



# Laser-Plasma Accelerators for Future Colliders and Light Sources

**Eric Esarey**  
**LOASIS Program**  
**Accelerator and Fusion Research Division**

**USPAS, Hampton, VA**  
***Jan 17, 2011***

<http://loasis.lbl.gov/>



U.S. DEPARTMENT OF  
**ENERGY**

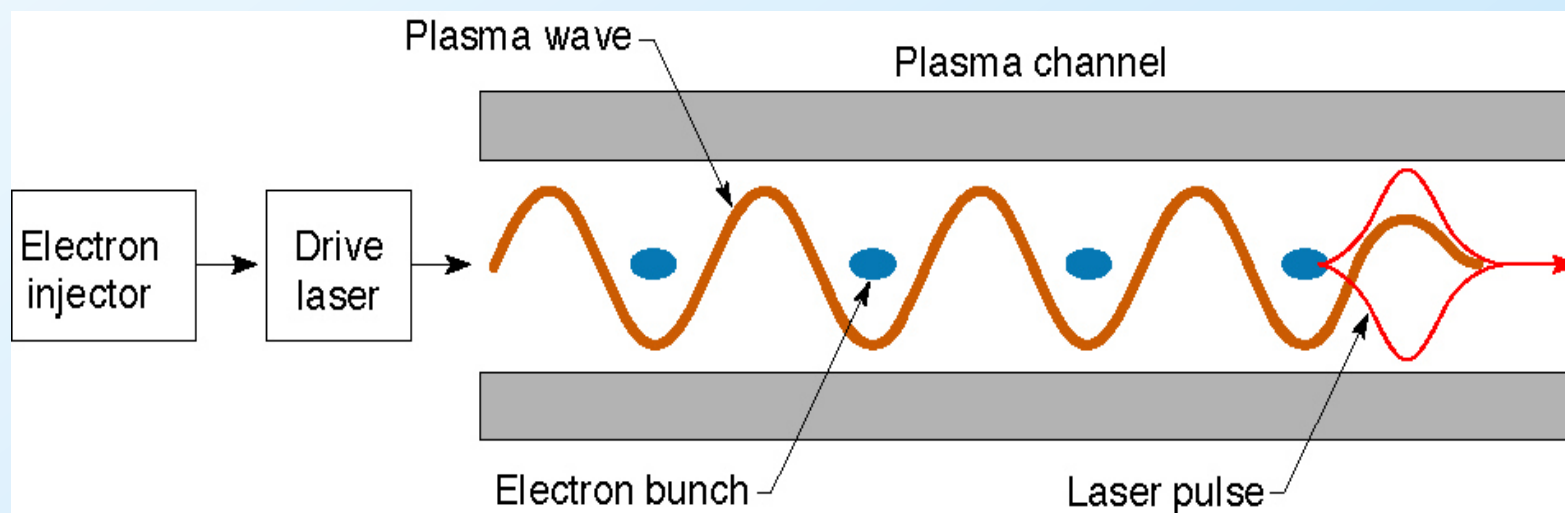
Office of  
Science



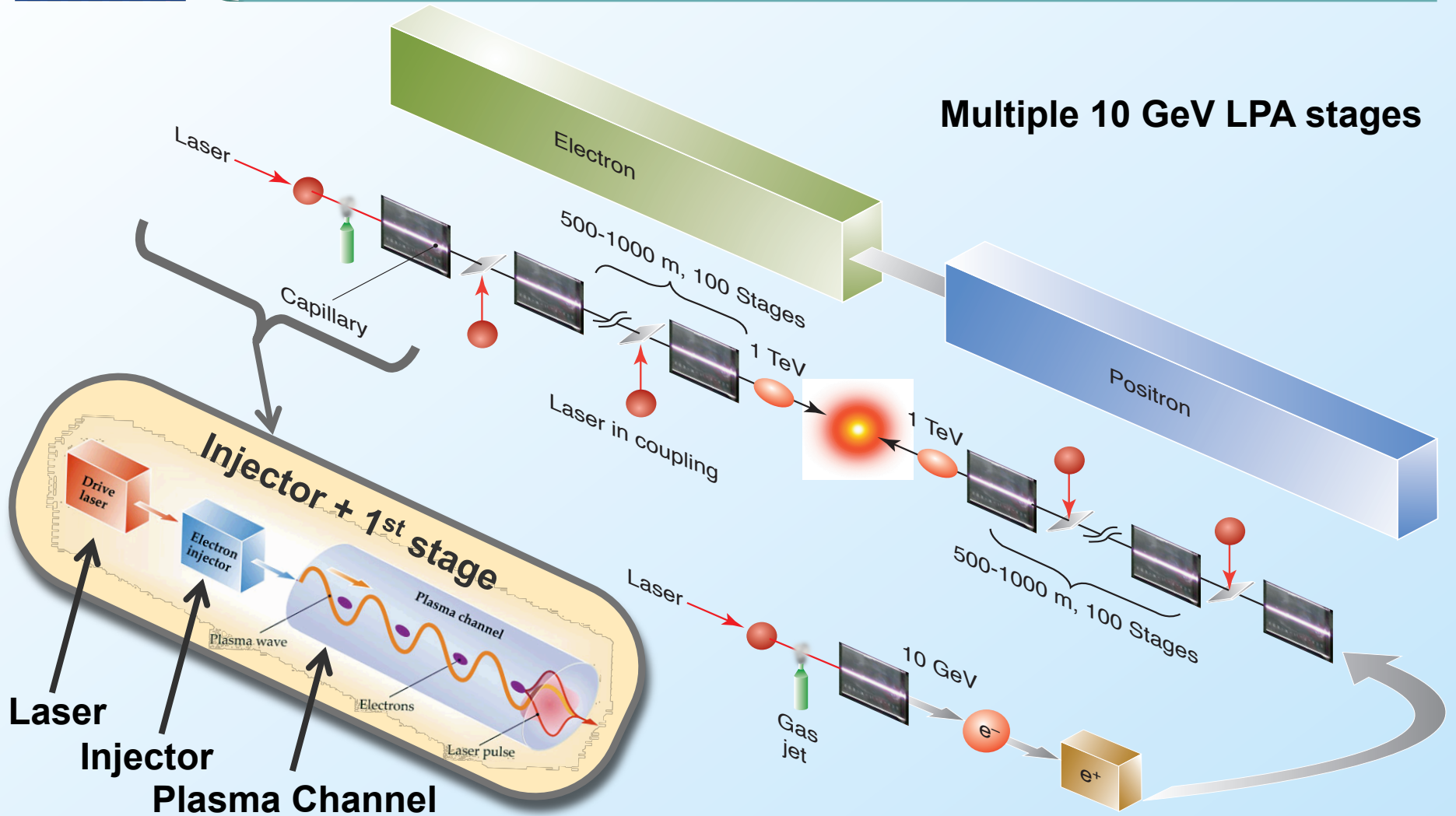
# Outline

- LPA Basics
- Applications: conceptual designs
  - Electron-positron linear collider
  - XUV/X-ray Free Electron Lasers
- BELLA Project and LBNL

## Laser-Plasma Accelerator



# Strawman Design of a TeV LPA Collider





# Laser-plasma accelerators (LPAs)

Tajima & Dawson, *Phys. Rev. Lett.* (1979); Esarey, Schroeder, Leemans, *Rev. Mod. Phys.* (2009)

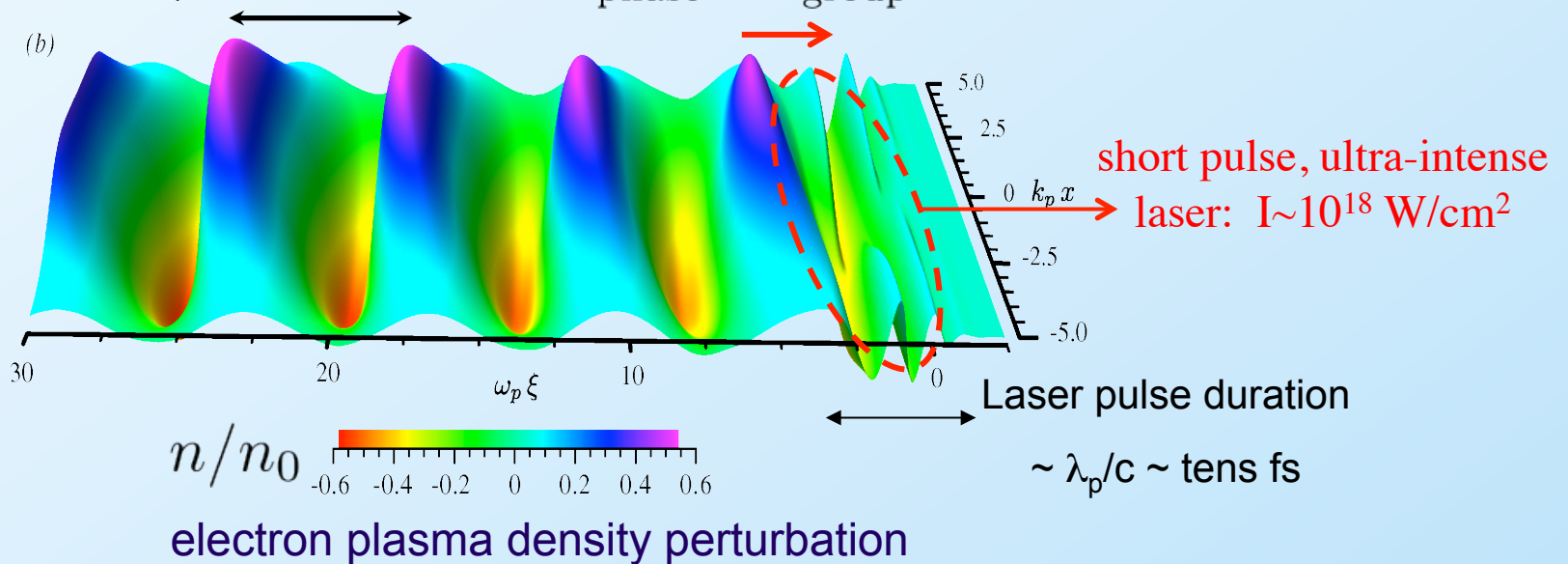
$$\left( \frac{\partial^2}{\partial t^2} + \omega_p^2 \right) \frac{n}{n_0} = c^2 \nabla^2 \frac{1}{4} \left( \frac{eE_{\text{laser}}}{mc^2\omega} \right)^2$$

Plasma wave: electron density perturbation

Laser ponderomotive force (radiation pressure)

$$\lambda_p = 2\pi c / \omega_p = (\pi r_e^{-1/2}) n_p^{-1/2} \sim 30 \mu\text{m}$$

$$v_{\text{phase}} \simeq v_{\text{group}} \simeq c$$





# Laser-plasma accelerators: >10 GV/m accelerating gradient

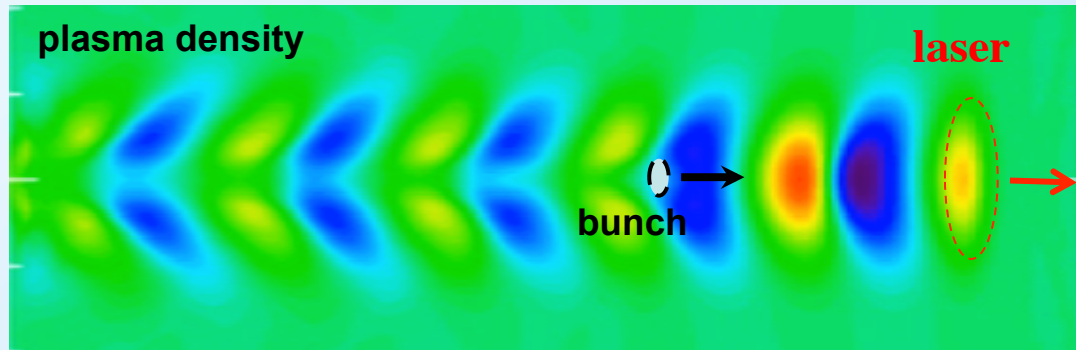
$$E \sim \left( \frac{mc\omega_p}{e} \right) \approx (96 \text{ V/m}) \sqrt{n_0 [\text{cm}^{-3}]}$$

plasma wave (wakefield)  $E \sim 100 \text{ GV/m}$  (for  $n \sim 10^{18} \text{ cm}^{-3}$ )

