



# Unit 11

## Electromagnetic design

### Episode III

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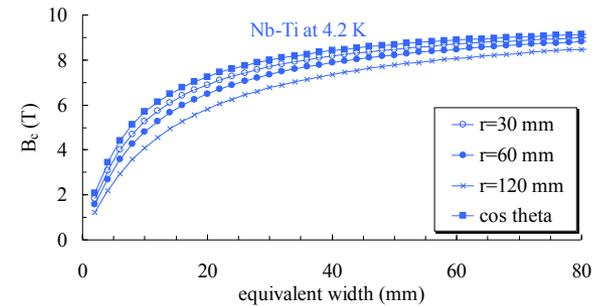
Lawrence Berkeley National Laboratory (LBNL)

*With significant re-use of material from the same unit lecture by Ezio Todesco, USPAS 2017*



# QUESTIONS

- Where can we operate the magnet ? How far from the critical surface ?
- Efficiency: the last Teslas are expensive ... are there **techniques to save conductor** ?



- What is the **effect of iron** ? Does it yield higher short sample fields ?
- What happens in **coil ends** ?
- Are there **other possible lay-outs** ?



# CONTENTS



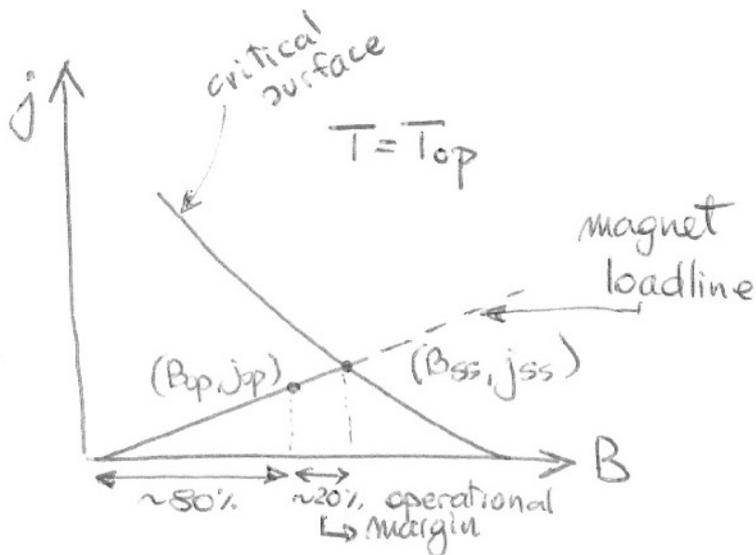
1. Operational margin
2. Grading techniques
3. Iron yoke
4. Coil ends
5. Other designs
6. A review of dipole and quadrupole lay-outs



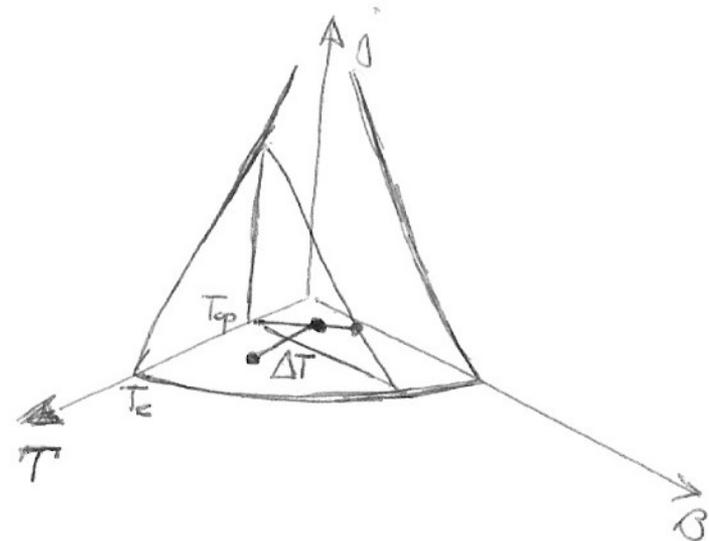
# Margin and operational risk



- Magnets have to work at a given distance from the critical surface, i.e. they are **never operated at short sample** conditions
  - At short sample, any small perturbation quenches the magnet
  - One usually operates at a **fraction of the loadline** which ranges from **60% to 90%**



Loadline with 20% operational margin



Operational margin and temperature margin

- This fraction translates into a **temperature margin**



# Temperature margin is a common figure of merit

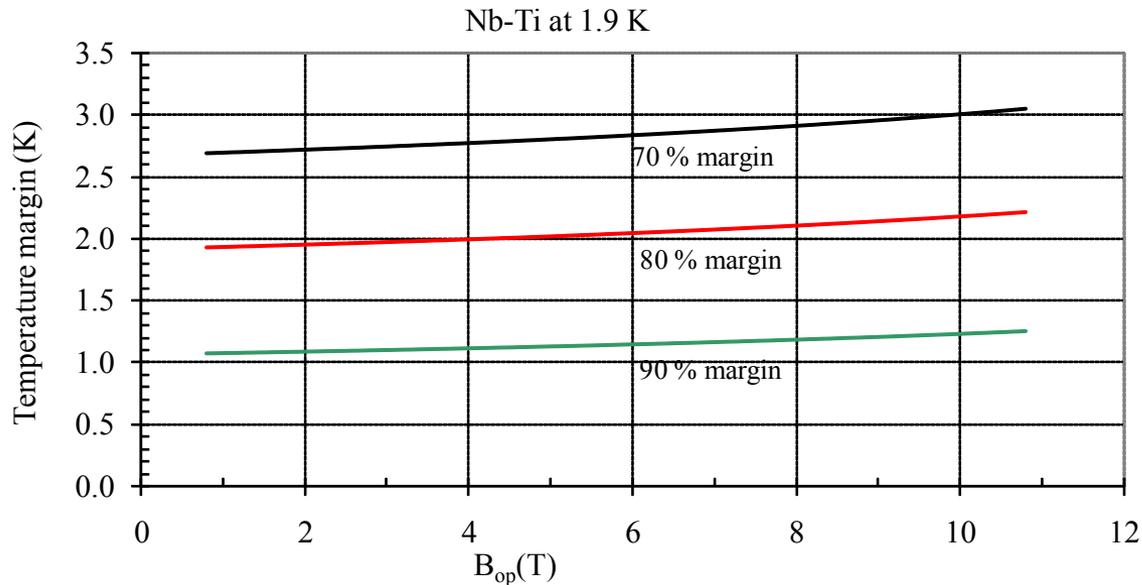


● How to compute the **temperature margin** ?

● One needs an **analytic fit** of the critical surface  $j_{ss}(B, T)$

● The temperature margin  $\Delta T$  is defined by **the implicit equation**

$$j_{ss}(B_{op}, T_{op} + \Delta T) = j_{op}$$



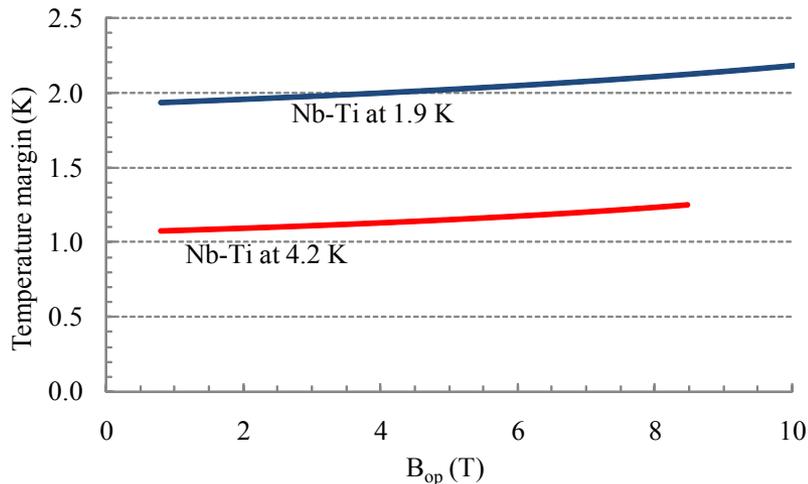
● Nb-Ti at 1.9 K at 80% of the loadline has about 2 K of temperature margin



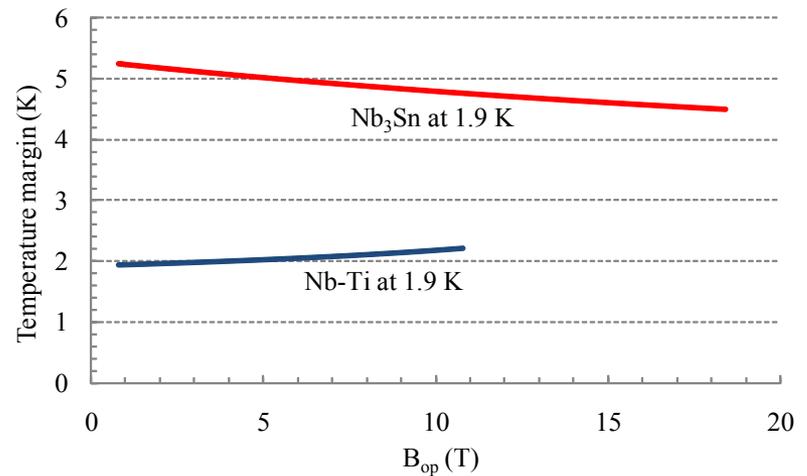
# Examples of temperate margin and role of superconductor

## Some parametric analysis

- Nb-Ti at 4.2 K loses at least **1/3 of temperature margin w.r.t. 1.9 K**
  - But the specific heat is larger ...
  - But helium is not superfluid ...
- Nb<sub>3</sub>Sn has a temperature margin **2.5 times larger than Nb-Ti**
  - This is due to the shape of the critical surface
  - At 80%, Nb<sub>3</sub>Sn has about 5 K of temperature margin



Temperature margin of Nb-Ti at 1.9 K and at 4.2 K



Temperature margin of Nb-Ti versus Nb<sub>3</sub>Sn



# Transient vs steady losses



## ● Two regimes

### 1. Fast losses or fast release of energy ( $\text{J}/\text{cm}^3$ )

- **Adiabatic case** – all heat stays there
- Main issue: the conductor must have high enough thermal inertia
- The deposited energy must not exceed the enthalpy margin
- **Enthalpy margin** is the critical parameter

### 2. Continuous losses (as debris coming from collisions, or losses from the beam) ( $\text{W}/\text{cm}^3$ )

- All heat is removed – **stationary case**
- Main issue: the heat must be extracted efficiently
- The gradient between the heat sink and the coil must not exceed the temperature margin
- **Temperature margin** is the critical parameter



## ● The idea

- The map of the field inside a coil is **strongly non-uniform**
- In a two layer configuration, the **peak field is in the inner layer**, and outer layer has systematically a lower field
- A **higher current density** can be put in the **outer layer**

## ● How to realize it

- First option: use **two different power supplies**, one for the inner and one for the outer layer (not common)
- Second option: use a different cable for the outer layer, with a smaller cross-section, and **put the same current** (cheaper)
  - The inner and outer layer have a splice, and they share the same current
  - Since the outer layer cable has a smaller section, it has a higher current density



# Examples of graded dipoles

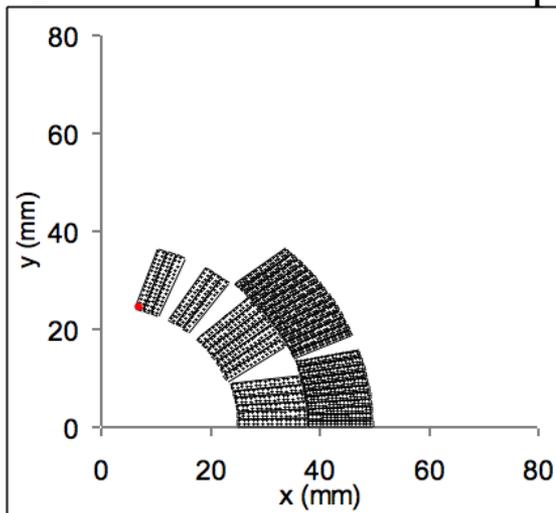
## ● Examples of **graded coils**

### ● LHC main dipole (~9 T)

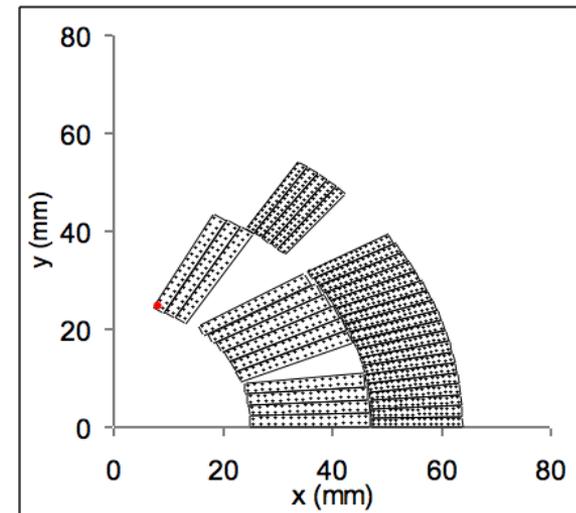
- grading of 1.23 (i.e. +23% current density in outer layer)
- 3% more in short sample field, **17% save of conductor**

### ● MSUT - Nb<sub>3</sub>Sn model of Univ. of Twente (~11 T)

- strong grading 1.65
- 5% more in short sample field, **25% save of conductor**



LHC main dipole



MSUT dipole



# We can study graded magnets using the tools defined earlier



## ● **Short sample limit** for a graded Nb-Ti dipole

- Each block has a current density  $j_1 \dots j_n$ , each one with a dilution factor  $\kappa_1 \dots \kappa_n$

- We fix the ratios between the current densities

$$\chi_1 \equiv \frac{j_1}{j_1} = 1 \quad \chi_2 \equiv \frac{j_2}{j_1} \quad \chi_n \equiv \frac{j_n}{j_1}$$

- We define the **ratio between central field and current densities**

$$B = \sum j_n \gamma_{c,n} \equiv j_1 \gamma_c$$

- We define the ratio between **peak field** in each block and central field

$$B_{p,n} \equiv \lambda_n B = \lambda_n \gamma_c j_1 = \frac{1}{\chi_n} j_n \lambda_n \gamma_c$$



- **Short sample limit** for a graded Nb-Ti dipole (continued I)

$$B = \sum j_n \gamma_{c,n} \equiv j_1 \gamma_c \qquad B_{p,n} = \frac{1}{\chi_n} j_n \lambda_n \gamma_n$$

- In each layer one has  $j_{c,n} \leq \kappa_n s (B_{c2}^* - B_{p,n})$   
and substituting the peak field expression one has

$$j_{c,n} \leq \frac{\chi_n \kappa_n s}{\chi_n + \lambda_n \kappa_n s \gamma_c} B_{c2}^*$$

- All these  $n$  conditions have to be satisfied – since the current densities ratios are fixed, one has

$$j_{c,1} = \frac{j_{c,n}}{\chi_n} \leq \frac{\kappa_n s}{\chi_n + \lambda_n \kappa_n s \gamma_c} B_{c2}^*$$

$$j_{c,1} = \text{Min}_n \frac{\kappa_n s}{\chi_n + \lambda_n \kappa_n s \gamma_c} B_{c2}^*$$



# How to calculate the short sample limit

## ● Short sample limit for a graded Nb-Ti dipole (continued II)

● The **short sample current is** 
$$j_{c,1} = \text{Min}_n \frac{SK_n}{\chi_n + \lambda_n SK_n \gamma_c} B_{c2}^*$$

● and the **short sample field is** 
$$B_{ss} = \text{Min}_n \frac{SK_n \gamma_c}{\chi_n + \lambda_n SK_n \gamma_c} B_{c2}^*$$

### ● Comments

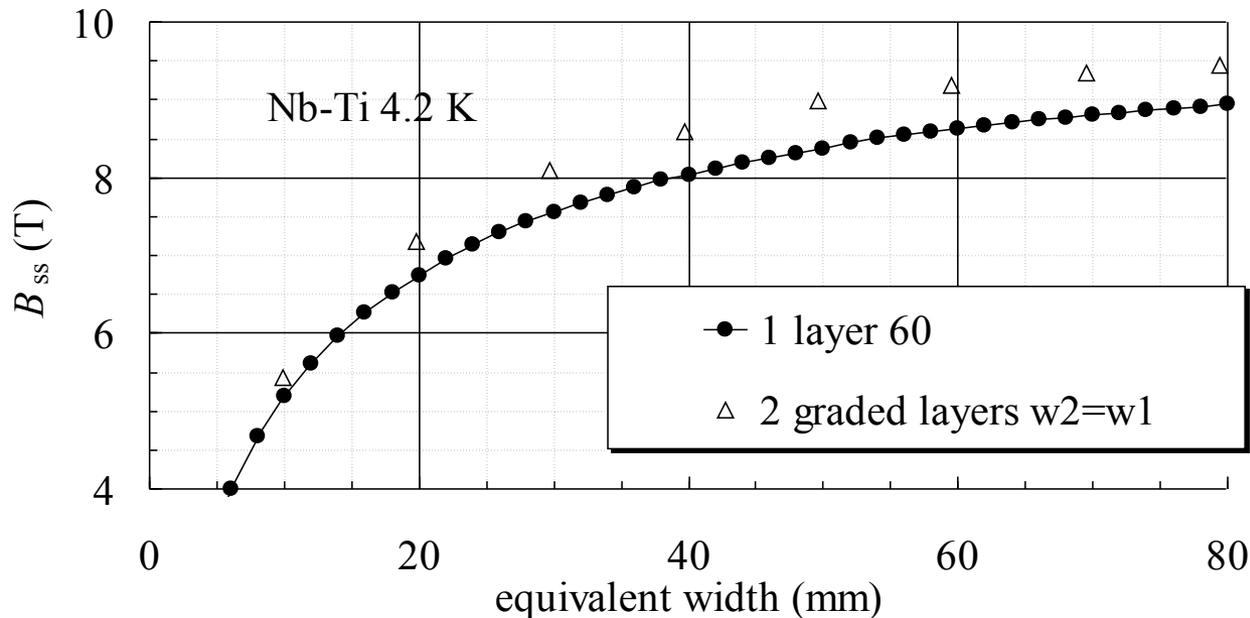
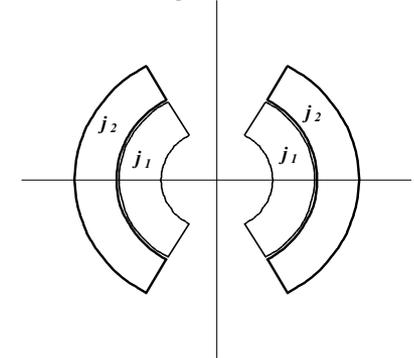
- The grading factor  $\chi$  in principle should be pushed to maximize the short sample field
- A limit in high grading is given by **quench protection issues**, that limit the maximal current density – in general the outer layer has lower filling factor to ease protection
- Please note that the equations **depend on the material** – a graded lay-out optimized for Nb-Ti will not be optimized for Nb<sub>3</sub>Sn



