlight no longer integrates over angles
- Pinhole projected onto source casts a ‘shadow’ in phase space: $y' = \frac{y}{d_1}$



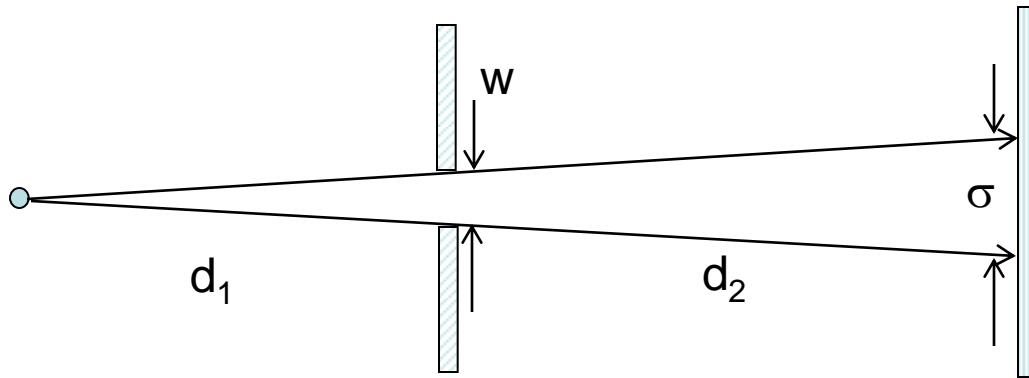
$$\left(\gamma y^2 + 2\alpha y y' + \beta y'^2\right)/2\varepsilon \rightarrow \frac{y^2}{2\varepsilon\beta} \cdot \left\{ 1 + \left(\alpha - \frac{\beta}{d_1} \right)^2 \right\}$$

$$(\varepsilon\beta)_{eff} = \frac{\varepsilon\beta}{1+F}$$

$\rho(y_i) = Ae^{-y_i^2/2(\varepsilon\beta)_{eff}}$

at the screen
(neglecting diffraction)

What size pinhole?



If the pinhole is large, ray-optic ‘spread’ dominates

$$\sigma \approx \frac{w \cdot (d_1 + d_2)}{d_1}$$

If the pinhole is small, diffraction dominates...

Evaluating the Source Size

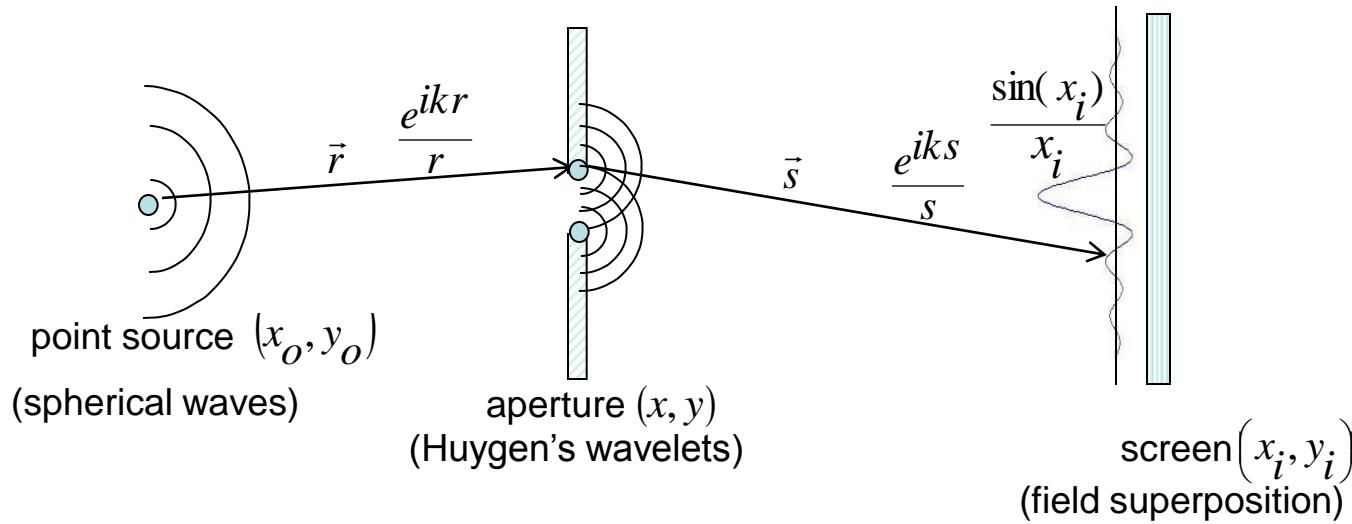
$$(\sigma_{image})^2 = \left(\frac{\sigma_{source}}{demag} \right)^2 + (\sigma_{blur})^2 + (\sigma_{diffraction})^2$$