**>10<sup>3</sup> larger than conventional RF accelerators  $\Rightarrow$  “>km to <m”**

Accelerating bucket  $\sim$  plasma wavelength

**$\rightarrow$  ultrashort (fs) bunches ( $< \lambda_p/4$ )**



- beam charge (set by beam loading):  $\sim 100 \text{ pC}$  (for  $n \sim 10^{18} \text{ cm}^{-3}$ )

- beam duration (set by trapping physics):  $< 10 \text{ fs}$

**$\rightarrow$  high peak current**  
 $\gtrsim 10 \text{ kA}$



## Basic design of a laser-plasma accelerator: single-stage limited by laser energy

- Laser pulse length determined by plasma density

- $k_p \sigma_z \leq 1, \quad \sigma_z \sim \lambda_p \sim n^{-1/2}$

- Wakefield regime determined by laser intensity

- Linear ( $a_0 < 1$ ) or blowout ( $a_0 > 1$ )

- Determines bunch parameters via beam loading

$$a_0^2 \simeq 7.3 \times 10^{-19} [\lambda(\mu\text{m})]^2 I_0 (\text{W}/\text{cm}^2),$$

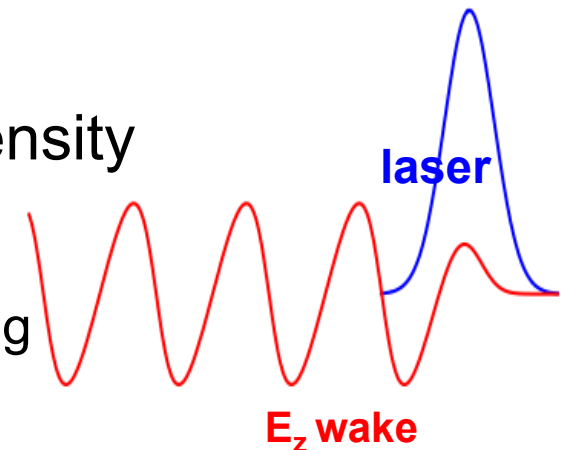
- Ex:  $a_0 = 1$  for  $I_0 = 2 \times 10^{18} \text{ W}/\text{cm}^2$  and  $\lambda_0 = 0.8 \mu\text{m}$

- Accelerating field determined by density and laser intensity

- $E_z \sim (a_0^2/4)(1+a_0^2/2)^{-1/2} n^{1/2} \sim 10 \text{ GV}/\text{m}$

- Energy gain determined by laser energy via depletion\*

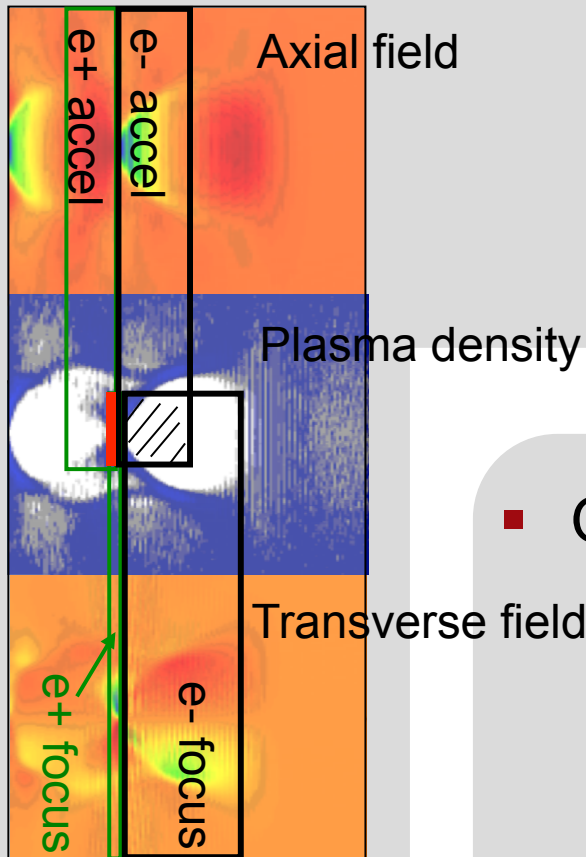
- Laser: Present CPA technology 10's J/pulse



\*Shadwick, Schroeder, Esarey, Phys. Plasmas (2009)

# Linear & blowout regimes: e<sup>+</sup>/e<sup>-</sup> acceleration

$a_0=4$



## Blowout regime

- high field
- very asymmetric
  - focuses e<sup>-</sup>
  - defocuses e<sup>+</sup>
- self-trapping

## Quasilinear

- linear: symmetric e<sup>+</sup>/e<sup>-</sup>
- high  $a_0$  desired for gradient
  - too high enters bubble
- $a_0 \sim 1-2$  good compromise
- dark current free

$a_0=1$

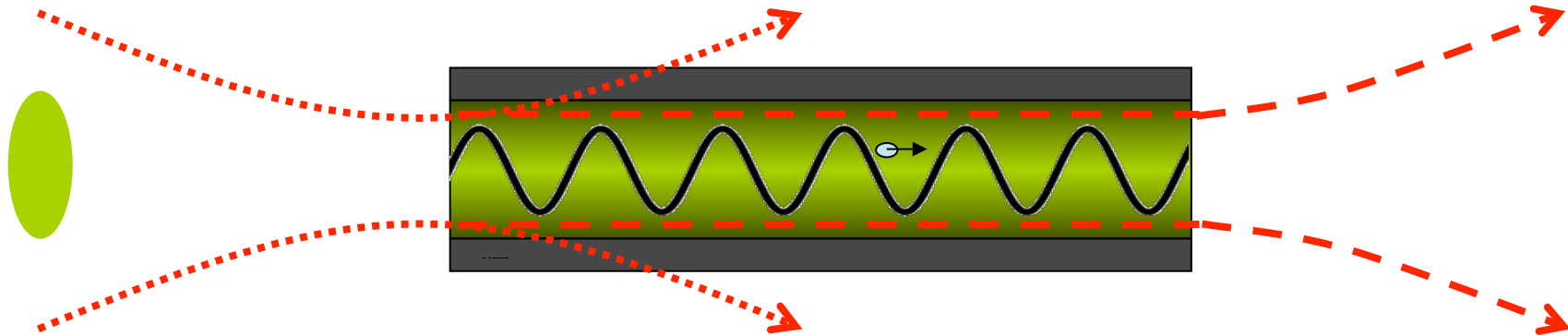




$$\Delta W = E_z \cdot L$$

## Limits to acceleration length: diffraction

- “3D”: Diffraction, Dephasing, Depletion
- **Diffraction** of laser pulse
  - $Z_R = \pi r_0^2 / \lambda_0 \sim 2 \text{ cm}$ ,  $Z_R \ll L_{\text{dephase}} < L_{\text{deplete}}$
  - Solution: Density channels



- Parabolic channel guides gaussian modes
- Channel depth:  $\Delta n [\text{cm}^{-3}] = 10^{20} / (r_0[\mu\text{m}])^2 \sim 2 \times 10^{16} \text{ cm}^{-3}$