# Comparison of single layer vs graded 2-layer

● Results for a two layer **with same width** sector case, Nb-Ti

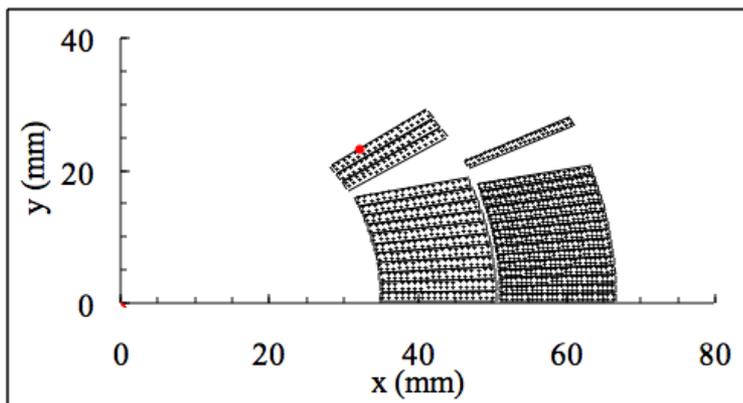
- The gain in short sample field is ~5%
- But given a short sample field, one saves a lot !
  - At 8 T one can use 30 mm instead of 40 mm (-25%)
  - At 9 T one can use 50 mm instead of 80 mm (-37%)



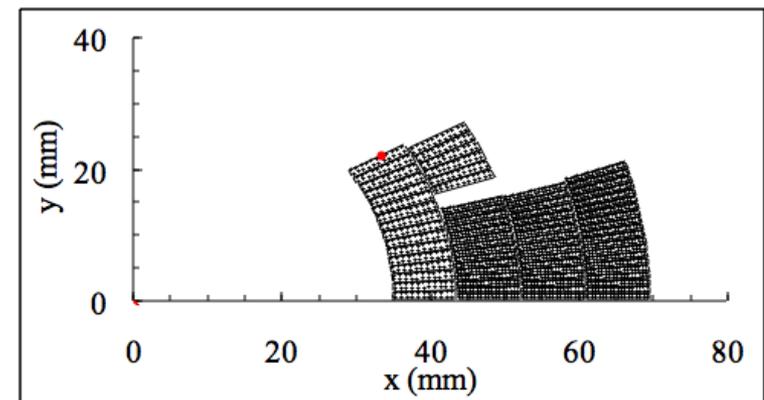


# Now apply the technique to quadrupoles

- Similar strategy for quadrupoles – gain of 5-10% in  $G_{ss}$ 
  - LHC MQXB – quadrupole for IR regions
    - grading of 1.24 (i.e. +24% current density in outer layer)
    - 6% more in short sample field, **41% save of conductor**
  - LHC MQY – quadrupole close to IR regions
    - Special grading (grading inside outer layer, upper pole with lower density) of 1.43
    - 9% more in short sample field, **could not be reached without grading**



LHC MQXB



LHC MQY



# Some basic comments concerning the use of iron



- An **iron yoke** usually surrounds the collared coil – it has several functions
  - Keep the return magnetic flux close to the coils, thus avoiding fringe fields
  - In some cases the iron is partially or totally contributing to the **mechanical structure**
    - RHIC magnets: no collars, plastic spacers, iron holds the Lorentz forces
    - LHC dipole: very thick collars, iron give little contribution
  - Considerably **enhance the field** for a given current density
    - The increase is relevant (10-30%), getting higher for thin coils
    - This allows using lower currents, easing the protection
  - Increase the short sample field
    - The increase is **small (a few percent)** for “large” coils, but can be considerable for small widths
    - This action is effective when we are far from reaching the asymptotic limit of  $B_{c2}^*$



# How to size the iron - for shielding

- A **rough estimate** of the **iron thickness** necessary to avoid fields outside the magnet
  - The iron cannot withstand more than 2 T (see discussion on saturation, later)
  - **Shielding condition** for dipoles:  $rB \sim t_{iron} B_{sat}$ 
    - i.e., the iron thickness times 2 T is equal to the central field times the magnet aperture - One assumes that all the field lines in the aperture go through the iron (and not for instance through the collars)
    - Example: in the LHC main dipole **the iron thickness is 150 mm**

$$t_{iron} \sim \frac{rB}{B_{sat}} = \frac{28 * 8.3}{2} \sim 100 \text{ mm}$$

- Shielding condition for quadrupoles:  $\frac{r^2 G}{2} \sim t_{iron} B_{sat}$



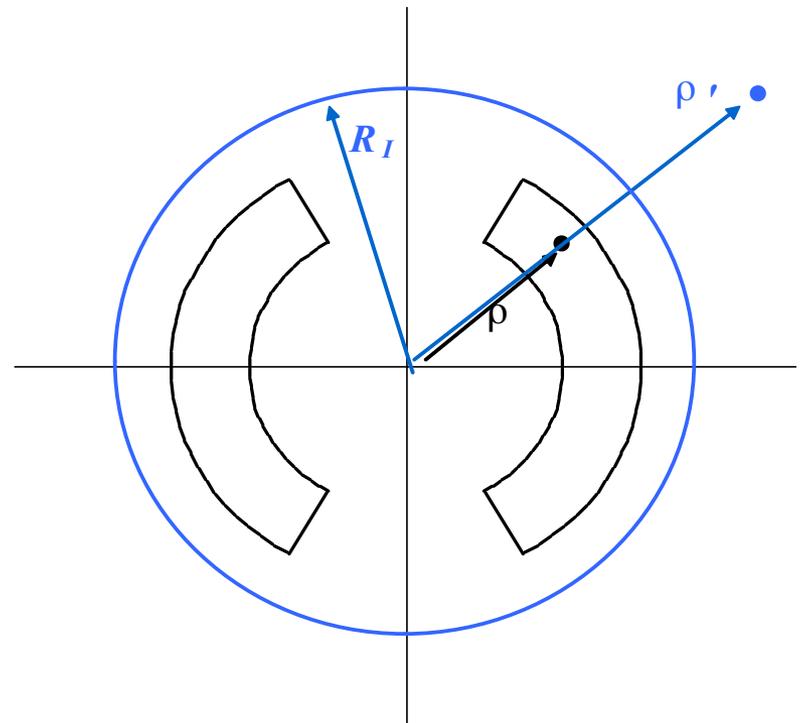
# We can analyze the influence of iron using image currents

● The iron yoke contribution can be estimated analytically for **simple geometries**

- Circular, non-saturated iron: **image currents** method
- Iron effect is equivalent to add to each current line a second one

- at a distance  $\rho' = \frac{R_I^2}{\rho}$
- with current  $I' = \frac{\mu - 1}{\mu + 1} I$

● Limit of the approximation: iron is not saturated (less than 2 T)

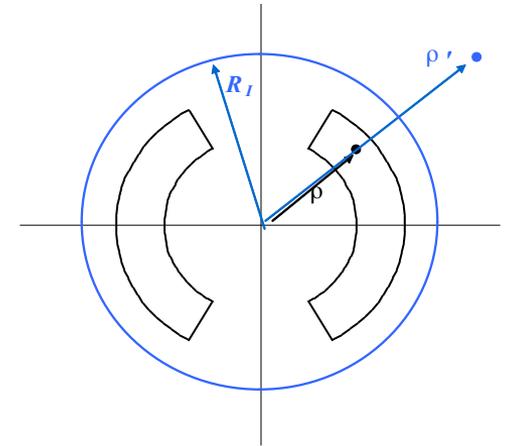




## ● Remarks on the equations

$$\rho' = \frac{R_I^2}{\rho} \quad I' = \frac{\mu - 1}{\mu + 1} I$$

- When iron is not saturated, one has  $\mu \gg 1$  and then  $I' = I$
- Since the image is far from the aperture, its impact on **high order multipoles is small**
- The impact of the iron is **negligible** for
  - Large coil widths
  - Large collar widths
  - High order multipoles
- The iron can be relevant for
  - **Small coil** widths, **small collar** widths, **low order** multipoles, main component
- At most, iron can double the main component for a given current density (i.e. can give a  $\Delta\gamma=100\%$ )
  - This happens for infinitesimally small coil and collar widths





# Iron influence on main field

$$B = \gamma_c J_E$$

- Estimate of the **gain in main field**  $\Delta\gamma$  for a sector coil

$$B_1 = kjw$$

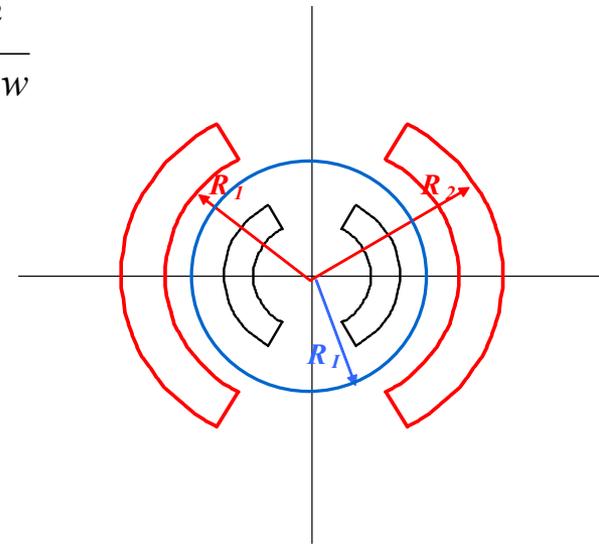
$$\Delta B_1^{iron} = kj'(R_2 - R_1)$$

$$R_1 = \frac{R_I^2}{r + w}$$

*k is just a temporary transfer function term...*

$$\frac{\Delta B_1^{iron}}{B_1} = \frac{j'(R_2 - R_1)}{jw}$$

$$R_2 = \frac{R_I^2}{r}$$



the current density has to satisfy the integral condition

$$j [(r + w)^2 - r^2] = \frac{\mu - 1}{\mu + 1} j' [R_2^2 - R_1^2]$$

and one obtains

$$\frac{\Delta B_1^{iron}}{B_1} = \frac{\mu - 1}{\mu + 1} \frac{(r + w)r}{R_I^2}$$

- For higher order multipoles

- The relative contribution becomes very small

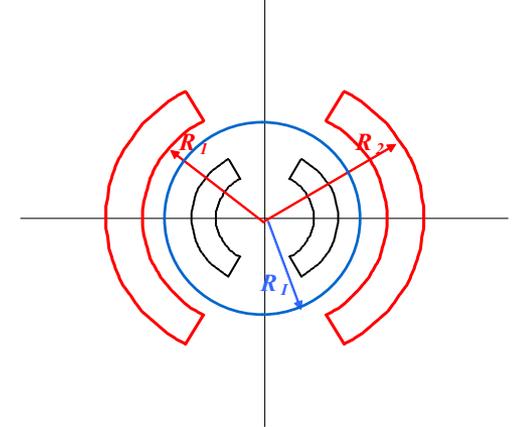
$$\frac{\Delta B_n^{iron}}{B_n} = \frac{\mu - 1}{\mu + 1} \left[ \frac{(r + w)r}{R_I^2} \right]^n$$



# Examples of iron enhancement to main field

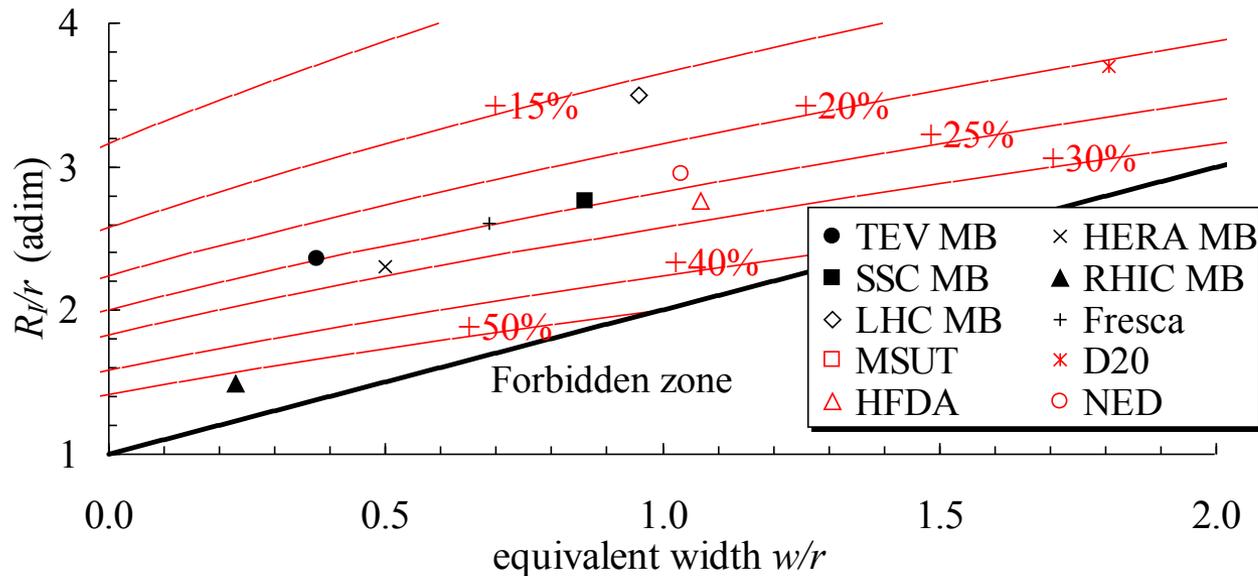
- Estimate of the gain in main field for fixed current in a sector coil

$$\frac{\Delta B_1^{iron}}{B_1} = \frac{\mu - 1}{\mu + 1} \frac{(r + w)r}{R_I^2}$$



## Examples of several built dipoles

- Smallest: LHC ~16% (18% actual value)
- Largest: RHIC ~55% (56% actual value)





# Influence of iron on short sample field

- Impact of the iron yoke on dipole short sample field, Nb-Ti

$$B_{ss} = \frac{\kappa s \gamma_c}{1 + \lambda \kappa s \gamma_c} B_{c2}^*$$

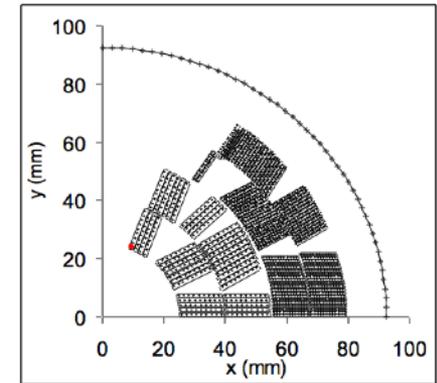
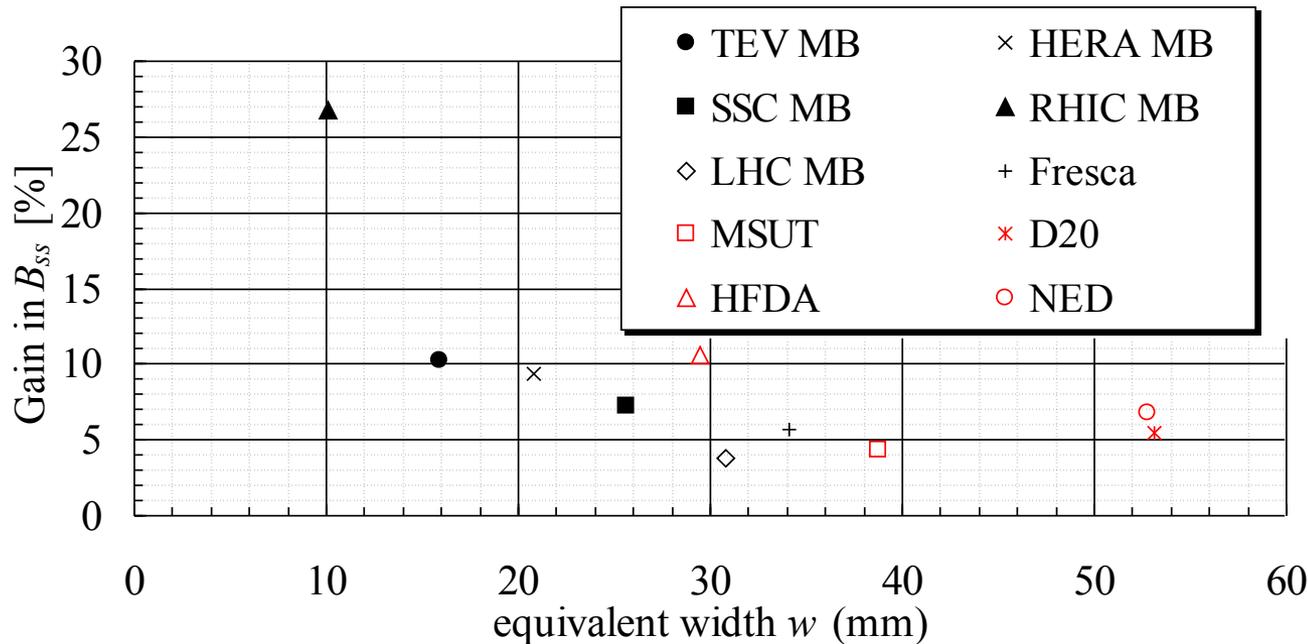
- The change of  $\gamma_c$  is the change of B for a fixed current, previously computed
  - Two regimes:
    - for  $\lambda \kappa s \gamma_c \ll 1$  the increase in  $\gamma$  corresponds to the same increase in the short sample field (“thin coils”)
    - for  $\lambda \kappa s \gamma_c \gg 1$  no increase in the short sample field (“thick coils”)
    - Please note that the “thin” and “thick” regimes depend on filling ratio  $\kappa$  and on the slope  $s$  of the critical surface
  - For the Nb<sub>3</sub>Sn one has to use the corresponding equations
    - Phenomenology is similar, but quantitatively different