$$\sigma_{blur} = \frac{w}{\sqrt{2\pi}} \frac{(L_1 + L_2)}{L_1}$$

L₁ Source – pinhole 2.34 m
L₂ Pinhole - screen 1.2 m
Demagnification 1.95:1
W pinhole size 63 μm

$$\sigma_{diffraction} = \frac{\sqrt{12}}{4\pi} \frac{\lambda L_2}{w}$$

Diffraction Effects – monochromatic beam



$$F(x_i | x_o, y_i | y_o) = \frac{B}{\lambda rs} \iint_{\text{aperture}} e^{ik(r+s)} dx dy$$

Point Source Diffraction (cont'd)

$$F = \iint_{\text{aperture}} e^{ik(r+s)} dx dy \quad \text{field integral over pinhole aperture}$$

$$= U_x V_y \quad \text{retangular aperture - surface integral is } \underline{\text{separable}}$$

$$I_x = \text{intensity} = U_x^* U_x$$

$$I_y = V_y^* V_y$$

expand 'r' and 's' to 2nd order - the field integrals look like

$$U_x = \int_{x-\text{aperture}} \exp ik \left\{ \frac{(x_o-x)^2}{2d_1} + \frac{(x_i-x)^2}{2d_2} \right\} dx$$

Distributed Source Field Pattern

$$I(x_i|x_o) = \text{intensity} = U^*U \quad \text{is for a point source}$$

➤ Integrate again over the source distribution

$$I(x_i) = \int \rho(x_o) \cdot I(x_i|x_o) dx_o$$

where $\rho \sim e^{-x^2/2\sigma_x^2}$ (Gaussian distribution)

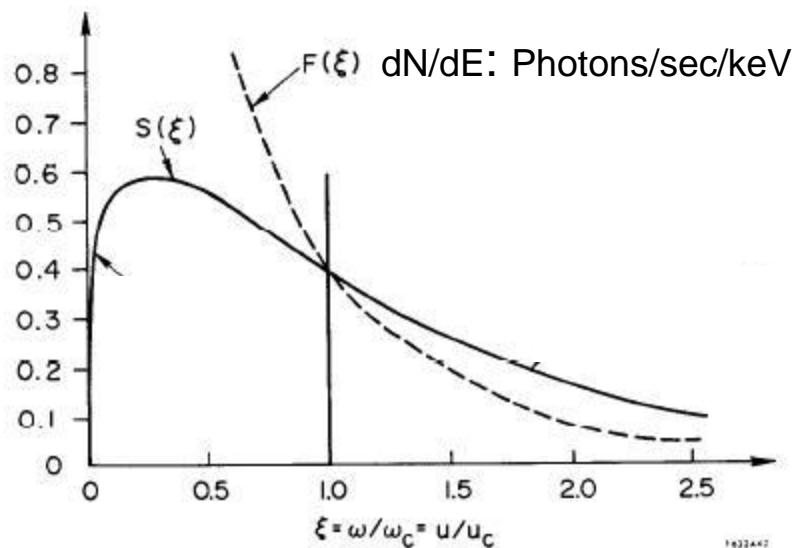
➤ Jack reduced the double integral to a single integral

$$I(x) = \int_0^z \frac{e^{-A z^2}}{z} \cdot \sin B z (1-z) \cdot \cos C x z \cdot dz$$