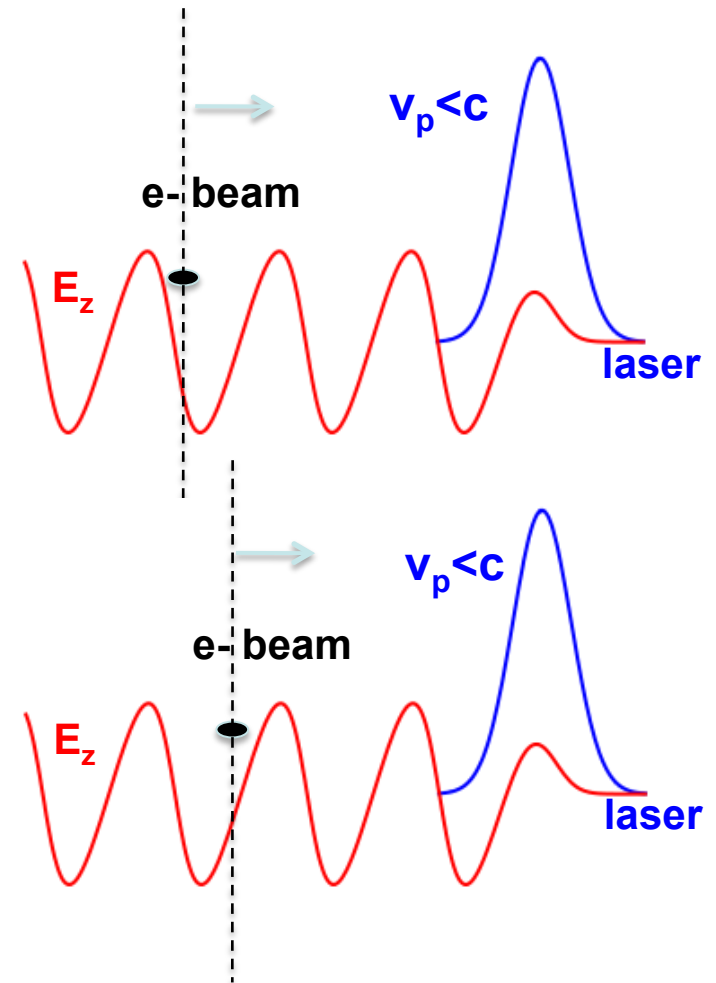




$$\Delta W = E_z \cdot L$$

## Limits to Acceleration Length: dephasing

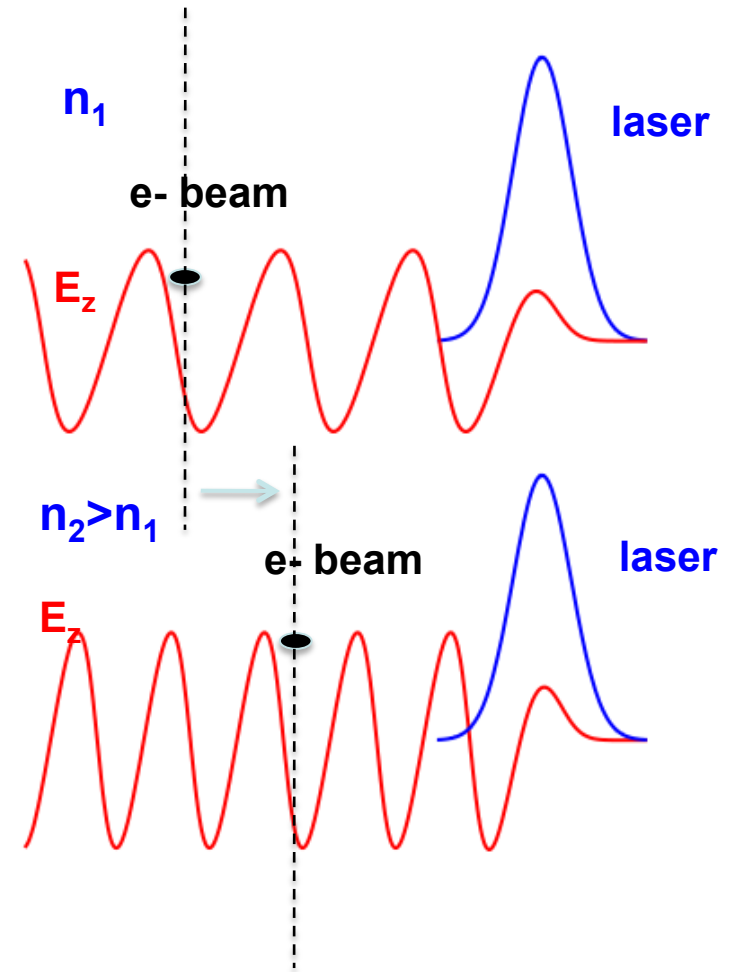
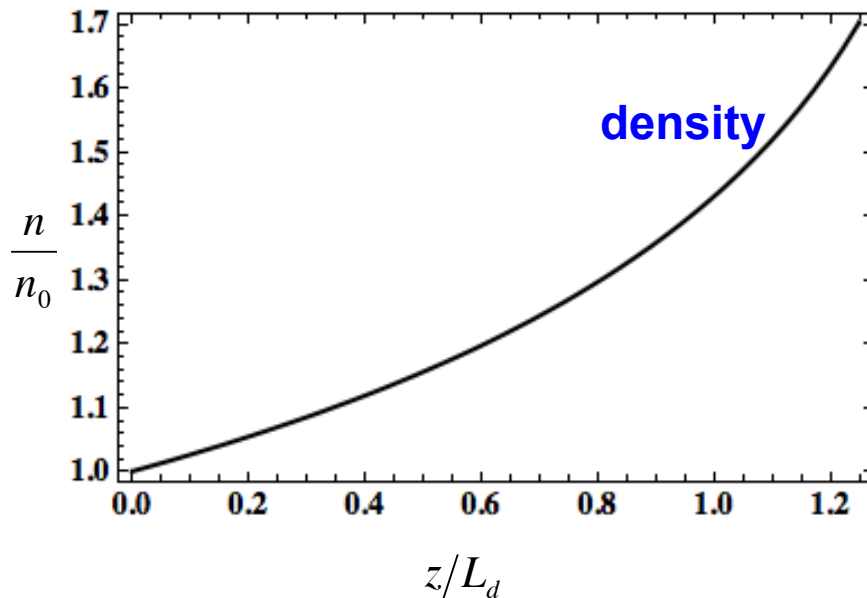
- **Dephasing:** e<sup>-</sup> outrun wake,
  - Phase velocity:  $v_p/c \approx v_g/c = 1 - \lambda_0^2/2\lambda_p^2$
  - $L_{\text{dephase}} (1 - v_g/c) = \lambda_p/2$ ,
  - $L_{\text{dephase}} = \lambda_p^3/\lambda_0^2 \sim n^{-3/2} \sim 1.6 \text{ m}$
- **Solution:** density tapering





# Density Tapering: Phase Lock e-

- For  $a_0 \sim 1$ ,  $L_{\text{dephase}}$  may be  $< L_{\text{deplete}}$
- Phase velocity depends on density
  - Phase position  $\sim \lambda_p \sim n^{-1/2}$
- Taper density to tune wake velocity
- Depletion then limits e<sup>-</sup> energy gain



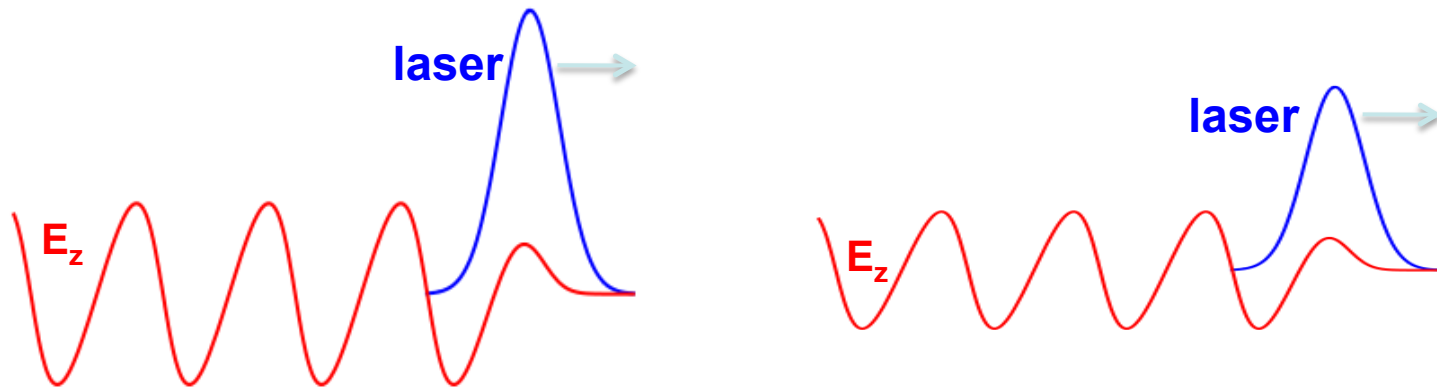
Katsouleas, PRA (1986); Rittershofer et al, PP (2010)



$$\Delta W = E_z \cdot L$$

## Limits to acceleration length: depletion

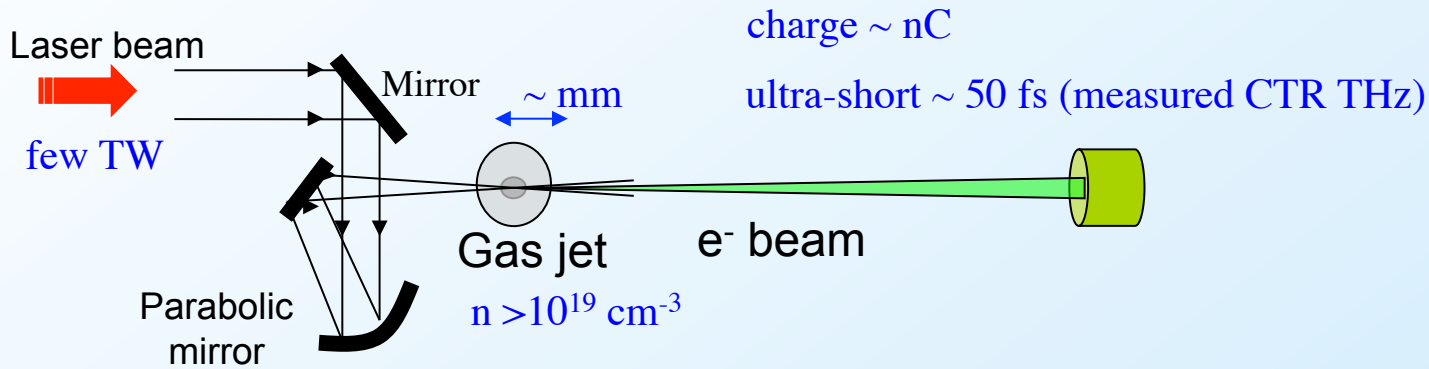
- **Depletion:** laser loses energy to wake
  - Energy balance:  $E_L^2 \sigma_z = E_z^2 L_{\text{deplete}}$
  - Linear limit  $a_0^2 \ll 1$ :  $L_{\text{deplete}} = a_0^{-2} L_{\text{dephase}} \gg L_{\text{dephase}}$
  - Nonlinear limit  $a_0^2 \gg 1$ :  $L_{\text{deplete}} \sim L_{\text{dephase}}$



**Solution: staging**

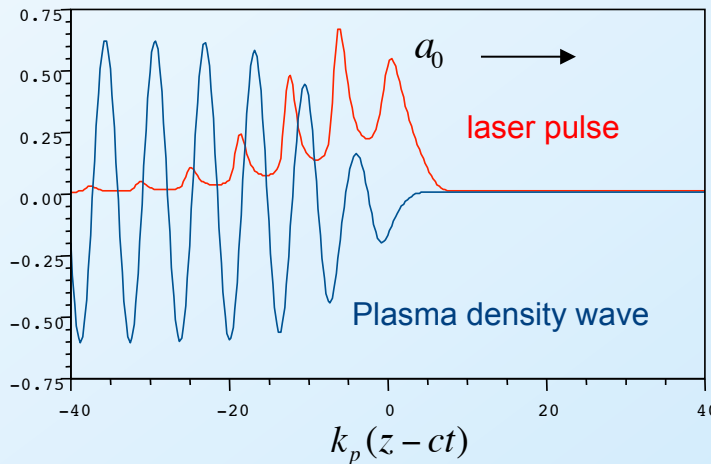


# Prior to 2004: Self-modulated laser-plasma accelerator experiments

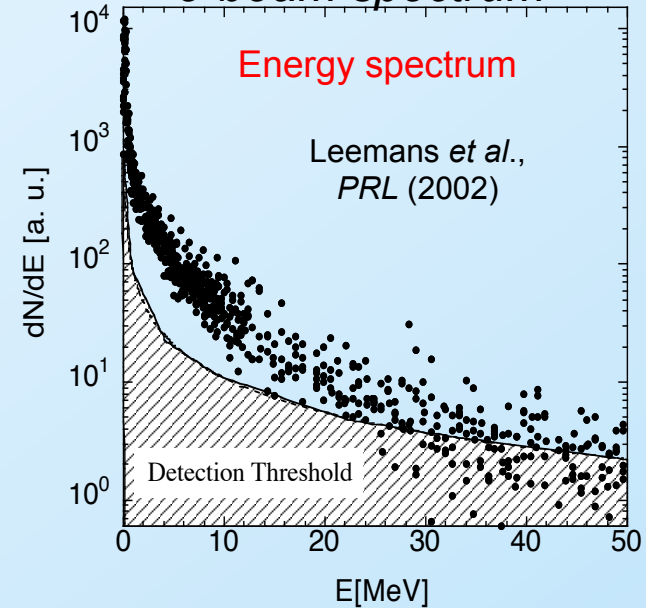


- Plasma wave generated via Raman scattering instability (modulation of a long laser pulse)

Schroeder *et al.*,  
*Phys. Plasmas*  
(2003)



## *e*-beam spectrum



Exponential distribution:

(1) Raman instability results in continued electron trapping

(2) High density  $\Rightarrow L_{\text{dephase}} \ll L_{\text{gas-jet}} \Rightarrow$  electrons accelerated and decelerated