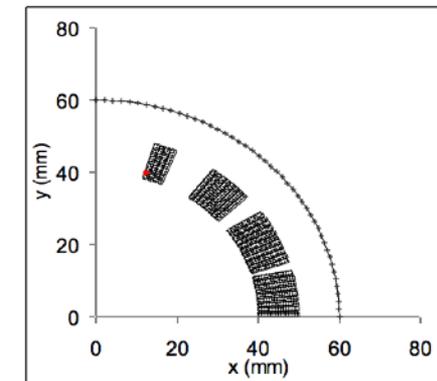
# Examples of iron influence



- Impact of the iron yoke on short sample field
  - Large effect (25%) on RHIC dipoles (thin coil and collars)
  - Between **4% and 10%** for most of the others  
(both Nb-Ti and Nb<sub>3</sub>Sn)



D20 and yoke



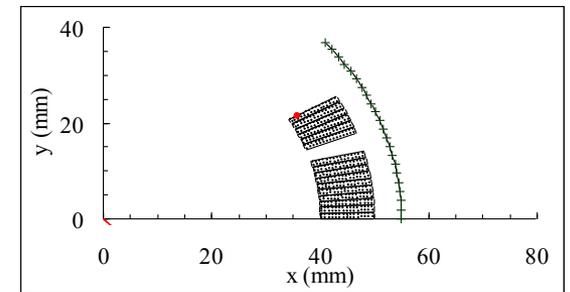
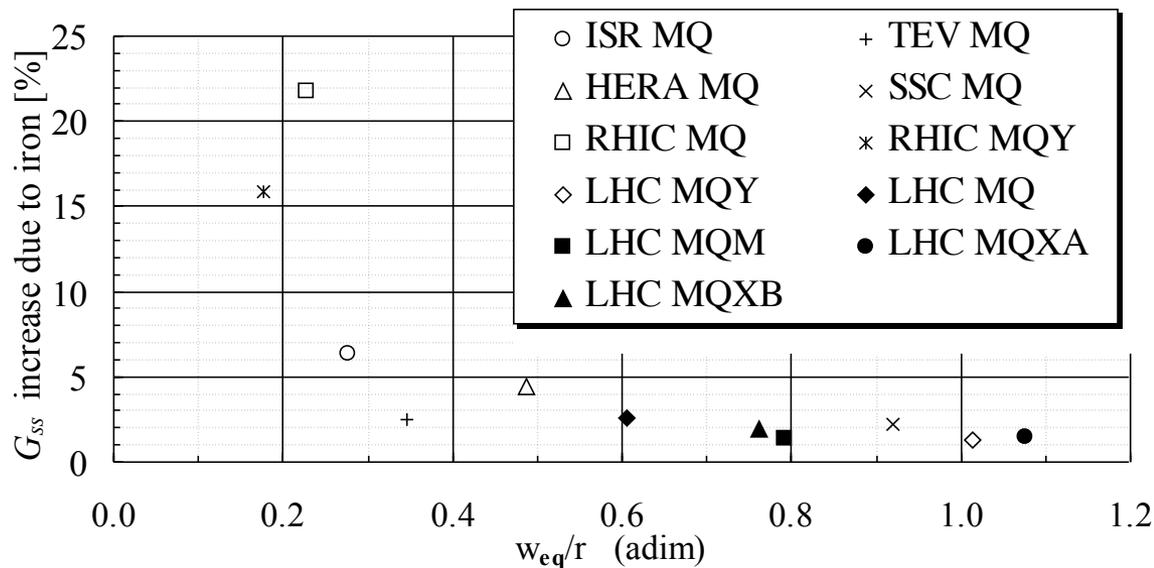
RHIC main dipole and yoke



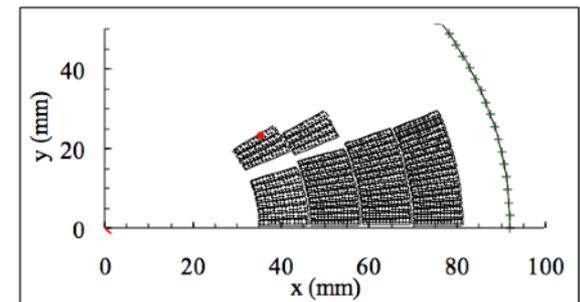
# Influence of iron on quadrupole field strength

● Similar approach can be used in quadrupoles

- Large effect on RHIC quadrupoles (thin coil and collars)
- Between 2% and 5% for most of the others
- The effect is smaller than in dipoles since the contribution to  $B_2$  is smaller than to  $B_1$



RHIC MQ and yoke



LHC MQXA and yoke

# Influence of iron is strongly field-dependent

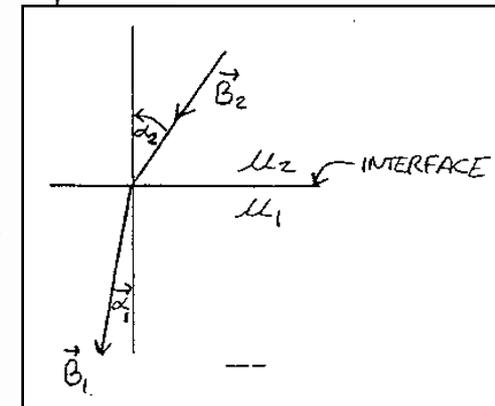
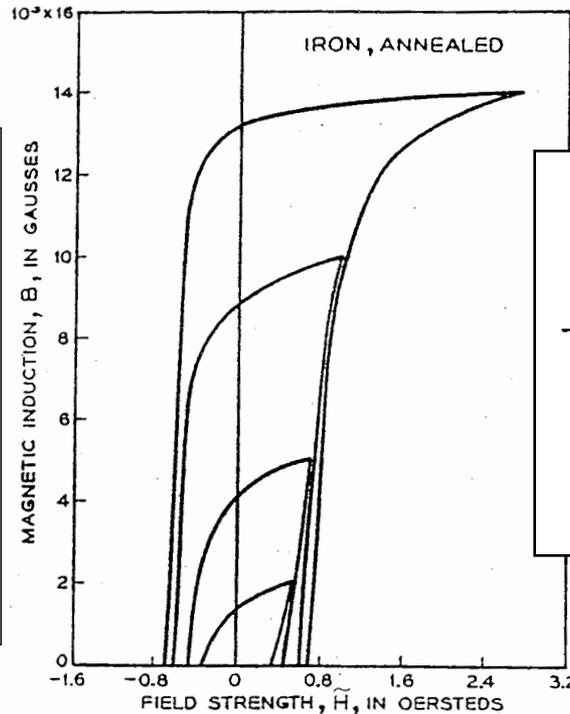
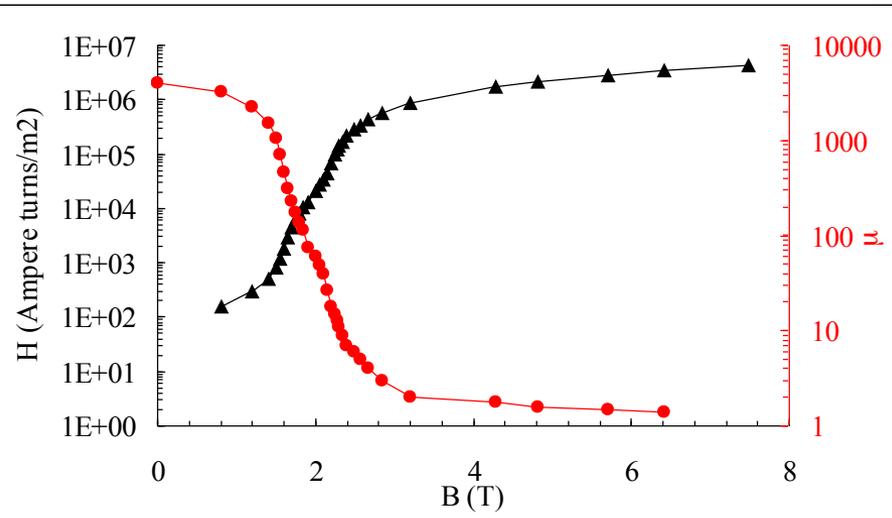
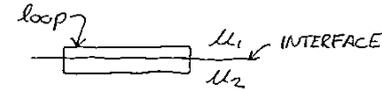
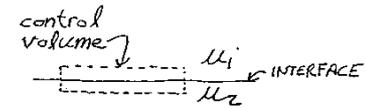
● Iron saturation: **B-H curve**  $B = \mu\mu_0 H$

- for  $B < 2$  T, one has  $\mu \gg 1$  ( $\mu \sim 10^3 - 10^4$ ), and the **iron can give a relevant contribution** to the field according to what discussed before
- for  $B > 2$  T,  $\mu \rightarrow 1$ , and the **iron becomes "transparent"** (no effect on field)

Continuity across an interface:

$$\vec{\nabla} \cdot \mathbf{B} = 0 \Rightarrow \Delta B_{\perp} = 0$$

$$\vec{\nabla} \times \mathbf{H} = 0 \Rightarrow \Delta H_{\parallel} = 0$$



Upper halves of hysteresis loops of ordinary annealed iron



# Iron saturation complicates modeling and analysis



## ● Impact on calculation

- When iron saturates → image current method cannot be applied, **finite element** method is needed (Poisson, Opera, Ansys, Roxie, ...)
- Accuracy of model is good (error less than 10% if B-H well known)

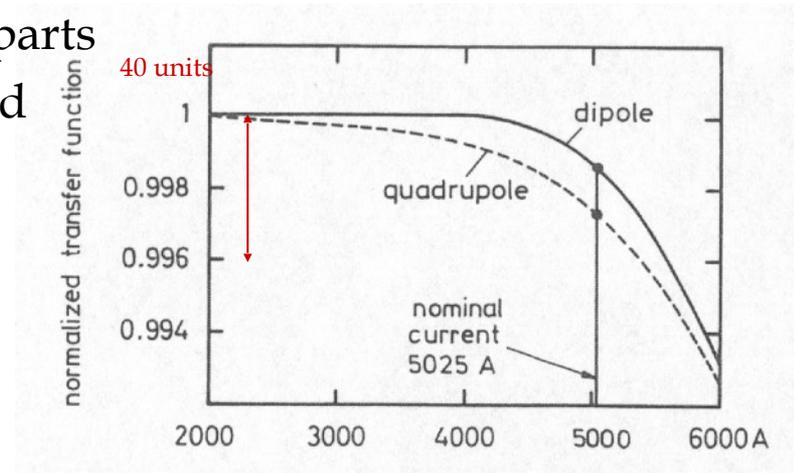
## ● Impact on main component and multipoles

- The main field is not  $\propto$  current → transfer function  **$B/i$  drops**
- Since the field in the iron has an

azimuthal dependence, some parts of the iron can be saturated and others not → **variation of  $b_3$**

## ● It **was considered critical**

- Led to warm iron design in Tevatron
- Today, even few % of saturation seem manageable in operation



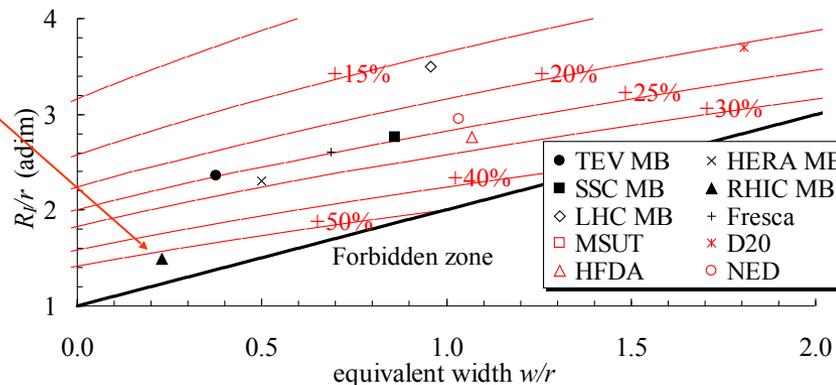
Impact of yoke saturation in HERA dipole and quadrupoles, From Schmuser, pg 58, fig. 4.12



# Optimization of iron yoke to compensate for saturation effects

## ● Corrective actions: **shaping the iron**

- In a dipole, the field is larger at the pole – iron will saturate there first
  - The dependence on the azimuth of the field in the coil provokes different saturations, and a strong impact on multipole
- One can **optimize** the shape of the iron to **reduce these effects**
  - Optimization of the **position of holes** (holes anyway needed for cryogenics) to minimize multipole change
  - **RHIC is the most challenging case**, since the iron gives a large contribution (50% to  $\gamma$ , i.e. to central field for a given current)

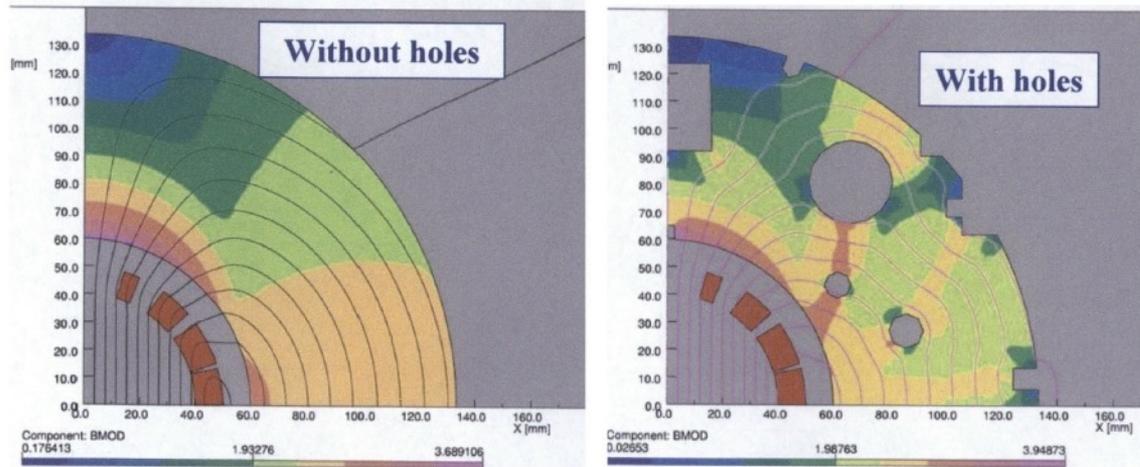




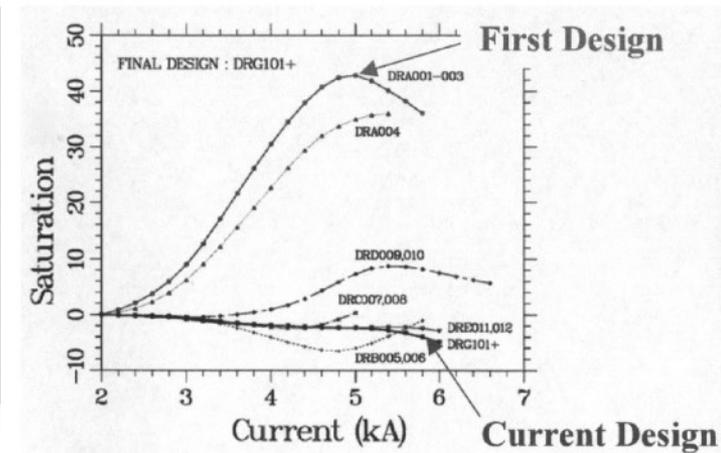
# Examples of iron shaping - RHIC

## ● Corrective actions: **shaping the iron** – the RHIC dipole

- The field in the yoke is larger on the pole
- Drilling holes in the right places, one can **reduce saturation impact on  $b_3$**  from 40 units to less than 5 units (**one order of magnitude**), and to correct also  $b_5$



Field map in the iron for the RHIC dipole, with and without holes  
From R. Gupta, USPAS Houston 2006, Lecture V, slide 12



Correction of  $b_3$  variation due to saturation for the RHIC dipoles, R. Gupta, ibidem

## ● A similar approach has been used for the LHC dipole

- Less contribution from the iron (20% only), but left-right asymmetries due to two-in-one design [S. Russenschuck, C. Vollinger, ...]