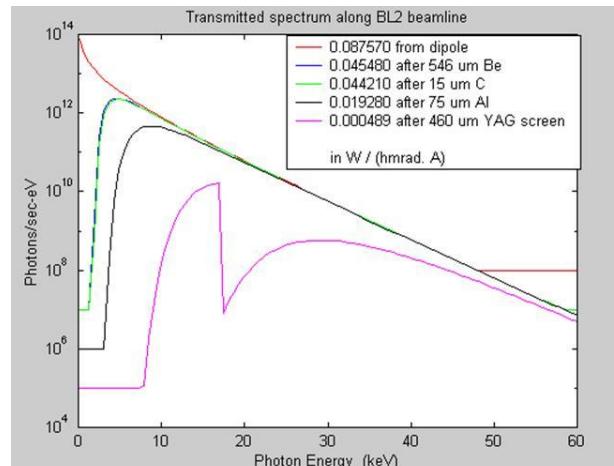
A, B and C are physical system parameters

'Polychromatic' Diffraction

Sands-121



spectrum at screen



C. Limborg - SSRL

FIG. 42--Normalized power spectrum S and photon number spectrum F of synchrotron radiation.

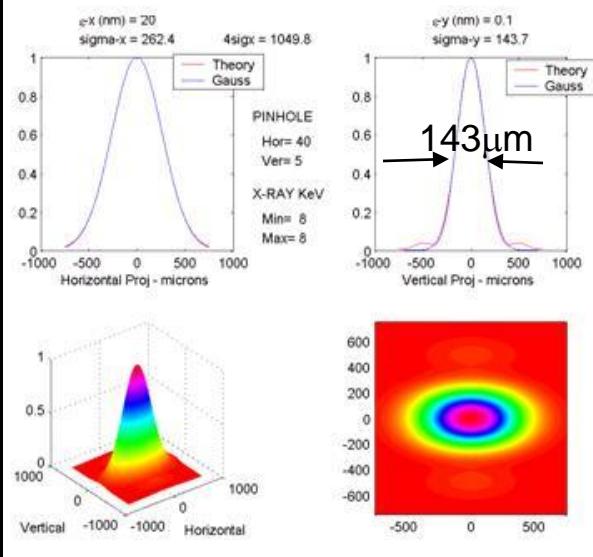


Integrate intensity pattern over photon spectrum

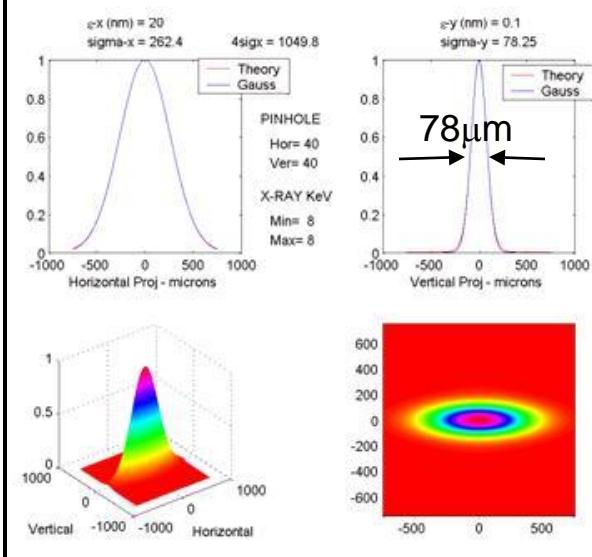
Putting it all together...

fresnel.m valid from geometric to diffraction regimes

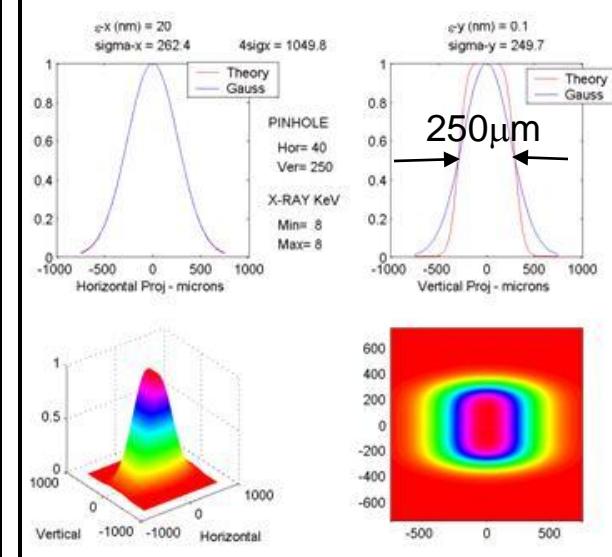
$A_y=5$ micron
(diffraction)