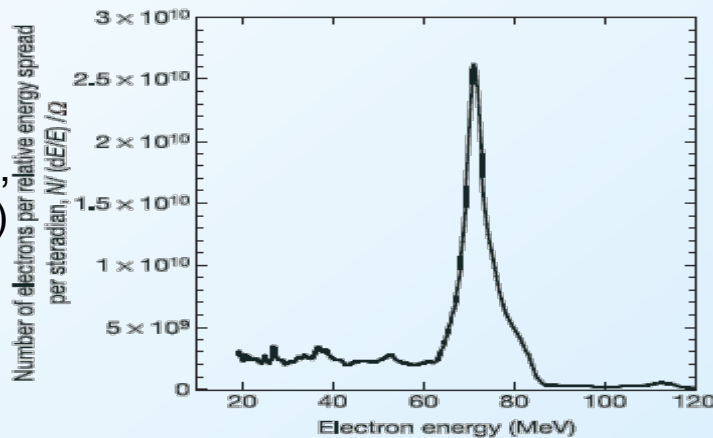


# 2004 Experimental Results: High-quality 100 MeV beams

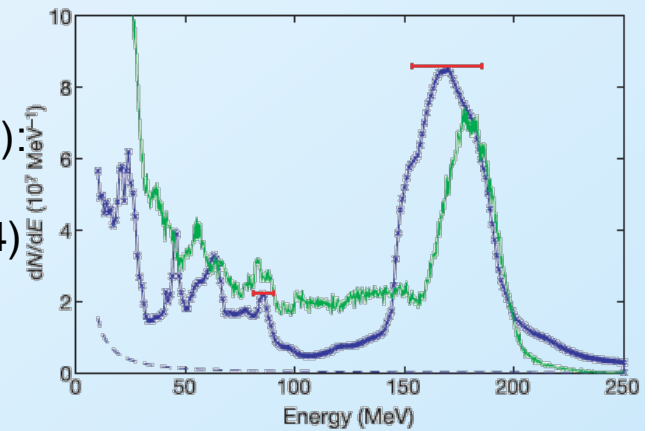
Extend interaction length and lower plasma density to match interaction length to dephasing length:  $L_{\text{int}} \sim L_{\text{dephase}} \sim L_{\text{deplete}}$

- Approach 1: bigger laser spot (more laser energy)

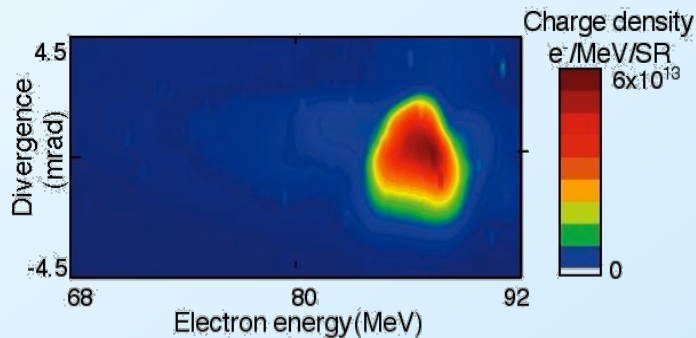
RAL (UK):  
Mangles et al,  
Nature (2004)



LOA (France):  
Faure et al,  
Nature (2004)



- Approach 2: preformed channel guided: LBNL expt.



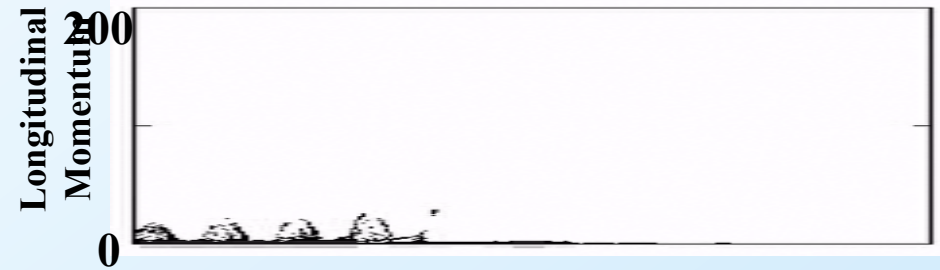
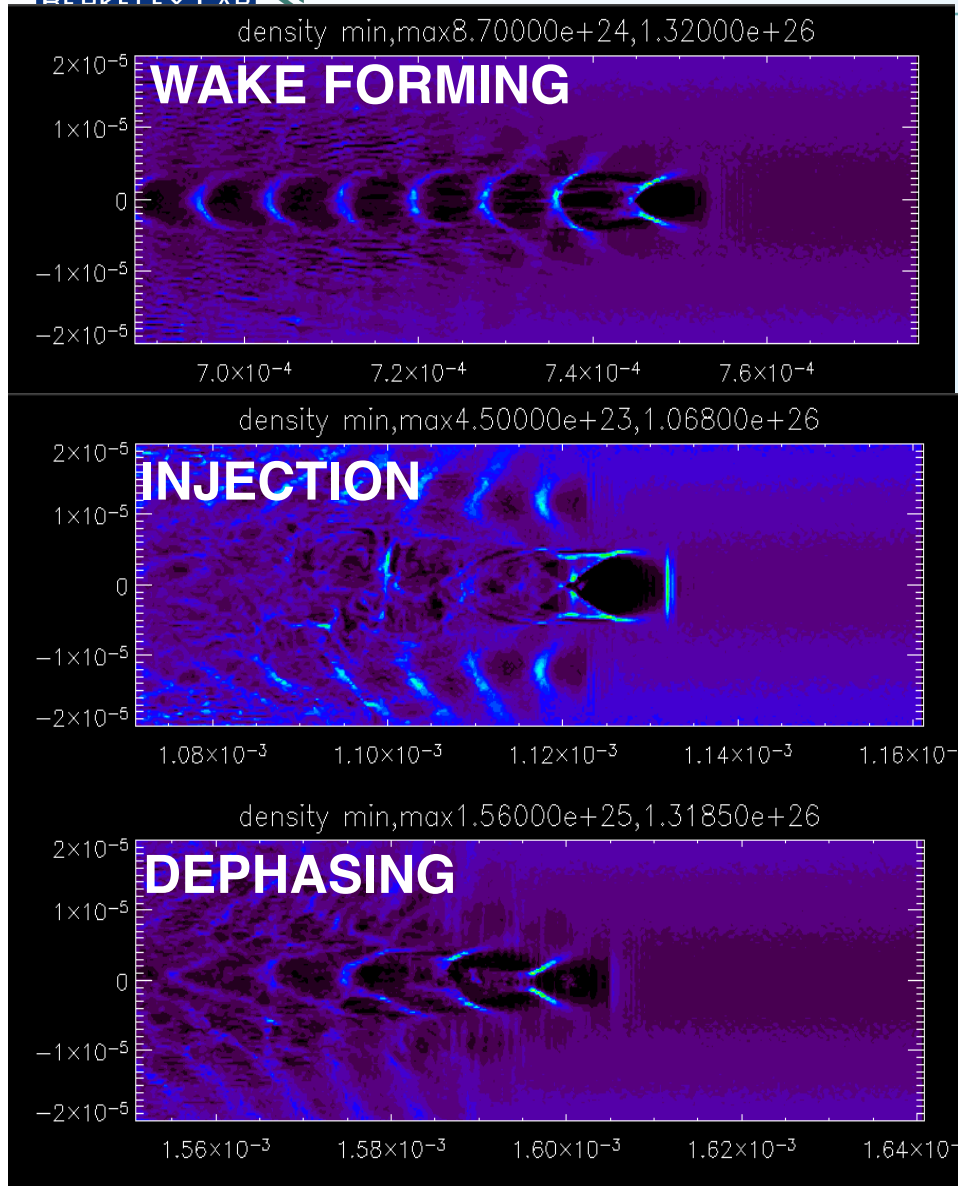
Geddes et al, Nature 431 (2004)

PIC Simulation of  
LBNL Expt.





# Wake Evolution and Dephasing Yield Low Energy Spread Beams in PIC Simulations



Propagation Distance



Propagation Distance



Propagation Distance

Geddes et al., Nature (2004) & Phys. Plasmas (2005)



# LWFA: Production of a Monoenergetic Beam

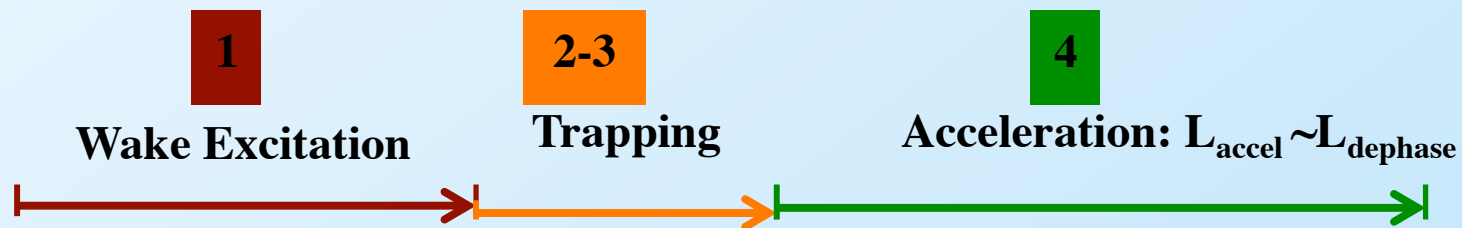
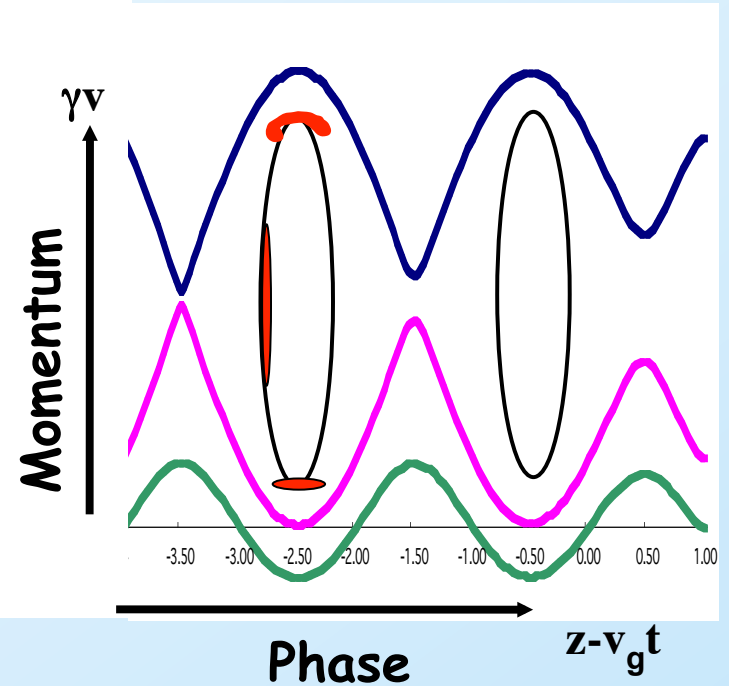
1. Excitation of wake (e.g., self-modulation of laser)
2. Onset of self-trapping (e.g., wavebreaking)
3. Termination of trapping (e.g., beam loading)
4. Acceleration