## ● Another possibility is to **shape the contour of the iron** (elliptical and not circular)



# Magnet end design is a critical issue

## ● Main features of the coil end design

++Mechanical: find the shape that minimizes the strain in the cable due to the bending (constant perimeter)

- In a  $\cos(\theta)$  magnet this **strain can be large** if the aperture is small
- In a racetrack design the cable is bent in the 'right' direction and therefore the strain is much less
- It is important to have codes to design the end spacers that **best fit the ends**, giving the best mechanical support – iteration with results of production is usually needed



End of a  $\cos\theta$  coil  
[S. Russenschuck, World Scientific, Fig. 32.13]



End spacers supporting the ends of a  $\cos\theta$  coil  
[S. Russenschuck, World Scientific, Fig. 32.13]

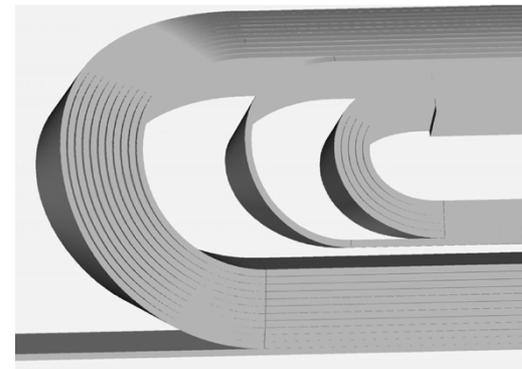


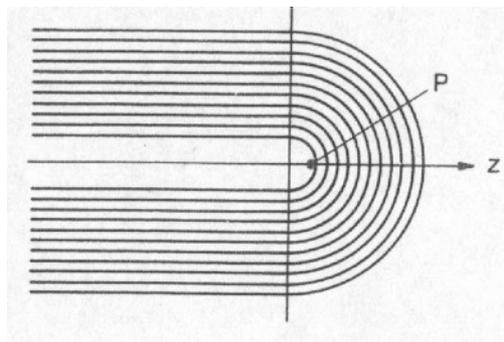
Fig. 2. Typical turns generated by BEND loaded into the CAD ProE program.  
Caspi, Ferracin TAS Vol 16, 2006



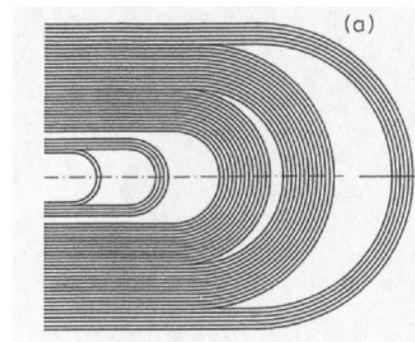
# Figure of merit for end design

## ● Main features of the coil end design

- + Magnetic: find the shape that allows to **avoid a higher field in the ends**
  - Due to the coil return, the main field in the ends is enhanced (typically several %)
  - On the other hand, the ends are often the most difficult parts to manufacture
  - It is common to **reduce the main field in the ends by adding spacers** - this makes the design a bit more complicated



Simple coil end with increased field in P  
[Schmuser,pg. 58]



Coil end with spacers to decrease  
the main field in the end  
[Schmuser,pg. 58]



# Magnet end design influences field quality

## ● Main features of the coil end design

+/- Magnetic: take care of field quality (especially if the magnet is short)

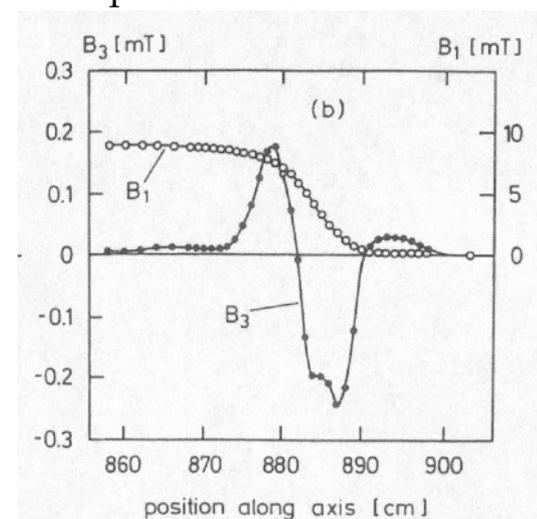
- In general a coil end will give a **non-negligible contribution to multipoles**
- Two possibilities
  - Leave it as it is and **compensate** the coil end **with the straight part** so that the multipoles integral over the magnet is optimal (cheap, simple)
  - Optimize the end spacer positions to set to zero the integral multipoles in each the head (more elegant, complicated)

## ● In the plot pseudo-multipoles are shown, extracted as Fourier coefficients

- The scaling with the reference radius is not valid
- They are not unique - if you start from radial or tangential expression,  $B_x$  or  $B_y$  you get different things
- They give an idea of the behavior of the field harmonics, and way to get a compensation

## ● The real 3d expansion can be written

(see A. Jain, USPAS 2006 in Phoenix: "Harmonic description of 2D fields", slide 4)



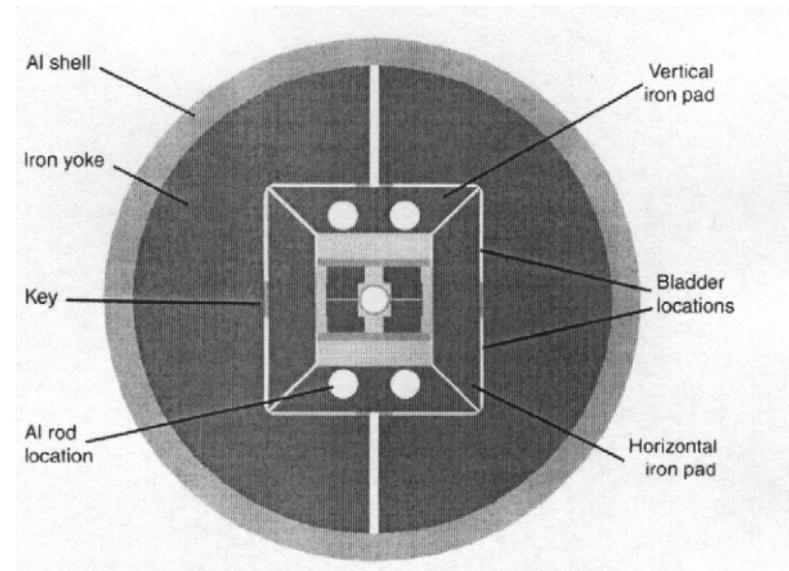
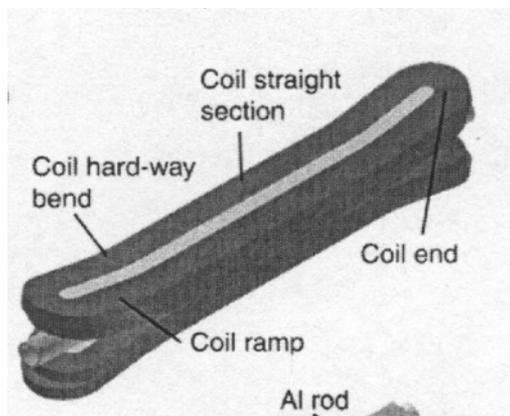
Main field and pseudo-multipoles in coil end optimized to have null integrated  $b_3$  [Schmuser, pg. 58]



# Lets look at other design concepts again...

## ● Block coil

- Cable is **not keystoneed**
- Cables are **perpendicular to the midplane**
- Ends are wound in the easy side, and slightly opened
- Internal structure to support the coil is needed
- Example: HD2 coil design



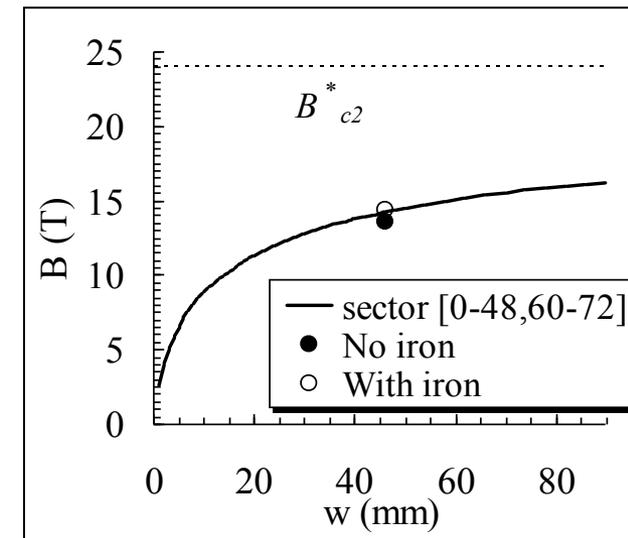
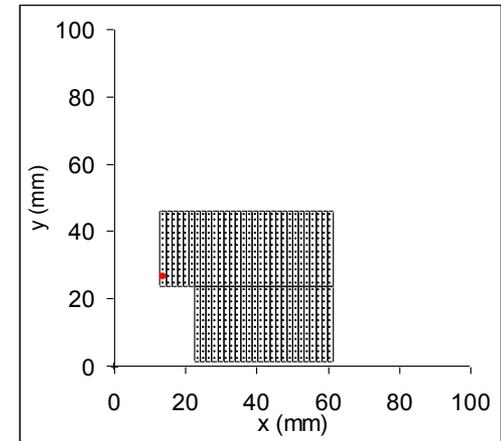
HD2 design: 3D sketch of the coil (left) and magnet cross section (right)  
[from P. Ferracin et al, MT19, IEEE Trans. Appl. Supercond. 16 378 (2006)]



# Flared-racetrack example

## ● Block coil – HD2

- Two layers, two blocks
- Enough parameters to have a good field quality
- Ratio peak field/central field not so bad:  
1.05 instead of 1.02 as for a  $\cos\theta$  with the same quantity of cable
- Ratio central field/current density is 12% less than a  $\cos(\theta)$  with the same quantity of cable
- Short sample field is **around 5% less** than what could be obtained by a  $\cos\theta$  with the same quantity of cable
- Reached 87% of short sample

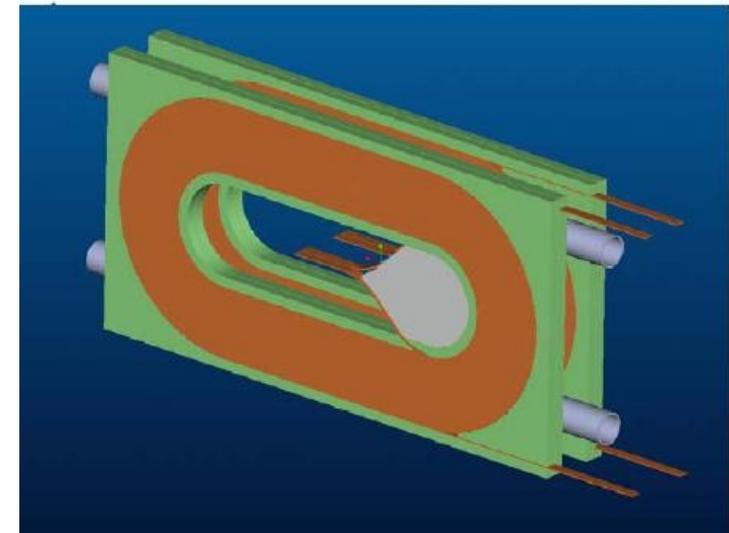
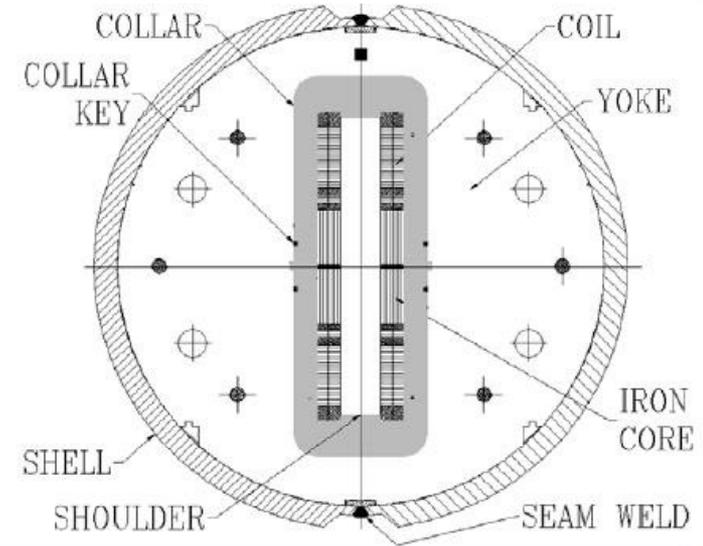




# Common coil example

## ● Common coil

- A two-aperture magnet
- Cable is not keystoneed
- Cables are parallel to the mid-plane
- Ends are wound in the easy side



### Common coil lay-out and cross-section

R. Gupta, *et al.*, "React and wind common coil dipole", talk at *Applied Superconductivity Conference 2006*, Seattle, WA, Aug. 27 - Sept. 1, 2006.

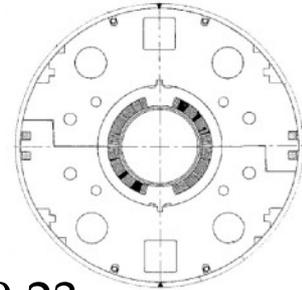
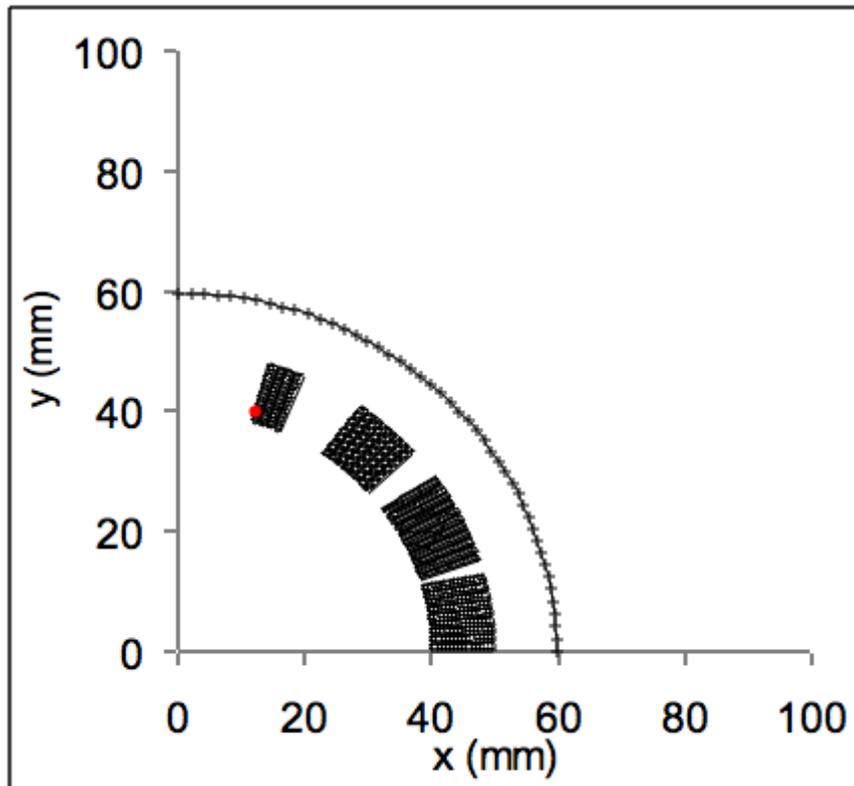


# Example dipole layouts - RHIC

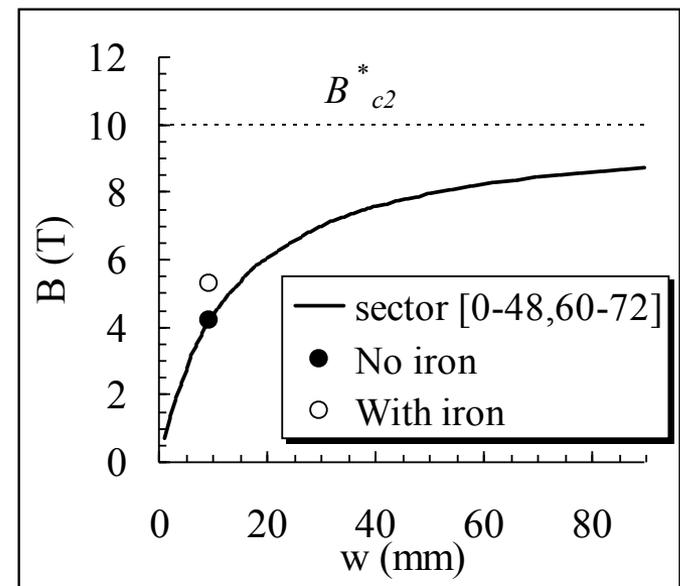


## RHIC MB

- Main dipole of the RHIC
- 296 magnets built in 04/94 – 01/96



- Nb-Ti, 4.2 K
- $w_{eq} \sim 9$  mm  $\kappa \sim 0.23$
- 1 layer, 4 blocks
- no grading