$A_y=40$ micron
(optimum)



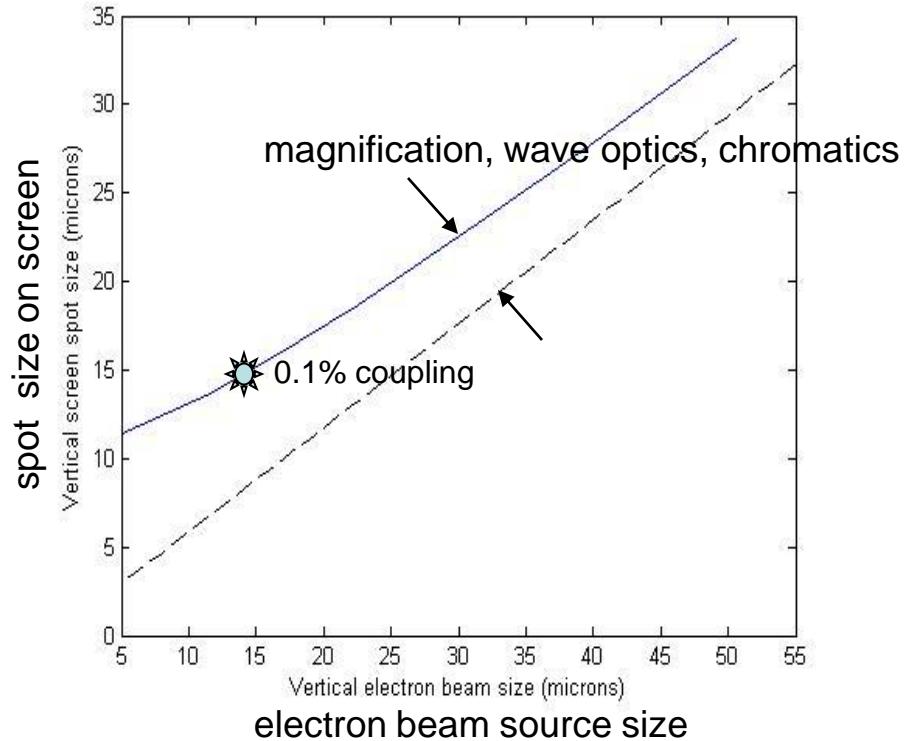
$A_y=250$ micron
(geometric)



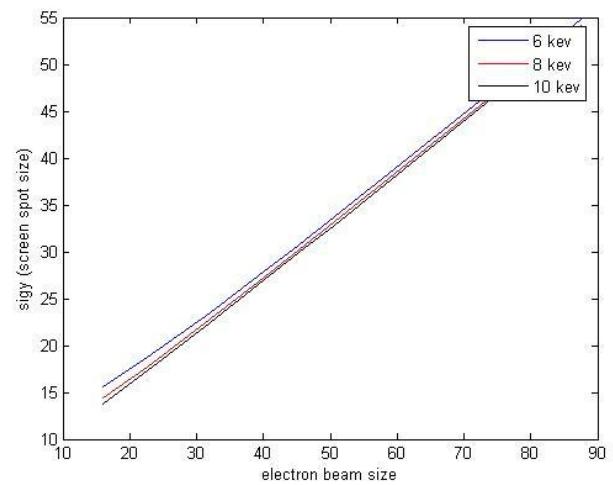
J. Bergstrom - CLS

Application to measurement

SPEAR3: $M=0.6$, $w=30\mu\text{m}$, 8keV



hardening of the spectrum



Summary

- Pinhole cameras effective in the x-ray regime
- System construction fairly straight-forward
- Power loading considerations
- Optimize aperture size
- Data analysis relies on comparison of model with measurement *fresnel.m*
- Effective for measuring small spot sizes