If  $>$  dephasing length: large energy spread

If  $\approx$  dephasing length: monoenergetic

• **Dephasing distance:**

$$L_{dph} \approx \left( \lambda_p^3 / \lambda^2 \right) \propto n_e^{-3/2}$$



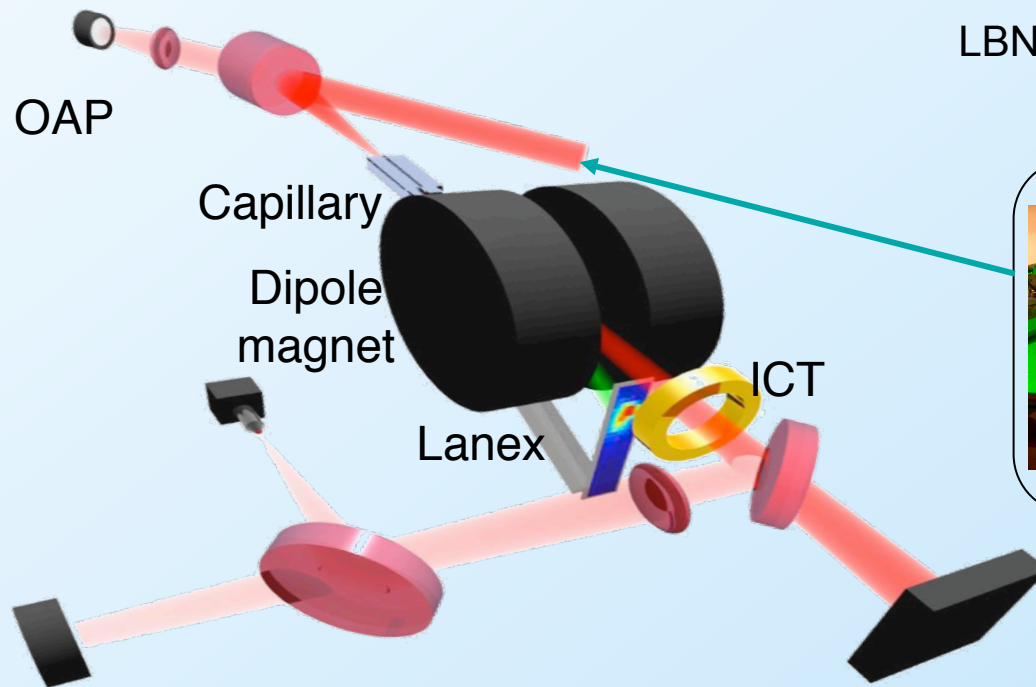


# Laser-plasma accelerator for GeV beams

Energy gain:  $W \sim (mc\omega_p/e)L_{acc} \propto n^{-1}$  → low density plasmas ( $\sim 10^{18} \text{ cm}^{-3}$ )

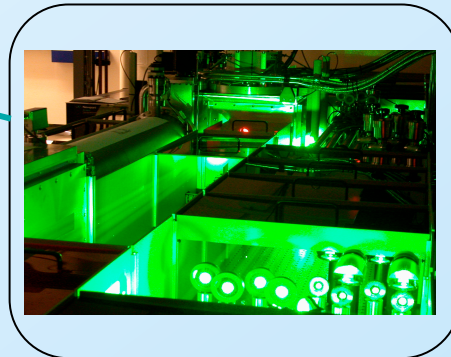
Accelerator length:  $L_{acc} \sim \lambda_p^3 / \lambda_L^2 \propto n^{-3/2}$  → long plasma channels ( $\sim \text{cm}$ )

Laser energy/power:  $U_{laser} \propto n^{-3/2}$   
 $P_{laser} \propto n^{-1}$  } → more laser energy (power)



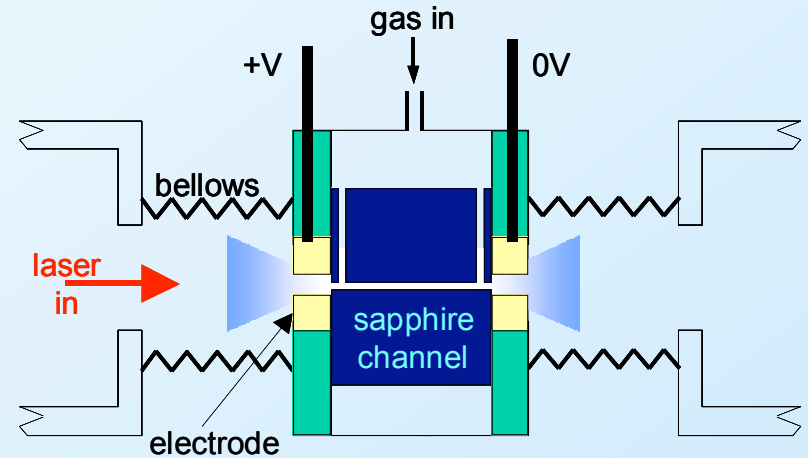
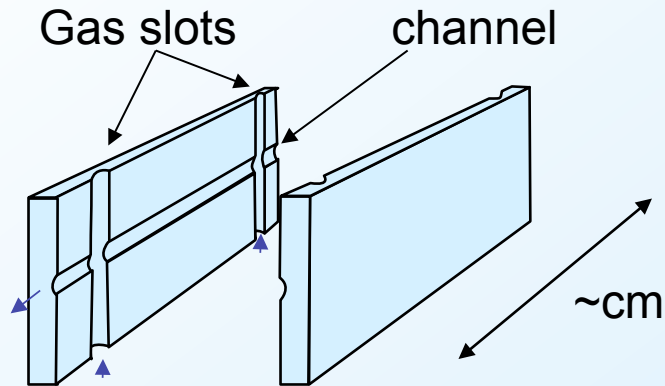
LBL Ti:Al<sub>2</sub>O<sub>3</sub> laser system:

3 J, 40 fs, 10 Hz

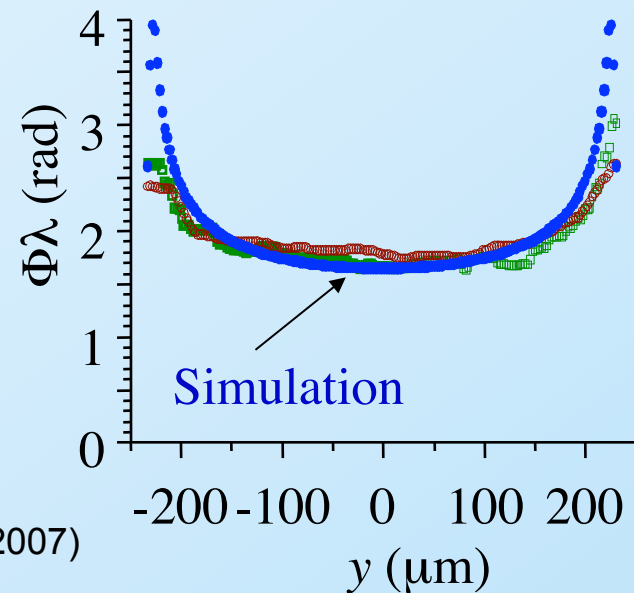




# Capillary discharge plasma waveguides



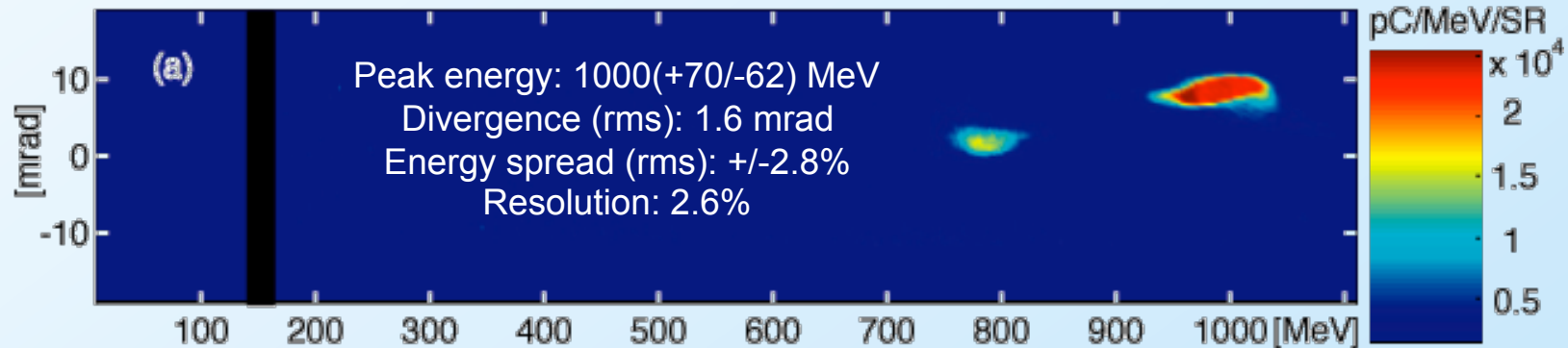
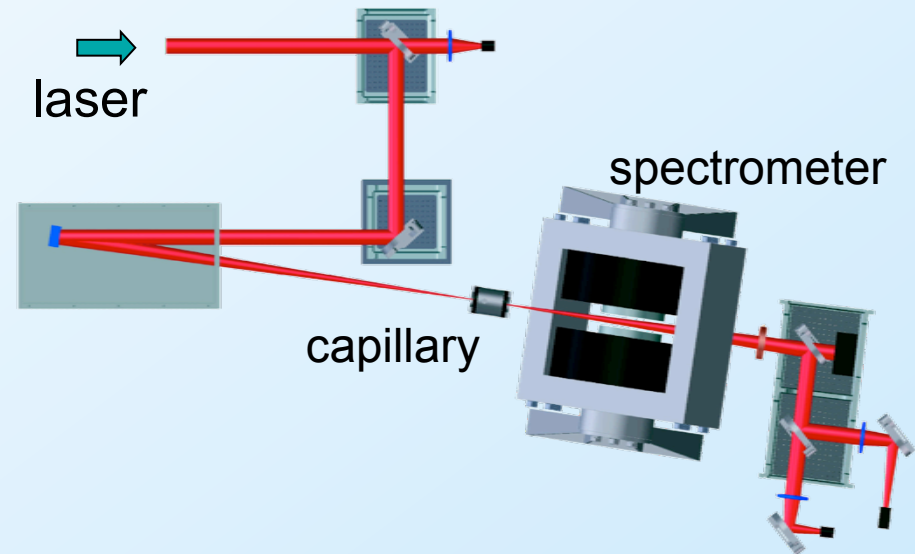
- Ionized by pulse discharge (200-500A, ~100ns)
- Plasma fully ionized for  $t > 50$  ns
- After  $t \sim 80$  ns plasma is in quasi-equilibrium: Ohmic heating is balanced by conduction of heat to wall
- Ablation rate small: cap. lasts for  $> 10^6$  shots
- $n_e \sim 10^{17} - 10^{19} \text{ cm}^{-3}$





# GeV electron beam from laser-plasma accelerator demonstrated

- $a_0 \sim 1.46$  (40 TW, 37 fs)
- $n_e \sim 4 \times 10^{18} \text{ cm}^{-3}$
- capillary: 33 mm length



Leemans et al., Nature Physics (2006)