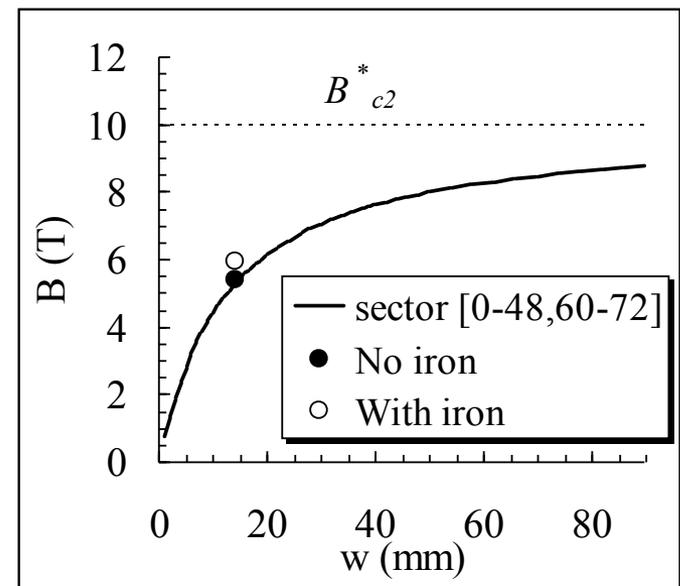
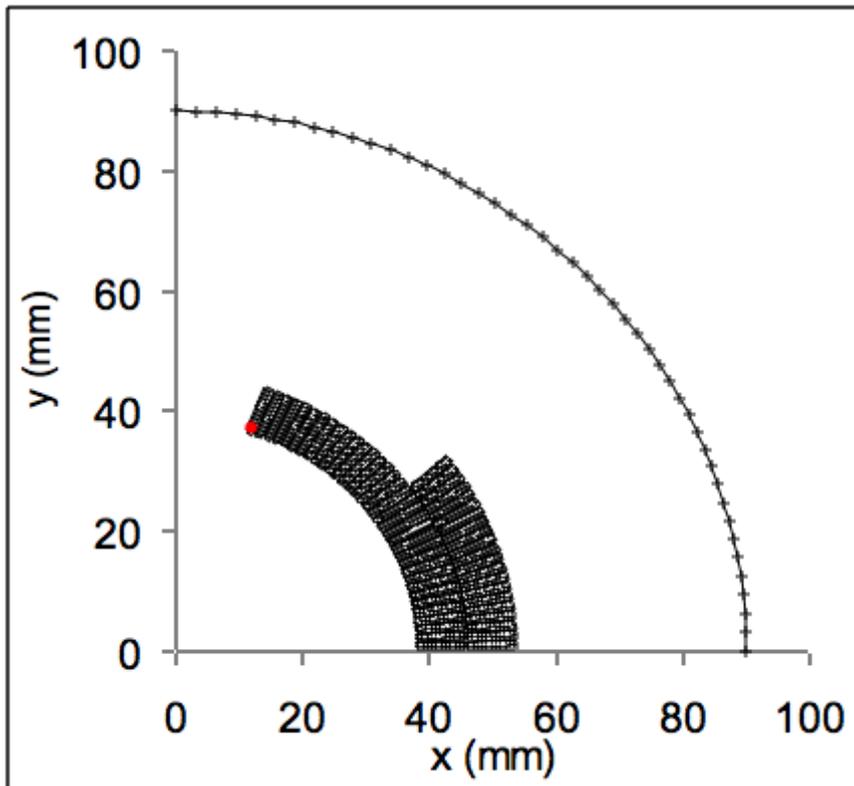
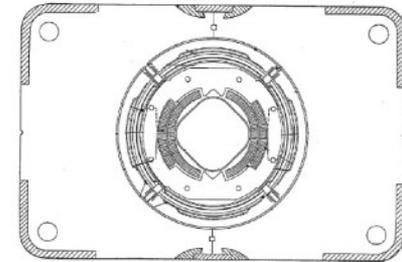
# Example dipole layouts - Tevatron



## Tevatron MB

- Main dipole of the Tevatron
- 774 magnets built in ~1980

- Nb-Ti, 4.2 K
- $w_{eq} \sim 14$  mm  $\kappa \sim 0.23$
- 2 layer, 2 blocks
- no grading



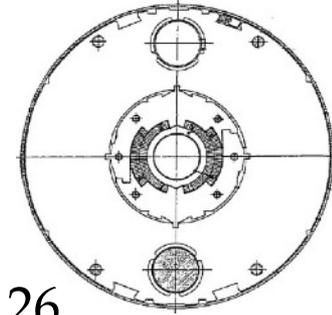
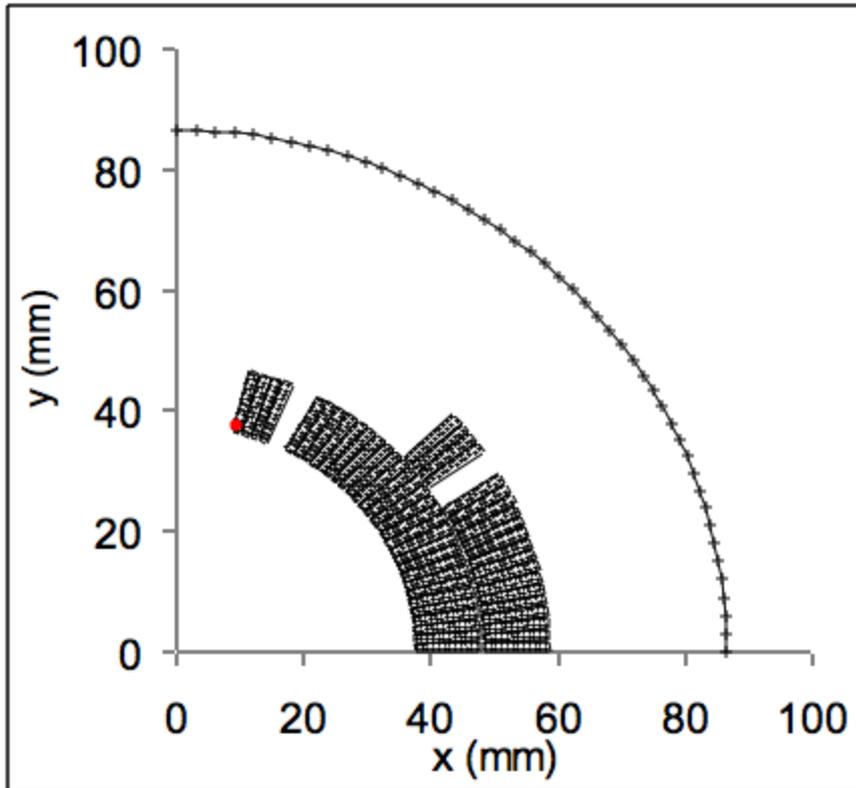


# Example of dipole layouts - HERA

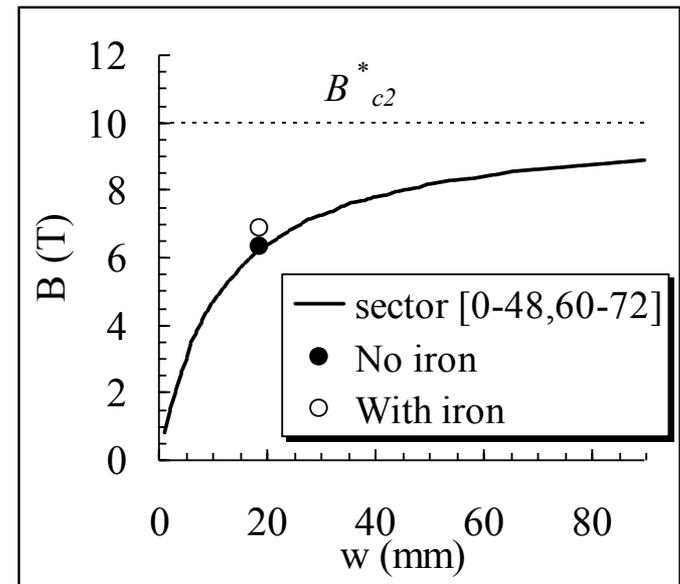


## HERA MB

- Main dipole of the HERA
- 416 magnets built in ~1985/87



- Nb-Ti, 4.2 K
- $w_{eq} \sim 19$  mm  $\kappa \sim 0.26$
- 2 layer, 4 blocks
- no grading

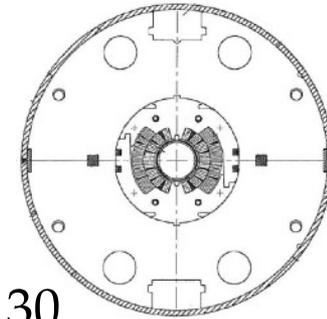
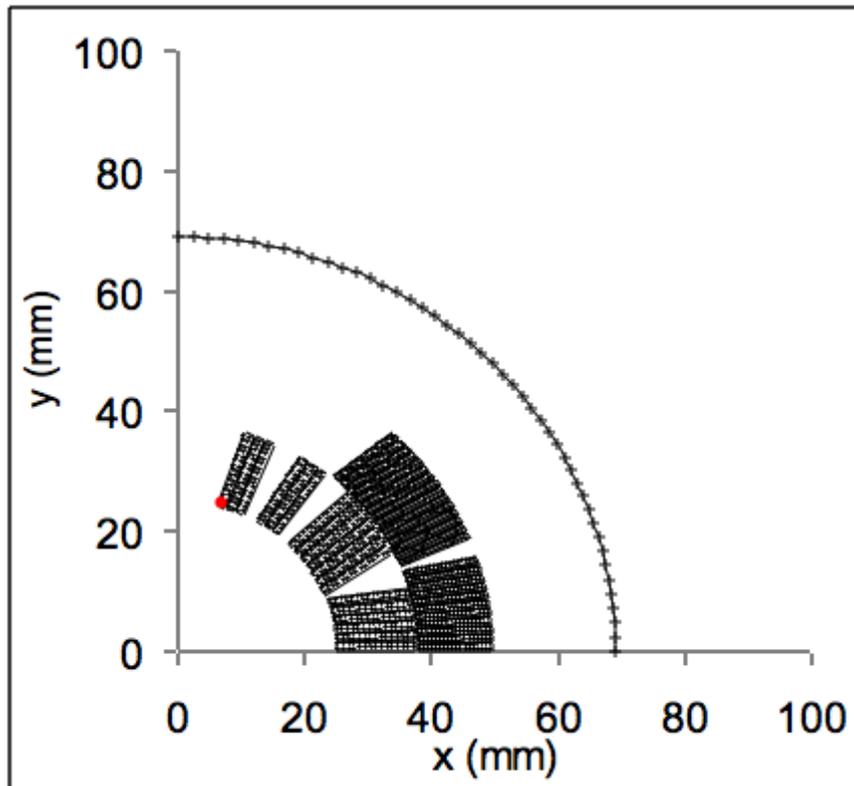




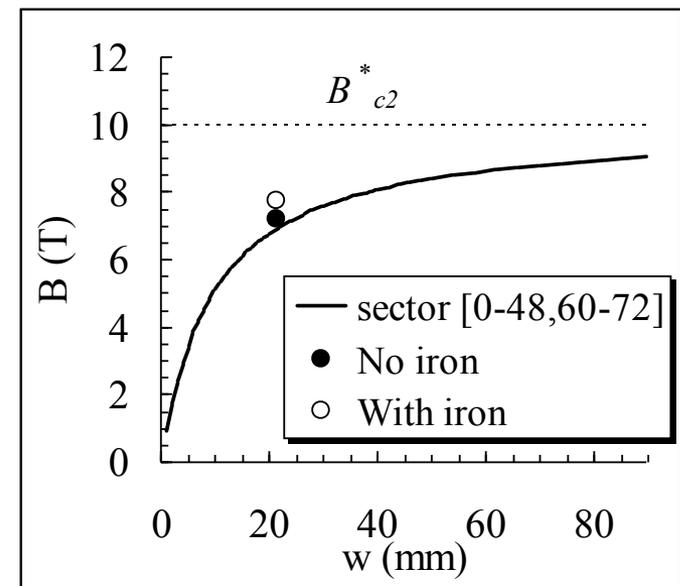
# Example dipole layouts - SSC

## SSC MB

- Main dipole of the ill-fated SSC
- 18 prototypes built in ~1990-5



- Nb-Ti, 4.2 K
- $w_{eq} \sim 22$  mm  $\kappa \sim 0.30$
- 4 layer, 6 blocks
- 30% grading

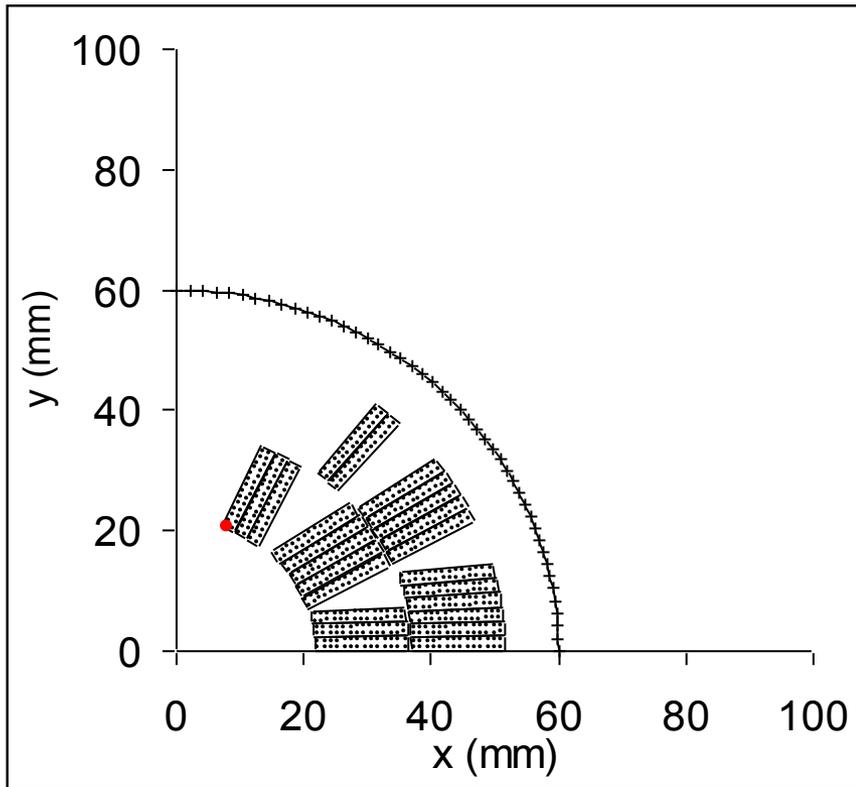




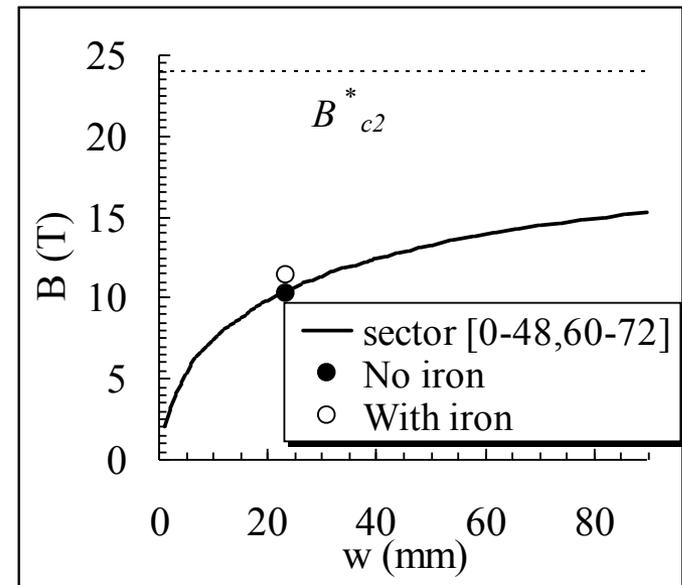
# Example dipole layouts - HFDA

## HFDA dipole

- Nb<sub>3</sub>Sn model built at FNAL
- 6 models built in 2000-2005



- Nb<sub>3</sub>Sn, 4.2 K
- $j_c \sim 2000$  to  $2500$  A/mm<sup>2</sup> at 12 T, 4.2 K (different strands)
- $w_{eq} \sim 23$  mm  $\kappa \sim 0.29$
- 2 layers, 6 blocks
- no grading