# Challenge: Controlled injection for improved beam quality and stability

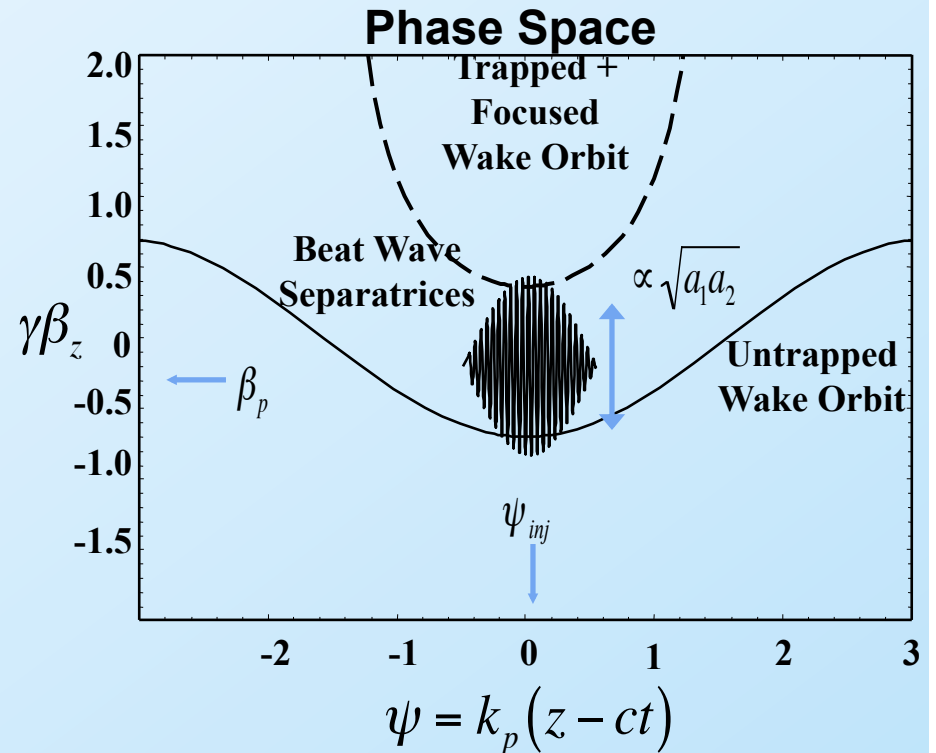
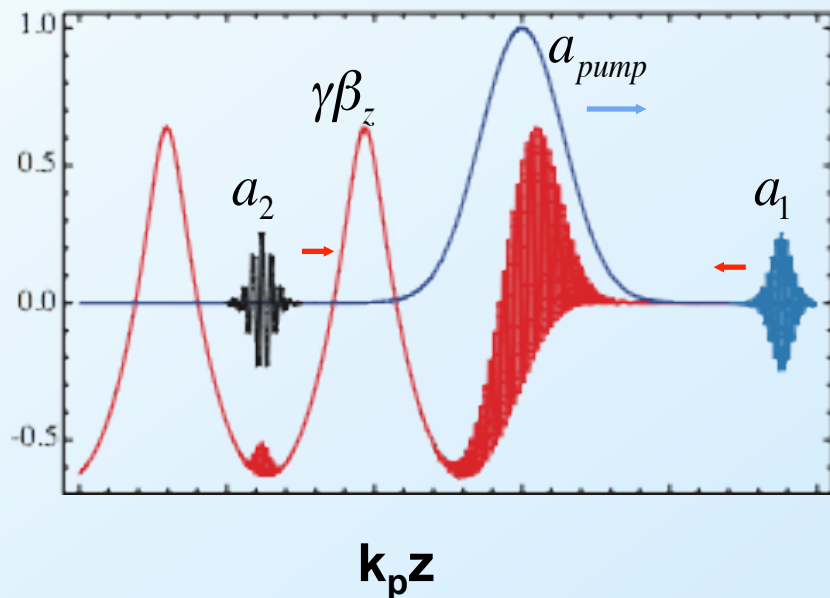
- In regime of beam self-trapped from background plasma, beam quality determined by self-trapping physics.
- Controlled injection (charge and location) of electrons into plasma wave to improve beam stability and quality
  - External injection (from conventional RF gun)
    - problematic: coupling to plasma-wavelength-scale and synchronization
  - Triggered trapping (injection) of plasma electrons:
    1. Laser-triggered injection (colliding pulse injection)
    2. Plasma density gradient injection
- In principle, triggered injection in a plasma wave could achieve beam quality (low emittance) beyond state-of-the-art photocathodes (space-charge shielding provided by ions, rapid acceleration)



# Controlled pulse injection enables detailed control of injection phase space via laser

Room for improvement:

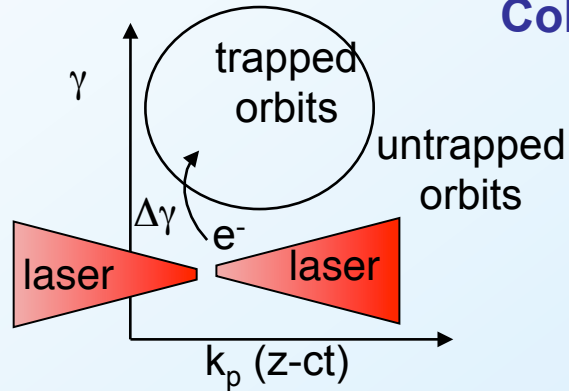
- **3-pulse** colliding pulse:
  1. control of injection position (by delay between pump and trailing pulses)
  2. lower colliding laser pulse intensity (less wake distribution)
- Phase velocity of beat separatrixes controlled by using different frequency laser pulses





# Controlled injection via colliding laser pulses improves beam quality

Theoretical development:

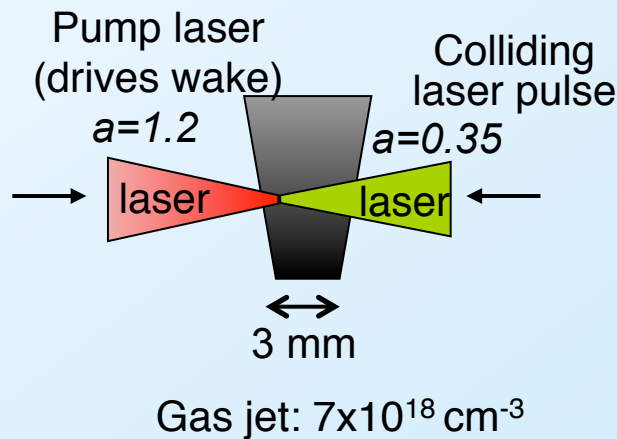


Colliding pulse injection:

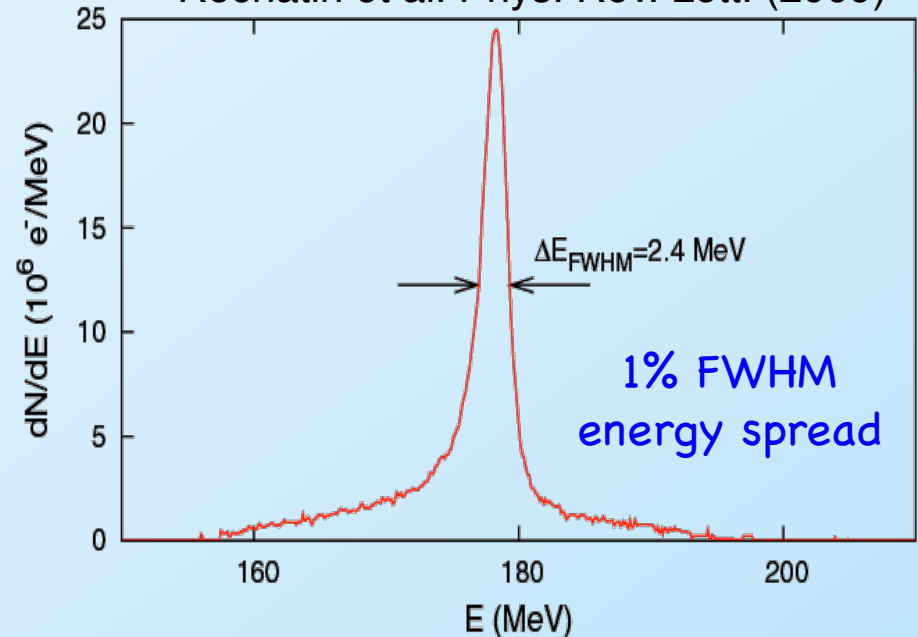
Esarey et al. PRL (1997);  
Schroeder et al. PRE (1999);  
Fubiani et al. PRE (2004)

Experimental demonstration:

LOA (France): Faure et al., Nature (2006)



Rechatin et al. Phys. Rev. Lett. (2009)





## Depletion: necessitates multiple stages

- Single stage energy gain limited by laser energy depletion
  - Diffraction limitation: mitigated by transverse plasma density tailoring
  - Dephasing limitation: mitigated by longitudinal plasma density tailoring

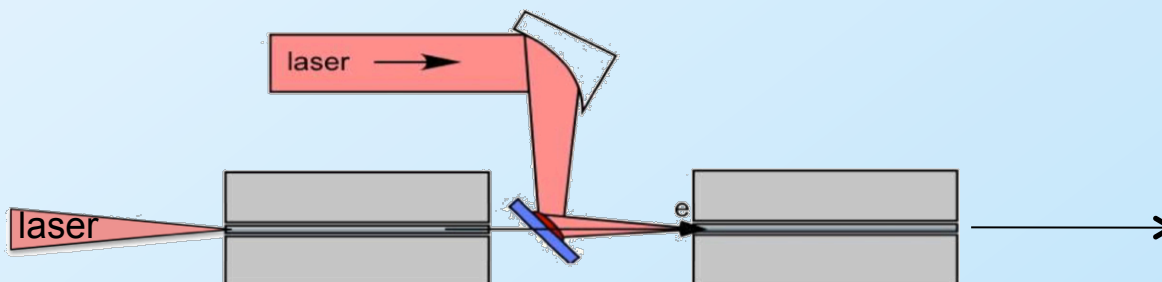
Depletion Length:  $L_D \propto \frac{1}{n_e^{3/2}}$

Accelerating field:  $E_0[\text{V/m}] \approx 100\sqrt{n[\text{cm}^{-3}]}$

Energy gain (linear regime):  $W_{\text{stage}}[\text{GeV}] \approx \frac{I[\text{W/cm}^2]}{n[\text{cm}^{-3}]}$

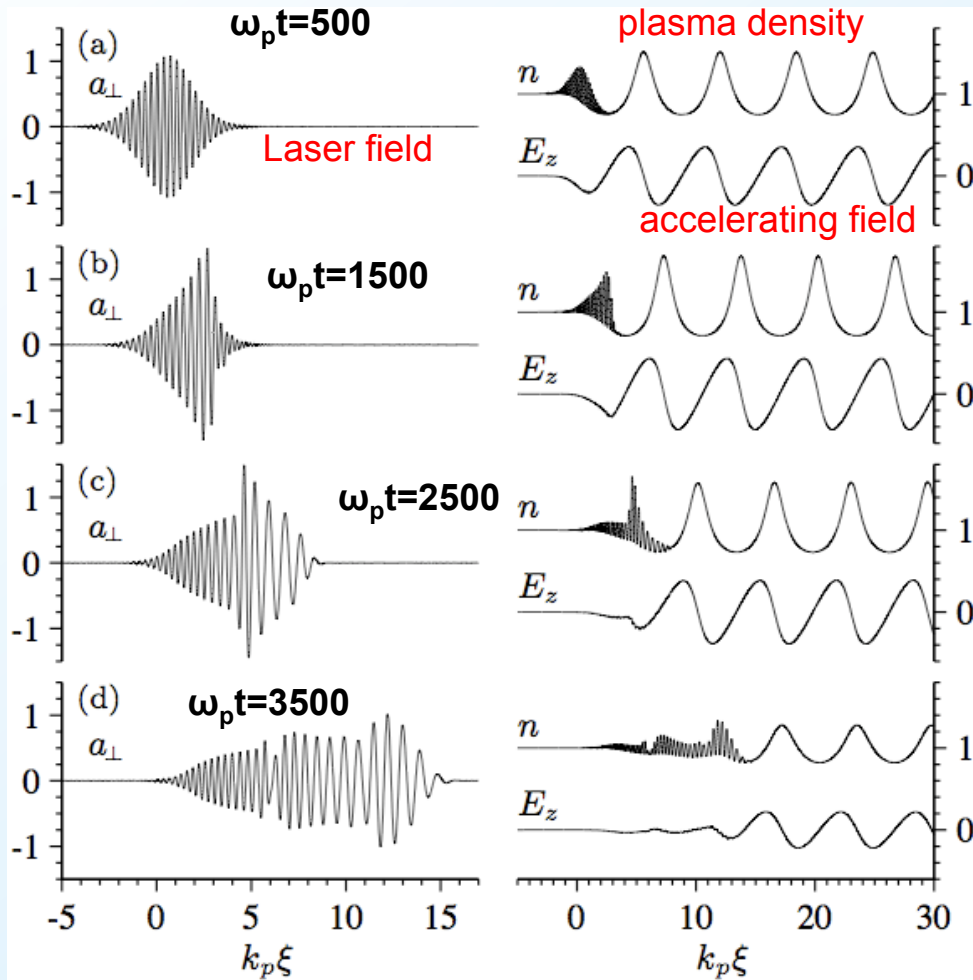
- Ex:  $W_{\text{stage}} = 10 \text{ GeV}$  for  $I = 10^{18} \text{ W/cm}^2$  and  $n = 10^{17} \text{ cm}^{-3}$

- Multiple-stages for controlled acceleration to high energy:



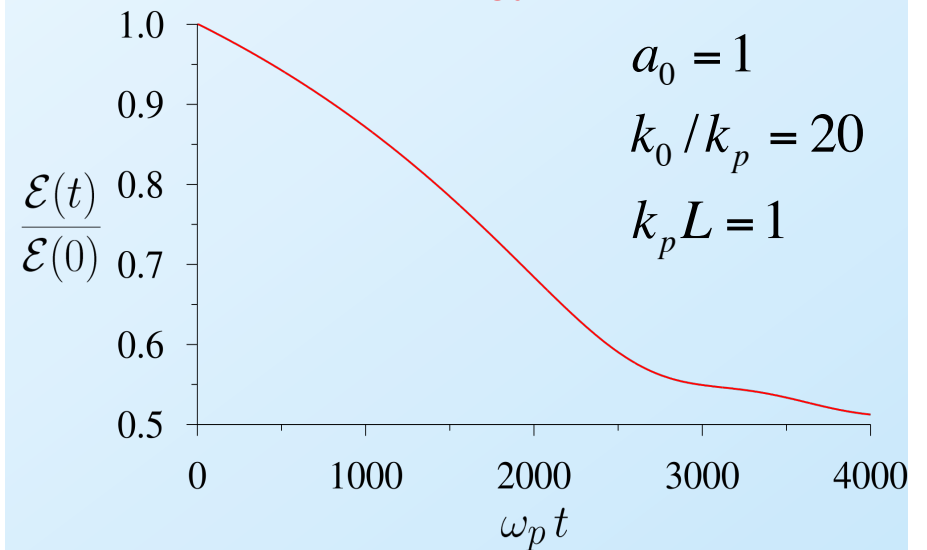


# Laser pulse evolution



$$a_0 = 8.6 \times 10^{-10} \lambda [\mu\text{m}] I^{1/2} [\text{W}/\text{cm}^{-2}]$$

Laser energy evolution:

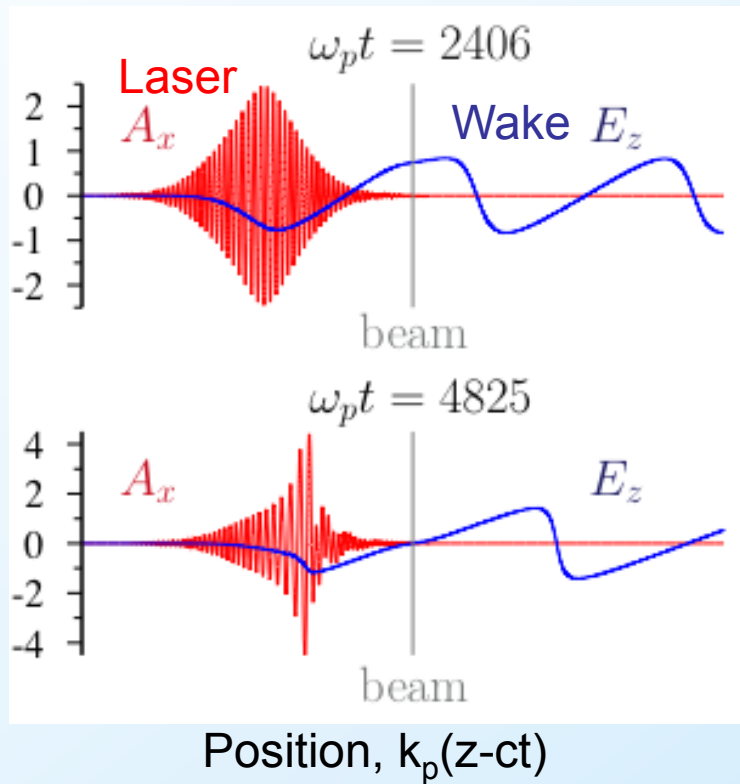


- Laser evolution interplay between laser intensity steepening, laser frequency red-shifting, energy depletion



# Longitudinal e-bunch dynamics: energy spread minimum near dephasing

Fluid plasma + e-bunch described by moments (includes beam loading)

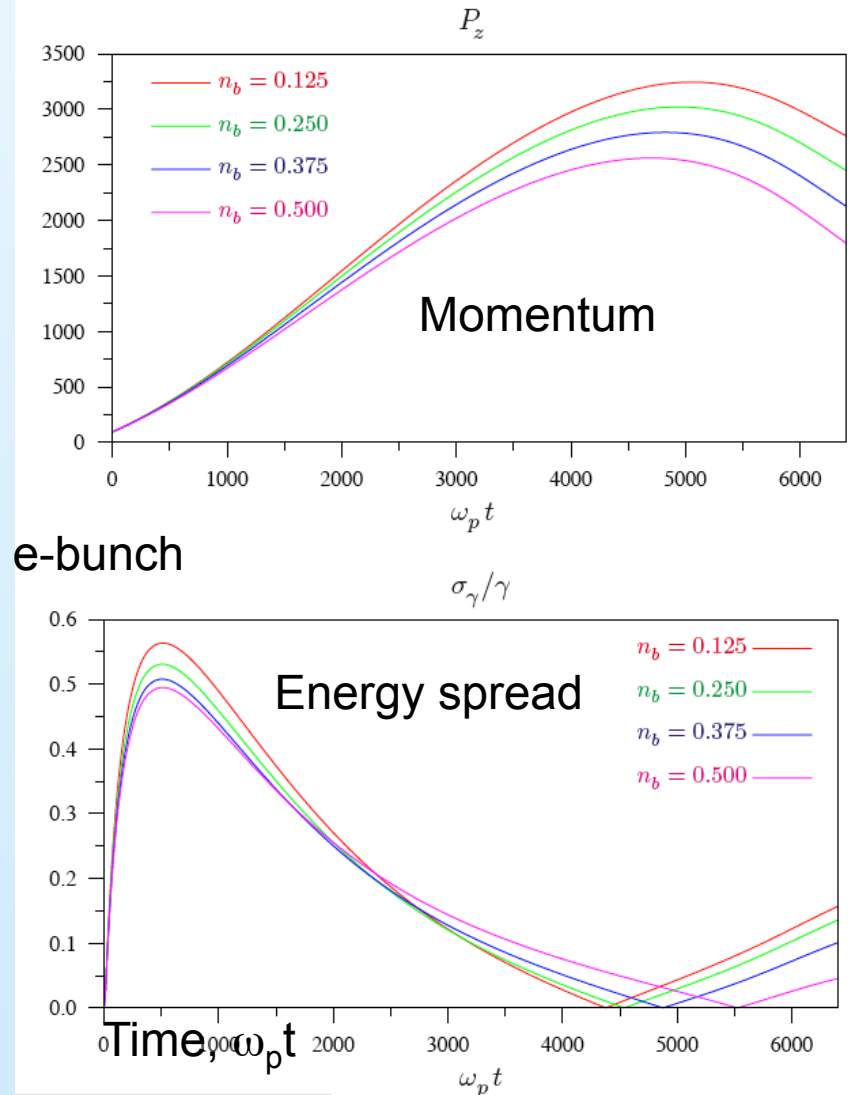


Energy spread

Initial:  $\sigma_\gamma/\gamma = 0.3\%$  at  $\gamma = 100$

Final:  $\sigma_\gamma/\gamma = 0.01\%$  at  $\gamma = 3000$

B.A. Shadwick et al.

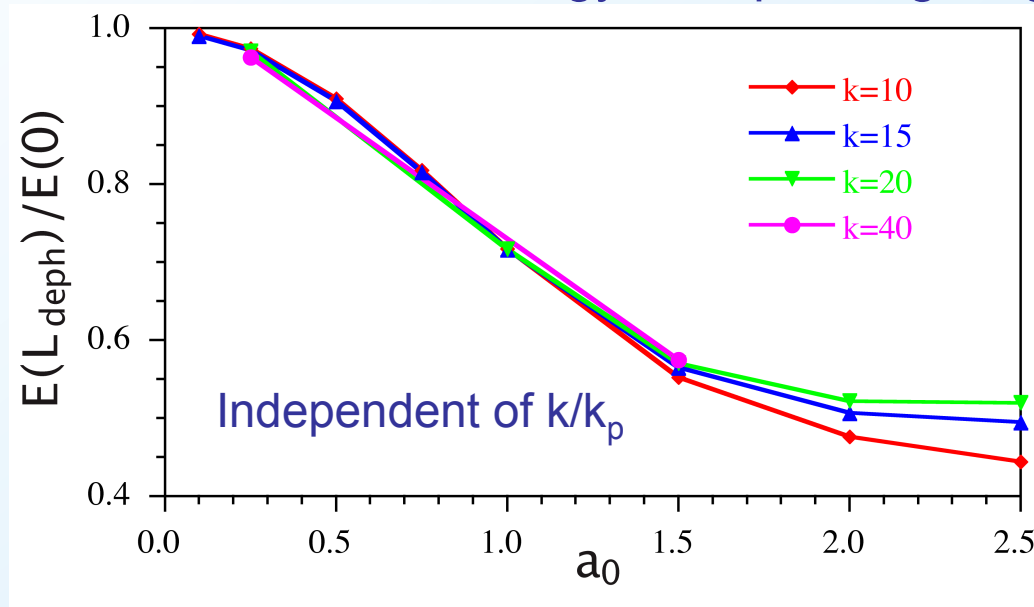






# Scaling laws from fluid code: dephasing/depletion lengths & energy gain

Fraction of laser energy at dephasing length



- Quasi-linear:  $a_0 \sim 1$ 
  - Dephasing  $\sim$  depletion
  - Good efficiency

- Fix laser parameters ( $a_0, k_p L_0, k_p r_0$ ), increase  $(k/k_p)$  to increase energy



## Point designs: 10 and 100 GeV

$a_0$	$P/P_c$	P(PW)	$W_L$	$t_0$ (fs)	$r_0$ ( $\mu\text{m}$ )	$\lambda_p$ ( $\mu\text{m}$ )	$n_0$ ( $\text{cm}^{-3}$ )	$L_{dp}$	$W_e$ (GeV)
2	2.2	0.38	40 J	98	53	80	$1.7 \times 10^{17}$	38 cm	10
1.5	1.1	0.30	40 J	130	63	99	$1.1 \times 10^{17}$	79 cm	10
1	0.45	0.22	40 J	170	82	140	$6.0 \times 10^{16}$	2.4 m	10
2	2.2	3.8	1.3 kJ	310	170	250	$1.7 \times 10^{16}$	12 m	100
1.5	1.1	3.0	1.3 kJ	390	200	310	$1.1 \times 10^{16}$	25 m	100
1	0.45	2.2	1.3 kJ	550	260	430	$6.0 \times 10^{15}$	78 m	100

Laser power:  $P[\text{GW}] = 21.5(a_0 r_0 / \lambda)^2$ , Critical power:  $P_c[\text{GW}] = 17(k/k_p)^2$ ,  $P/P_c = (a_0 k_p r_0)^2 / 32$ .  
 All assume:  $k_p L_0 = 2$ ,  $\lambda = 0.8 \mu\text{m}$