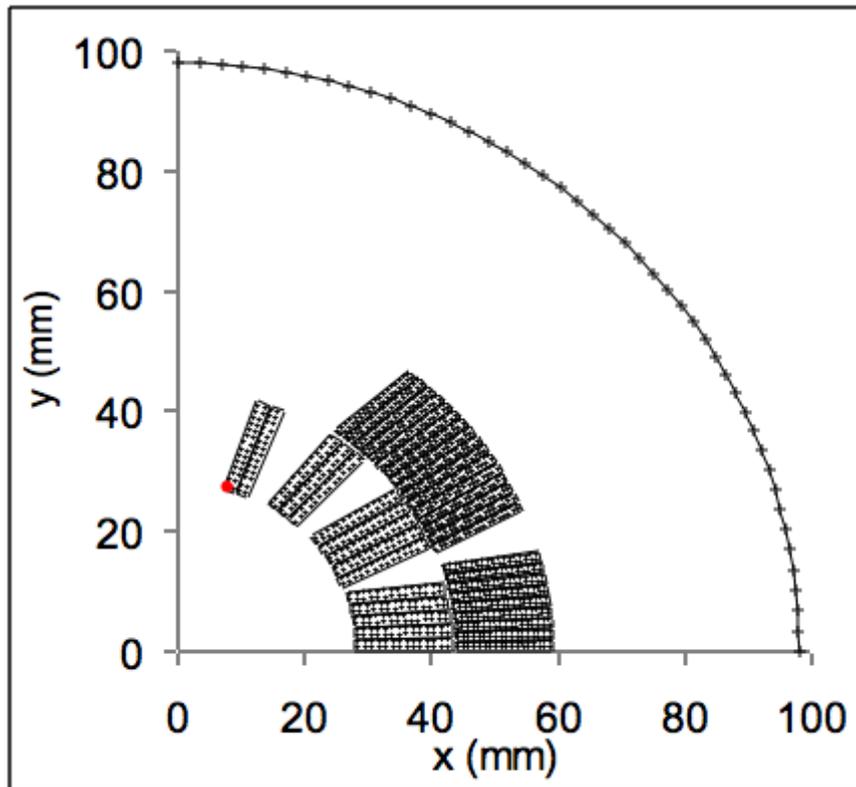




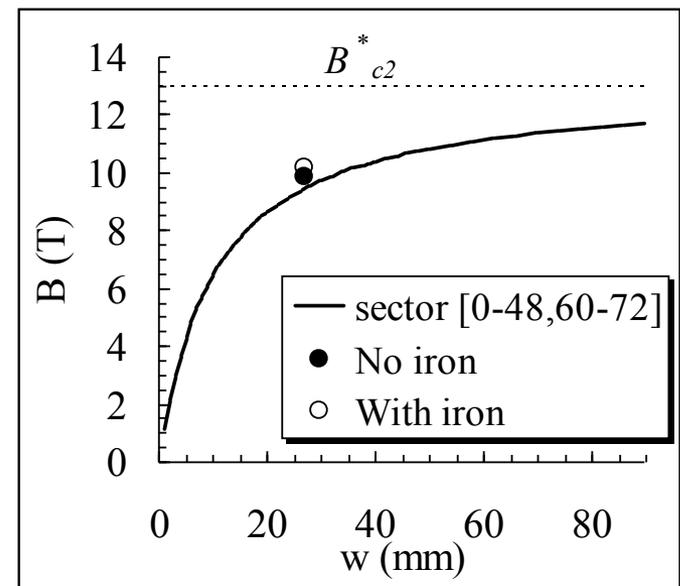
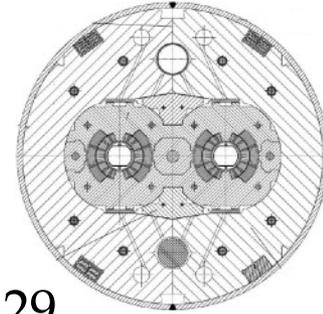
# Example dipole layouts - LHC MB

## LHC MB

- Main dipole of the LHC
- 1276 magnets built in 2001-06



- Nb-Ti, 1.9 K
- $w_{eq} \sim 27$  mm  $\kappa \sim 0.29$
- 2 layers, 6 blocks
- 23% grading



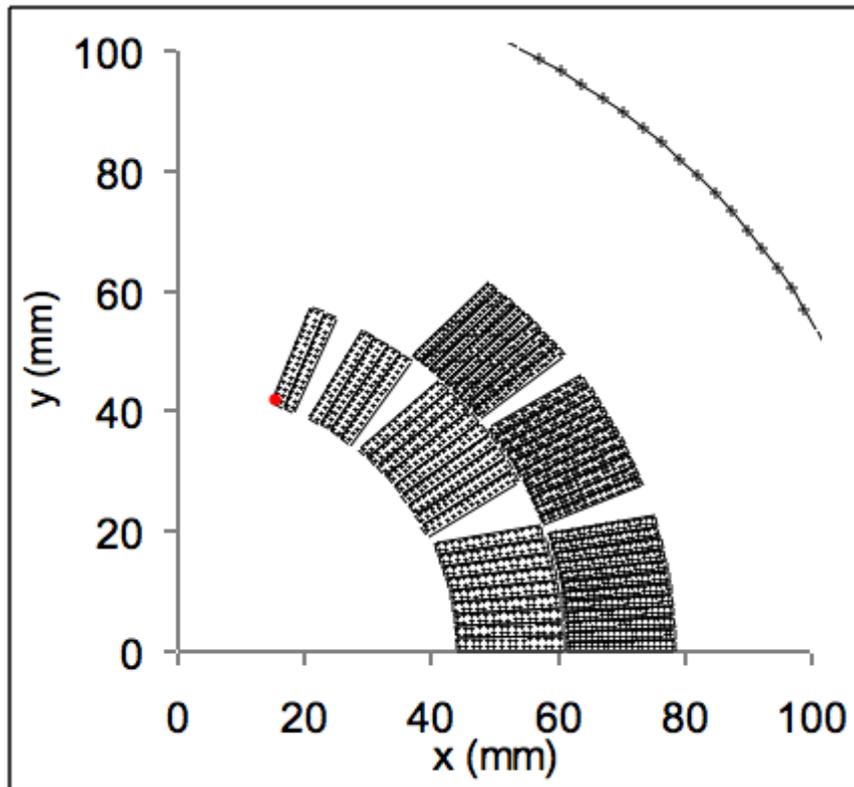


# Example dipole layouts - LHC MB - FRESCA

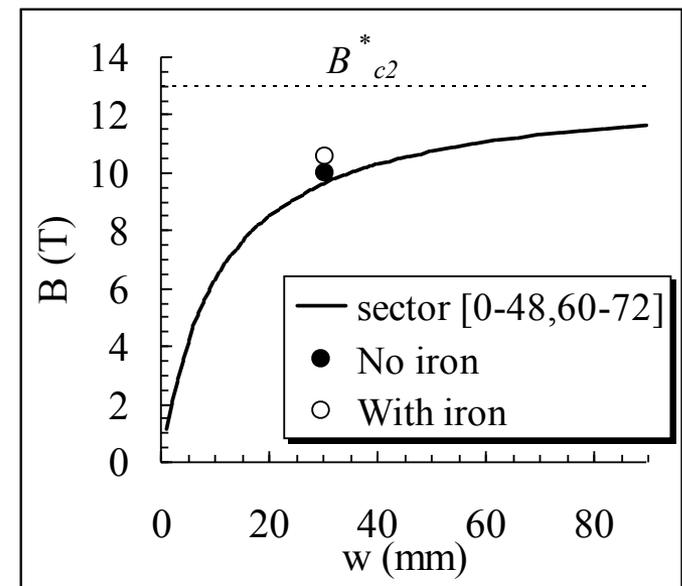


## FRESCA

- Dipole for cable test station at CERN
- 1 magnet built in 2001



- Nb-Ti, 1.9 K
- $w_{eq} \sim 30$  mm  $\kappa \sim 0.29$
- 2 layers, 7 blocks
- 24% grading



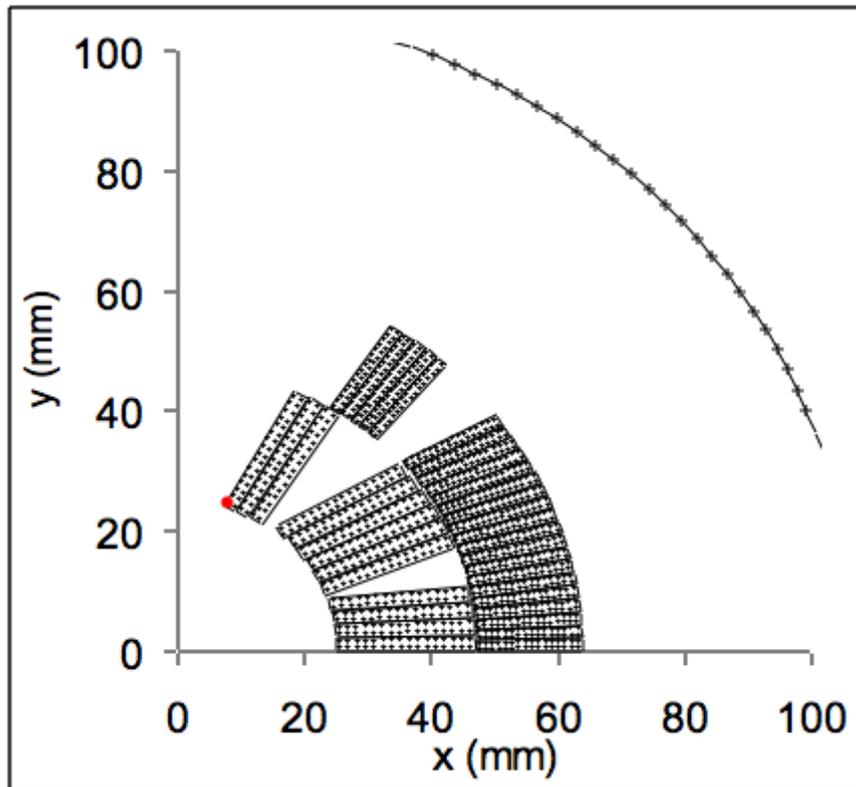


# Example dipole layouts - MSUT

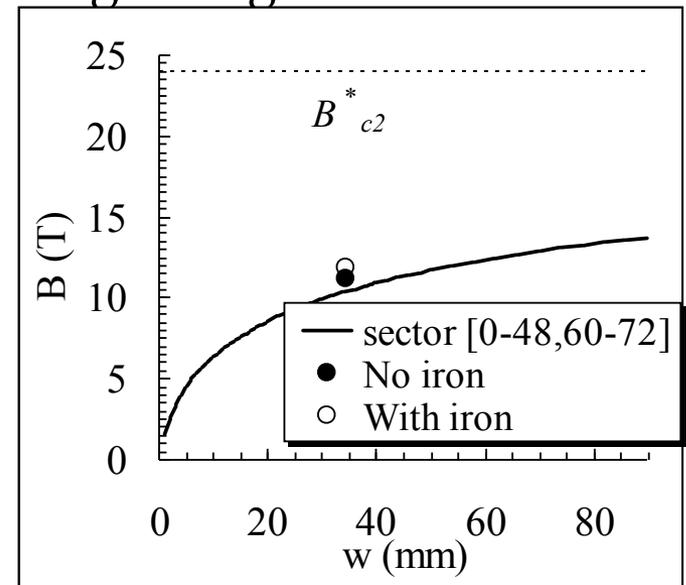


## MSUT dipole

- Nb<sub>3</sub>Sn model built at Twente U.
- 1 model built in 1995



- Nb<sub>3</sub>Sn, 4.2 K
- $j_c \sim 1100$  A/mm<sup>2</sup> at 12 T, 4.2 K
- $w_{eq} \sim 35$  mm  $\kappa \sim 0.33$
- 2 layers, 5 blocks
- 65% grading



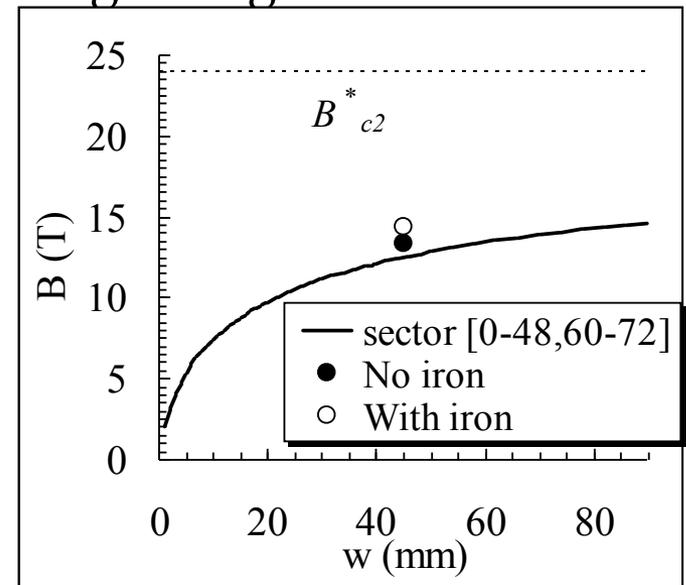
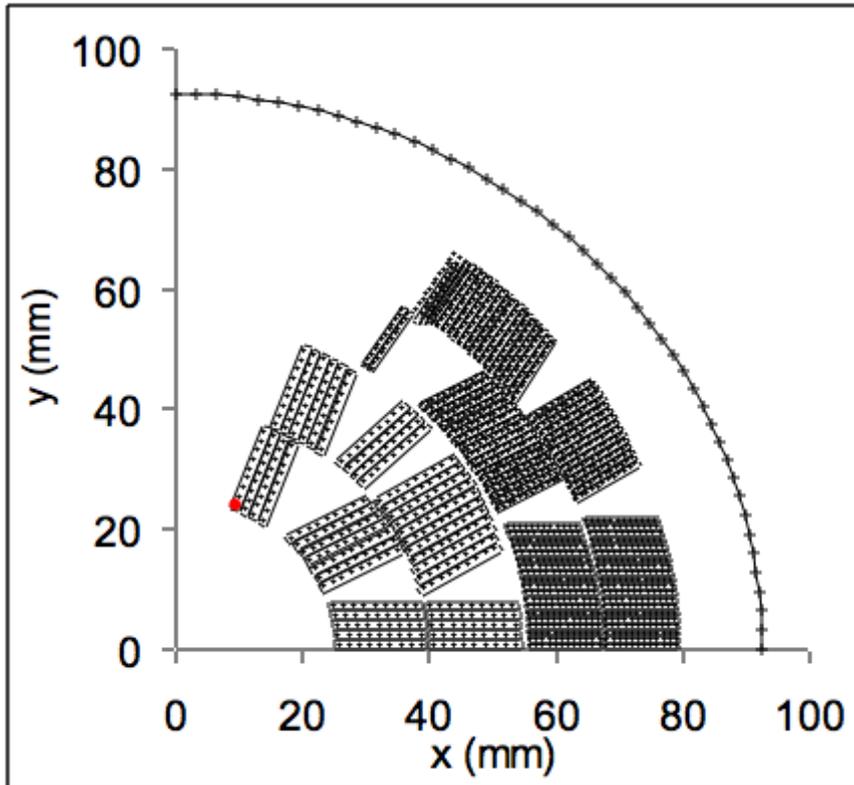


# Example dipole layouts - D20



## D20 dipole

- Nb<sub>3</sub>Sn model built at LBNL (USA)
- 1 model built in ~1998
- Nb<sub>3</sub>Sn, 4.2 K
- $j_c \sim 1100$  A/mm<sup>2</sup> at 12 T, 4.2 K
- $w_{eq} \sim 45$  mm  $\kappa \sim 0.48$
- 4 layers, 13 blocks
- 65% grading



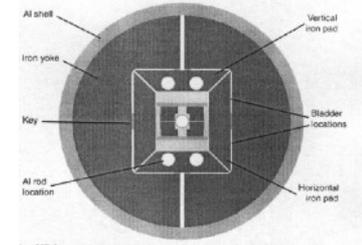
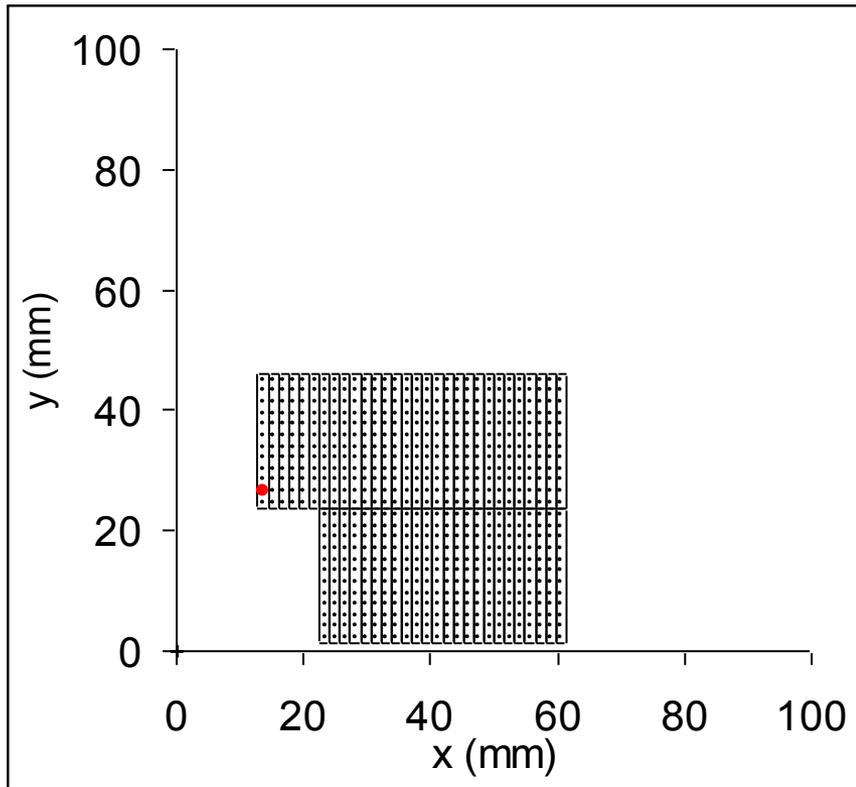