# Collider Requirements: Luminosity

- **Rate of events:** (luminosity) x (collision cross-section)
- **Luminosity:** cross-section  $\propto \gamma^{-2} \rightarrow L[10^{34} \text{ cm}^{-2} \text{ s}^{-1}] \approx (E_{cm}[\text{TeV}])^2$

$$L = \frac{fN^2}{4\pi\sigma_x\sigma_y} = \frac{P_b}{4\pi E_{cm}} \frac{N}{\sigma_x\sigma_y}$$

- For fixed beam power,  $P_b = 2fN_b(\gamma mc^2)$ , transverse beam density must be increased
- **Limitations:**
  - Achievable beam emittance
  - Final focus optics to IP: adiabatic plasma lens
  - Beam-beam interaction (beamstrahlung)
  - Emittance growth in main linacs (beam scattering in plasma)



# 1 TeV LPA Collider Parameters

## Plasma density scalings:

### Stage density scalings:

$$E_0 \propto n^{1/2}$$

$$L_{\text{stage}} \propto n^{-3/2}$$

$$W_{\text{stage}} \propto n^{-1}$$

$$U_L \propto n^{-3/2}$$

$$N_b \propto n^{-1/2}$$

### Collider density scalings (for fixed luminosity):

$$f \propto n$$

$$N_{\text{stage}} \propto n$$

$$P_b \propto n^{1/2}$$

$$P_{\text{laser}} \propto n^{-1/2}$$

Schroeder et al., AAC08

Plasma number density, $n_0$	$10^{17} \text{ cm}^{-3}$
Energy, center of mass, $E_{\text{cm}}$	1 TeV
Beam energy, $\gamma mc^2$	0.5 TeV
Number per bunch, $N$	$4 \times 10^9$
Collision rate, $f$	15 kHz
Beam Power, $P_b = fN\gamma mc^2$	4.8 MW
Luminosity, $\mathcal{L}$	$2 \times 10^{34} \text{ s}^{-1} \text{ cm}^{-2}$
Bunch length, $\sigma_z$	1 $\mu\text{m}$
Horizontal rms beam size at IP, $\sigma_x$	0.1 $\mu\text{m}$
Vertical rms beam size at IP, $\sigma_y$	1 nm
Horizontal normalized emittance, $\epsilon_{nx}$	1 mm-mrad
Vertical normalized emittance, $\epsilon_{ny}$	0.01 mm-mrad
Beamstrahlung parameter, $Y$	35
Plasma wavelength, $\lambda_p$	105 $\mu\text{m}$
Energy gain per stage, $W_{\text{stage}}$	10 GeV
Single stage laser-plasma interaction length	0.9 m
Drive laser coupling distance between stages	0.5 m
Laser energy per stage	40 J
Laser wavelength	1 $\mu\text{m}$
Initial normalized laser intensity, $a_0$	1.5
Average laser power per stage	600 kW
Number of stages	50
Main linac length	70 m
Efficiency (wall-plug to beam)	5%
Total wall-plug power	190 MW



# Collider power and efficiency requirements: High average power laser

- Beam power:  $P_b = fNE_{cm}$

$$\left. \begin{array}{l} N \sim 4 \times 10^9 \\ f \sim 15 \text{ kHz} \\ E_{cm} \sim 1 \text{ TeV} \end{array} \right\} P_b \sim 5 \text{ MW}$$

- AC wall-plug power:  $\sim 200 \text{ MW} \rightarrow 5\%$  efficiency

- Laser to plasma wave efficiency:  $\sim 50\%$
  - Plasma wave to beam efficiency:  $\sim 30\%$
- $\left. \begin{array}{l} \rightarrow \sim 15\% \text{ laser to beam efficiency} \\ \rightarrow \sim 33\% \text{ wall-plug to laser efficiency} \end{array} \right\}$

- Collider based on 10-GeV stages:

- (total beam energy  $\sim 300 \text{ J}$ )/(50 stages) =  $\sim 6 \text{ J/stage}$
- $\sim 40 \text{ J/laser}$  at  $15 \text{ kHz} = \sim 600 \text{ kW}$  average power laser

$\rightarrow$  beyond state-of-the-art laser technology  
 $\rightarrow$  Laser technology development required

- Energy remaining in plasma-based accelerator (damped plasma wave)
  - $\sim 10 \text{ J/stage}$  remains in plasma  $\rightarrow > 100 \text{ kW/m}$



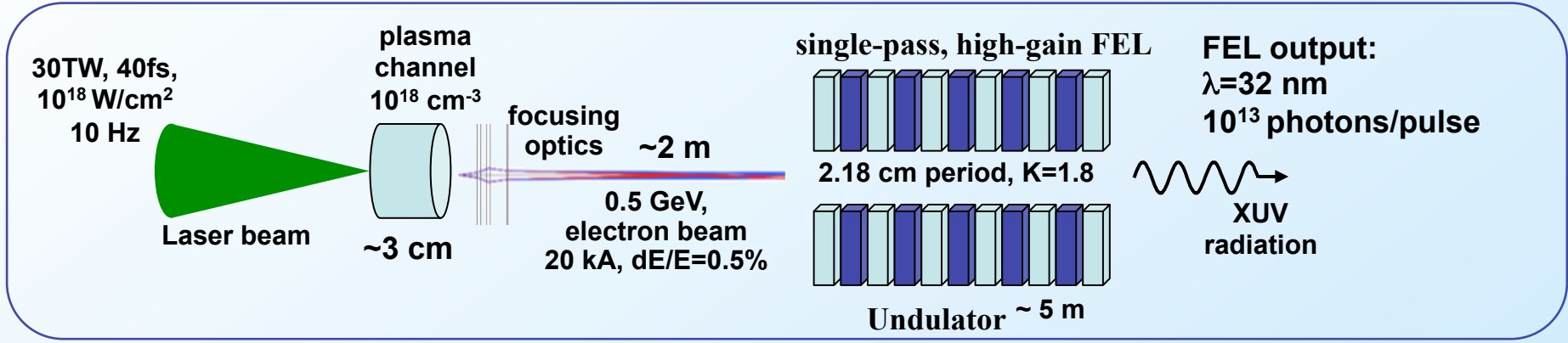
# BELLA: BErkeley Lab Laser Accelerator

- 1 PW laser facility
- 10 GeV electron beam from a meter long accelerator
- BELLA Project budget:
  - Funded by Office of Science – High Energy Physics
- Located in Bldg. 71 – old SUPERHILAC location
- Schedule: early finish mid 2012, CD-4 date: Dec. 2014
- CD-3 approval, ESAB signed: July 2010

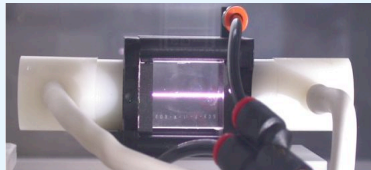
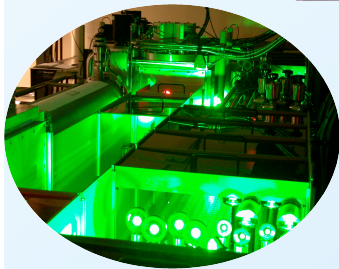




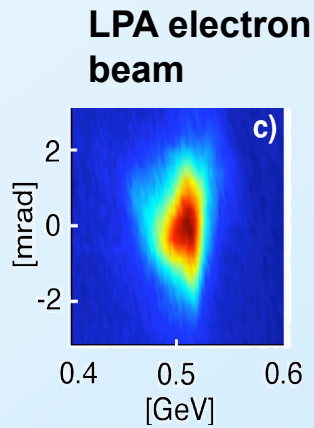
# Laser-plasma accelerator driven XUV FEL at LBNL



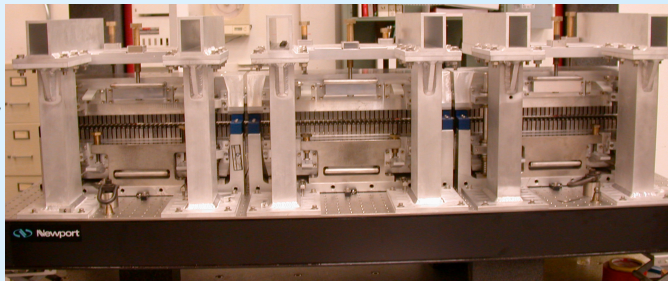
Ti:Al<sub>2</sub>O<sub>3</sub> laser system



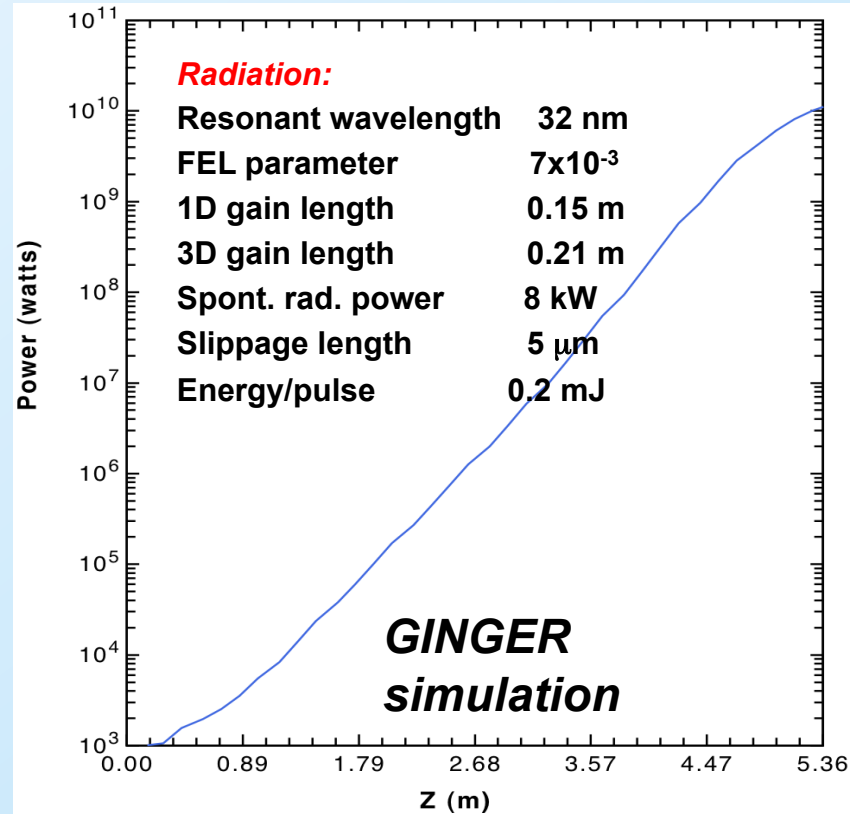
Plasma capillary technology



conventional undulator (THUNDER)



K. Robinson et al., IEEE QE (1987)





# Summary

- Laser plasma accelerators:
  - 1 GeV in  $< 3$  cm
  - BELLA Project will allow 10 GeV in  $< 1$  m
  - Developing techniques for beam control
  - Laser technology maturing rapidly
- Applications:
  - Compact accelerator for basic science
    - Collider based on 10 GeV LPA stages
  - Medical, homeland security
  - Compact light source based on Berkeley's LPA technology
    - 5<sup>th</sup> generation light source: LPA-FEL
- Students and postdocs from all over the world:
  - Award winning dissertations, more than 15 PhD's through program and ~ 80 students (MS and undergrad)