# Example dipole layouts - HD2

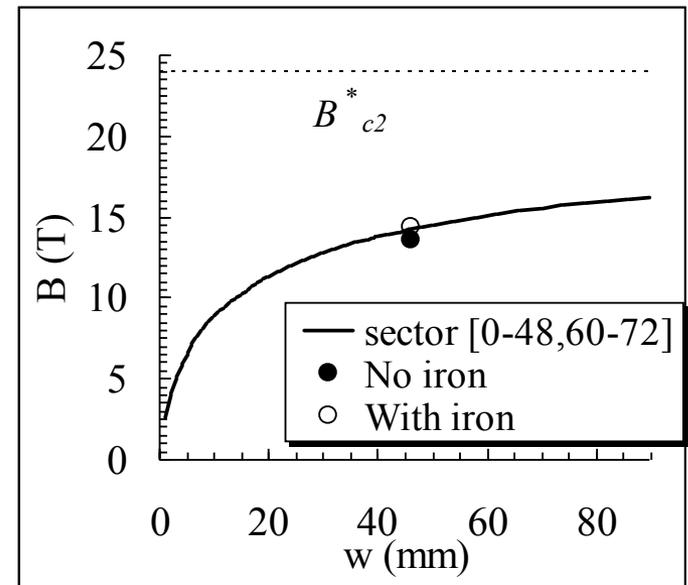


## HD2

- Nb<sub>3</sub>Sn model being built in LBNL
- 1 model to be built in 2008



- Nb<sub>3</sub>Sn, 4.2 K
- $j_c \sim 2500$  A/mm<sup>2</sup> at 12 T, 4.2 K
- $w_{eq} \sim 46$  mm  $\kappa \sim 0.35$
- 2 layers, racetrack, no grading



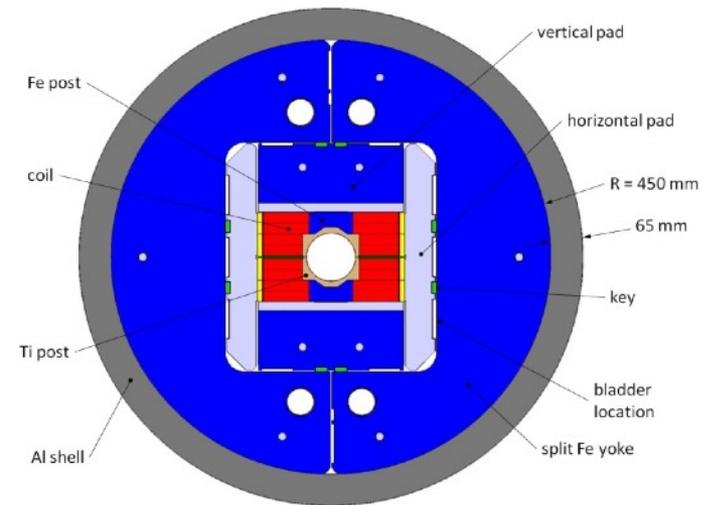
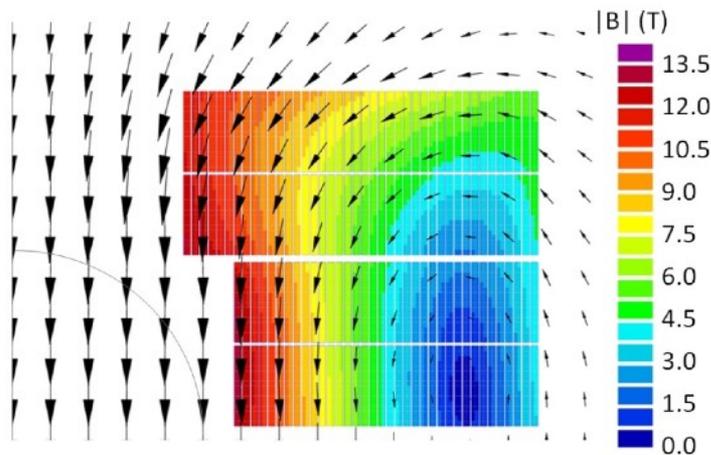


# Example dipole layouts - FRESCA-2



## Fresca2 dipole

- Nb<sub>3</sub>Sn test station founded by UE
- cable built in 2004-2006
- Operational field 13 T
- To be tested in 2014
- Nb<sub>3</sub>Sn, 4.2 K
- $j_c \sim 2500 \text{ A/mm}^2$  at 12 T, 4.2 K
- $w_{eq} \sim 80 \text{ mm}$      $\kappa \sim 0.31$
- Block coil 4 layers



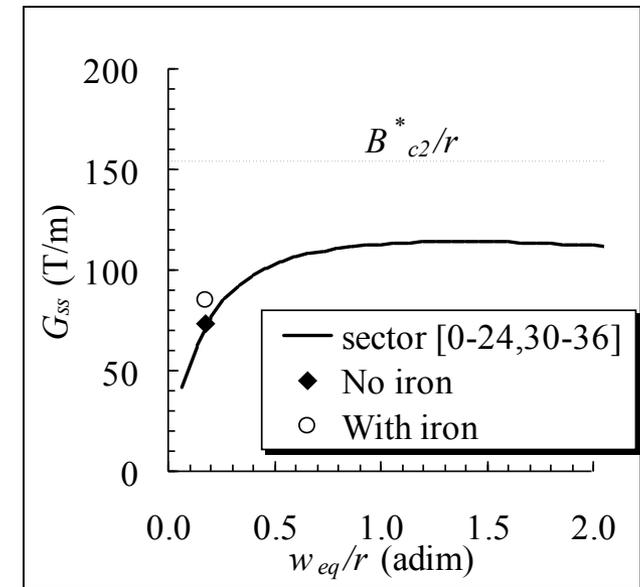
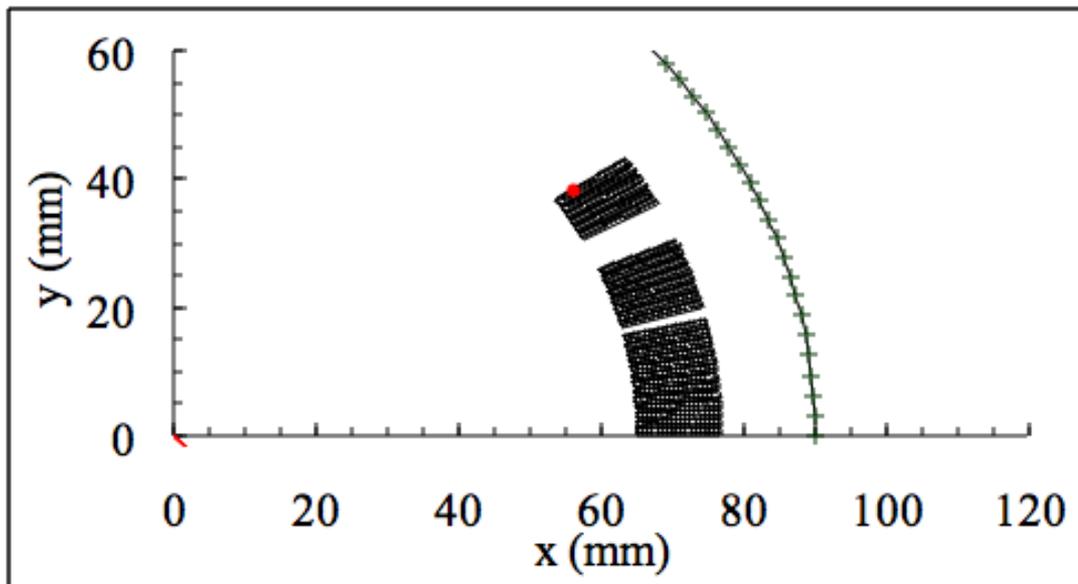


# Review of quadrupole layouts - RHIC



## RHIC MQX

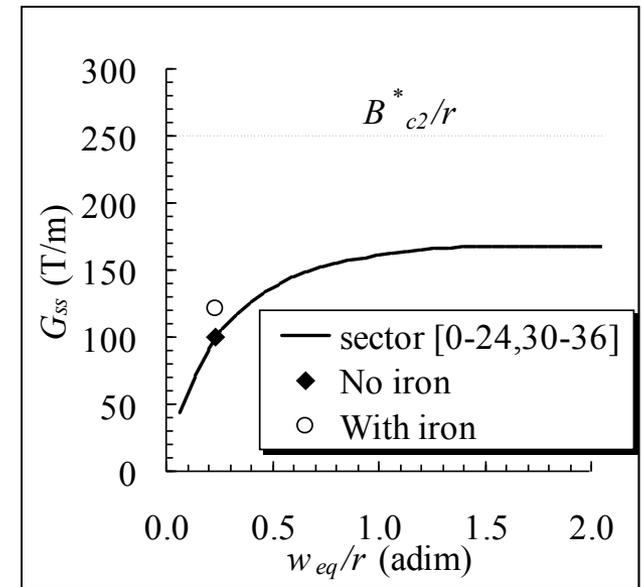
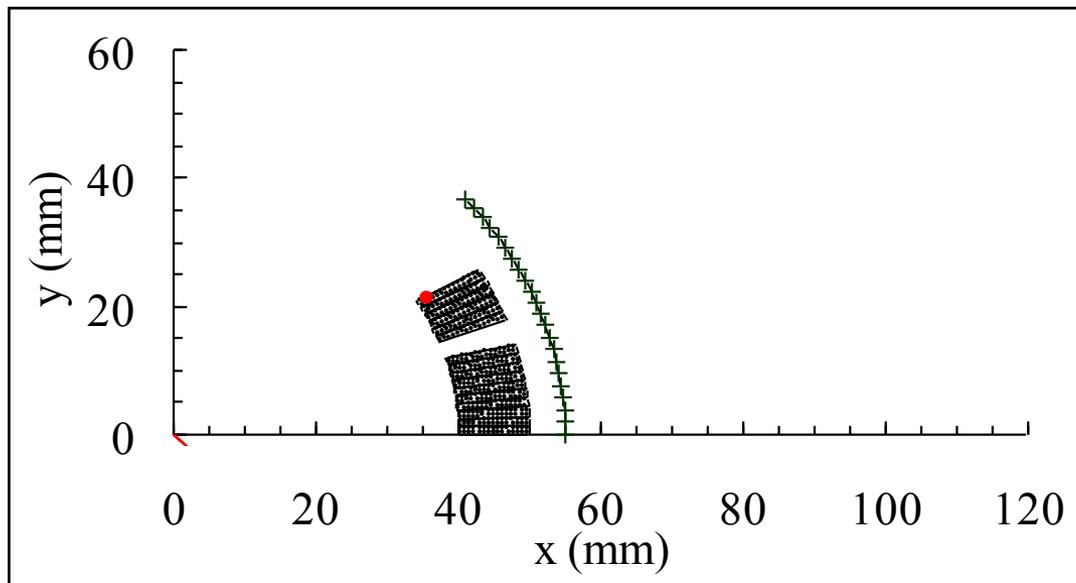
- Quadrupole in the IR regions of the RHIC
- 79 magnets built in July 1993/ December 1997
- Nb-Ti, 4.2 K
- $w/r \sim 0.18$      $\kappa \sim 0.27$
- 1 layer, 3 blocks, no grading





## RHIC MQ

- Main quadrupole of the RHIC
- 380 magnets built in June 1994 – October 1995
- Nb-Ti, 4.2 K
- $w/r \sim 0.25$      $\kappa \sim 0.23$
- 1 layer, 2 blocks, no grading



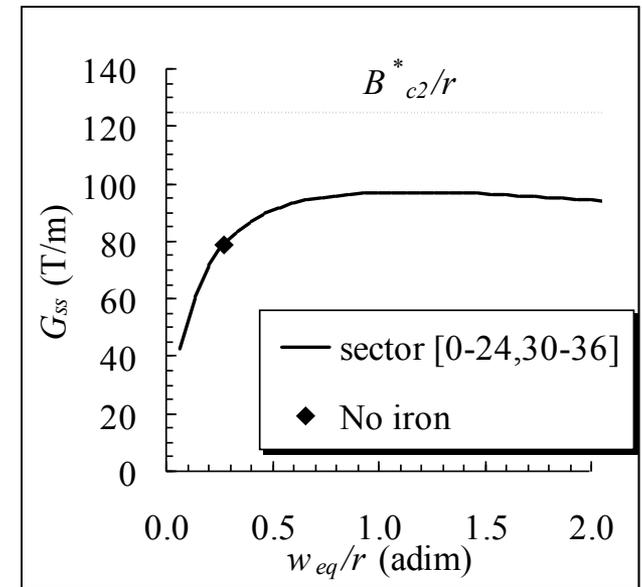
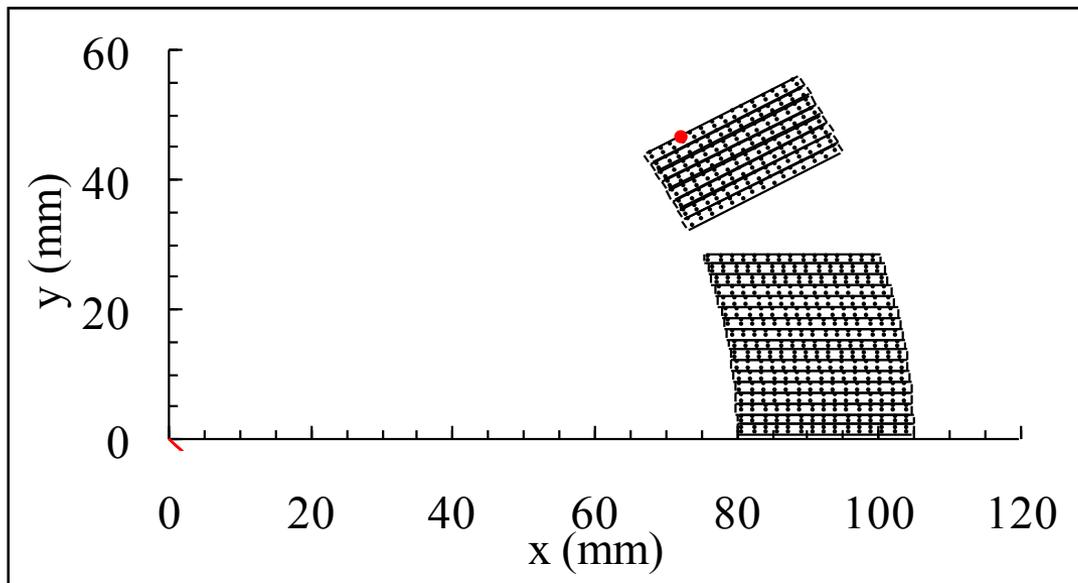


# Review of quadrupole layouts - LEP II



## LEP II MQC

- Interaction region quadrupole of the LEP II
- 8 magnets built in ~1991-3
- Nb-Ti, 4.2 K, no iron
- $w/r \sim 0.27$      $\kappa \sim 0.31$
- 1 layers, 2 blocks, no grading



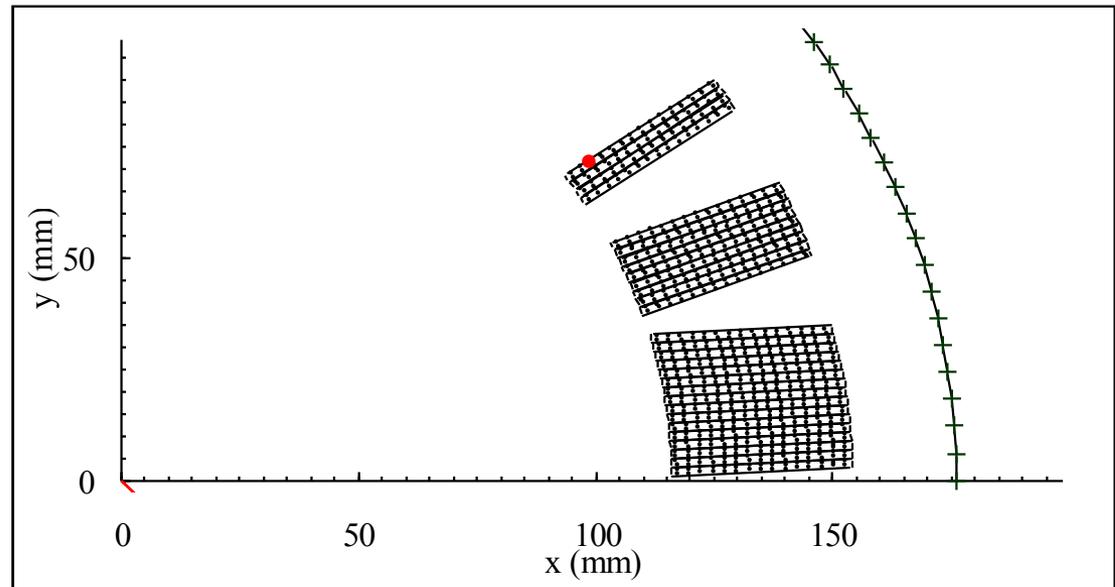
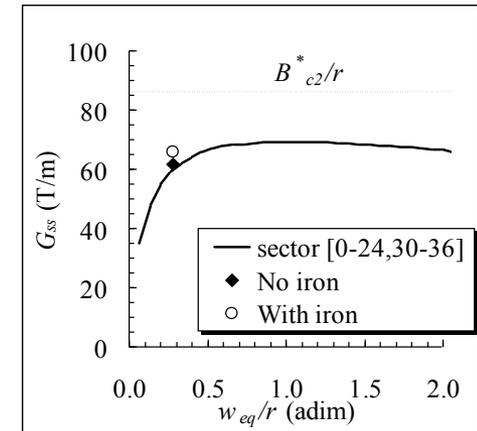


# Review of quadrupole layouts - ISR



## ISR MQX

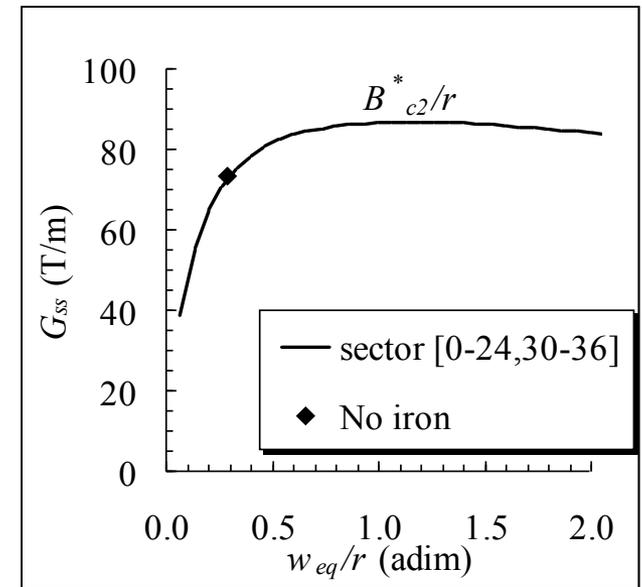
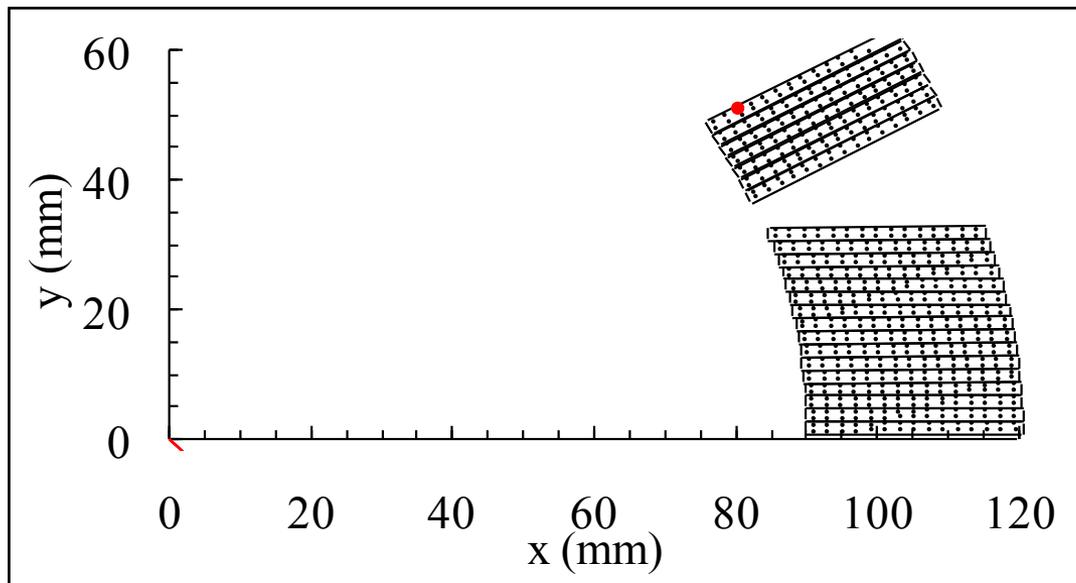
- IR region quadrupole of the ISR
- 8 magnets built in ~1977-79
- Nb-Ti, 4.2 K
- $w/r \sim 0.28$      $\kappa \sim 0.35$
- 1 layer, 3 blocks, no grading





## LEP I MQC

- Interaction region quadrupole of the LEP I
- 8 magnets built in ~1987-89
- Nb-Ti, 4.2 K, no iron
- $w/r \sim 0.29$      $\kappa \sim 0.33$
- 1 layers, 2 blocks, no grading



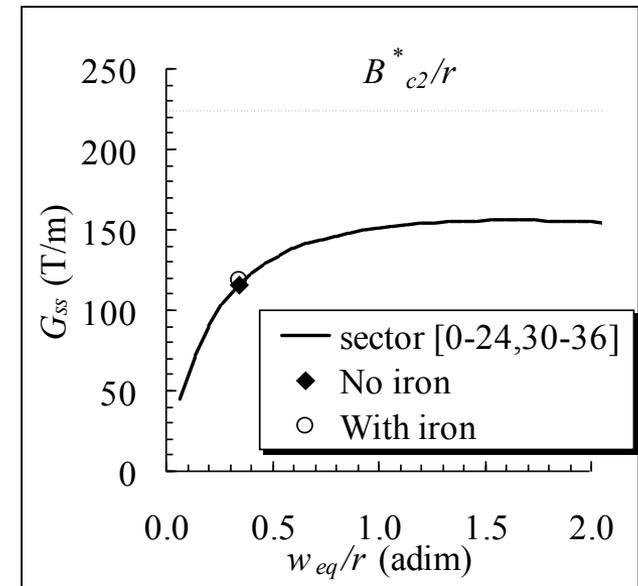
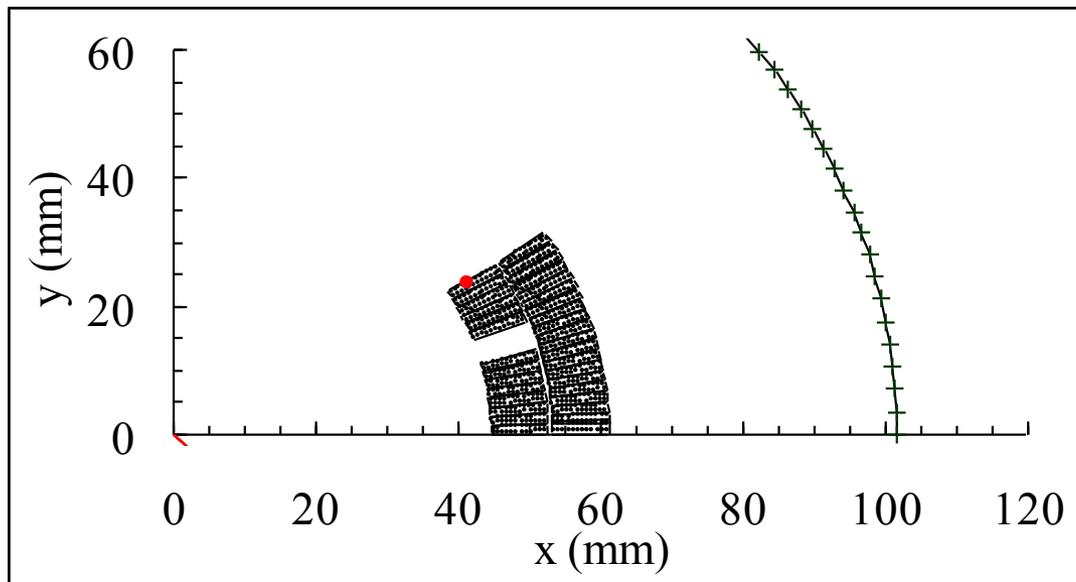


# Review of quadrupole layouts - Tevatron



## Tevatron MQ

- Main quadrupole of the Tevatron
- 216 magnets built in ~1980
- Nb-Ti, 4.2 K
- $w/r \sim 0.35$      $\kappa \sim 0.250$
- 2 layers, 3 blocks, no grading



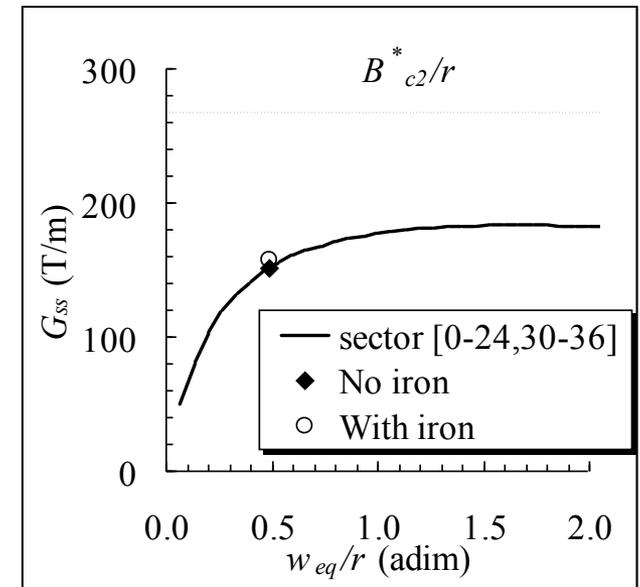
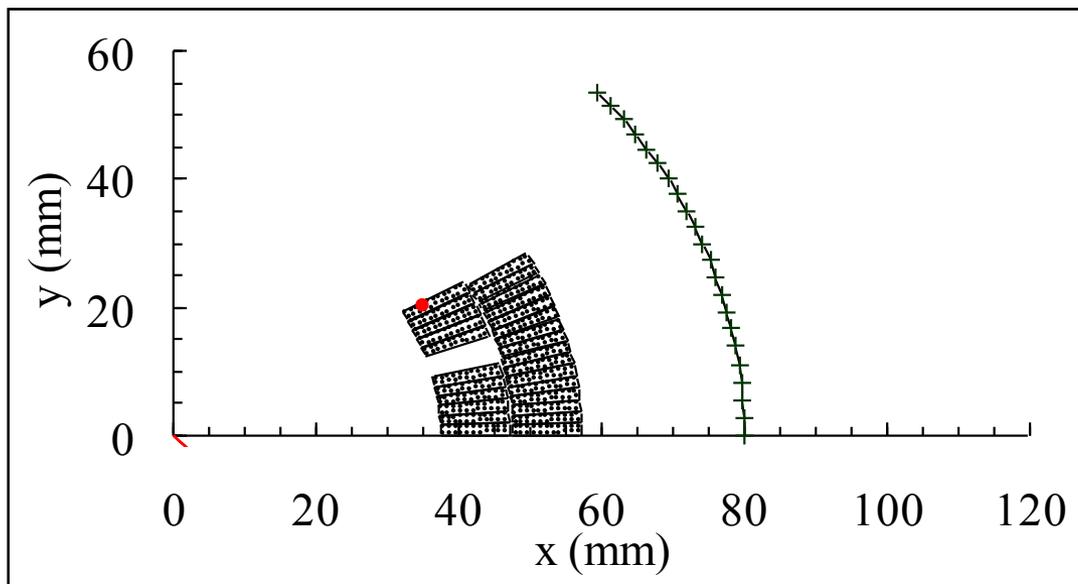


# Review of quadrupole layouts - HERA



## HERA MQ

- Main quadrupole of the HERA
- Nb-Ti, 1.9 K
- $w/r \sim 0.52$      $\kappa \sim 0.27$
- 2 layers, 3 blocks, grading 10%



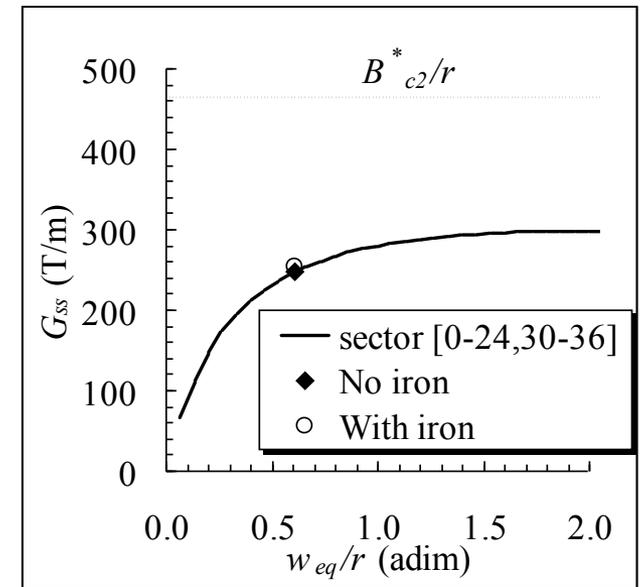
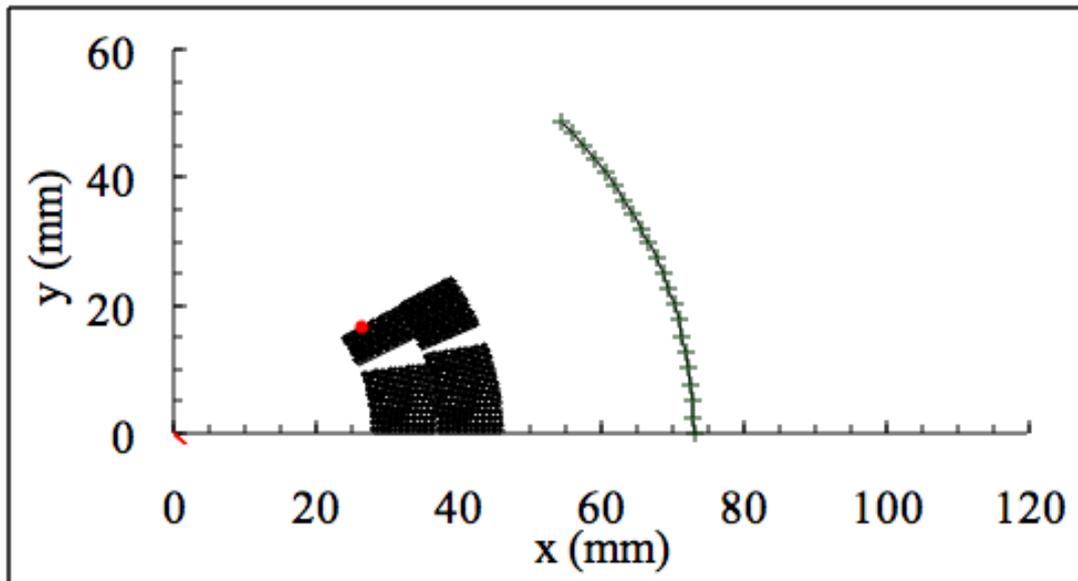


# Review of quadrupole layouts - LHC



## LHC MQM

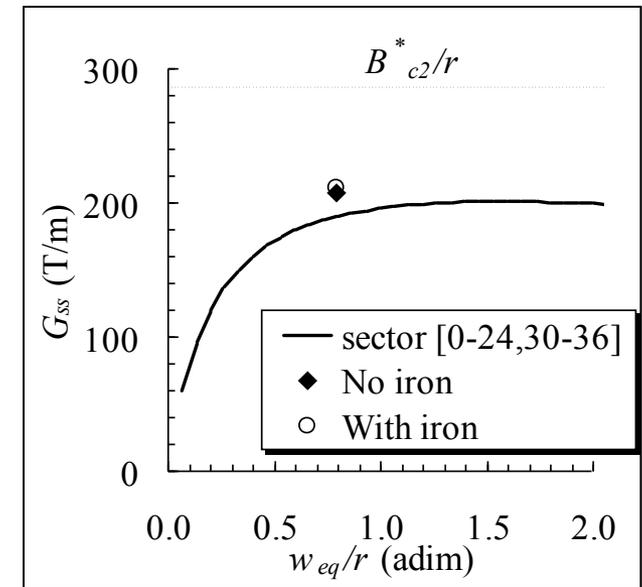
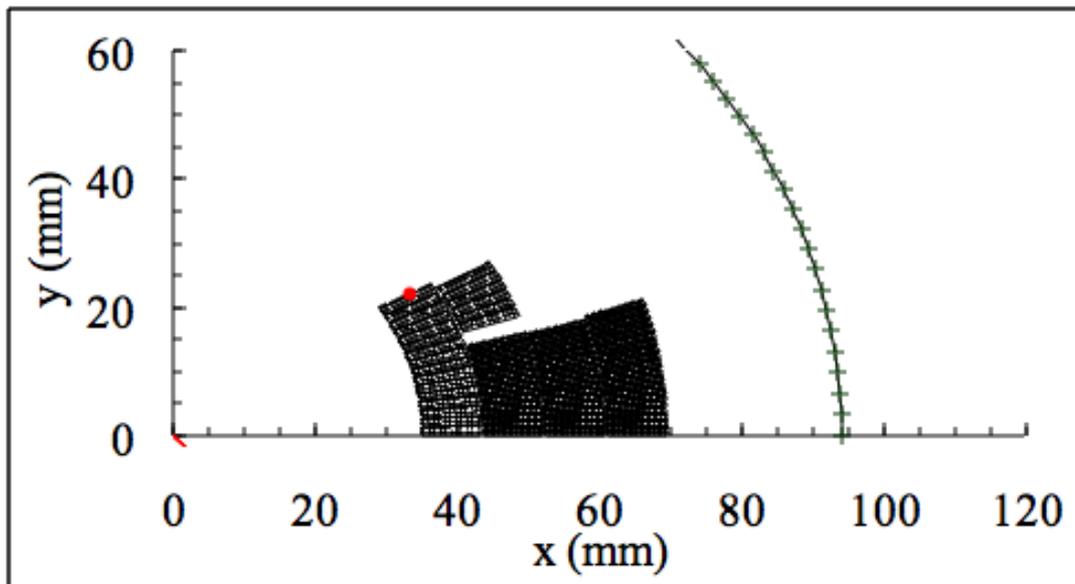
- Low- gradient quadrupole in the IR regions of the LHC
- 98 magnets built in 2001-2006
- Nb-Ti, 1.9 K (and 4.2 K)
- $w/r \sim 0.61$      $\kappa \sim 0.26$
- 2 layers, 4 blocks, no grading





## LHC MQY

- Large aperture quadrupole in the IR regions of the LHC
- 30 magnets built in 2001-2006
- Nb-Ti, 4.2 K
- $w/r \sim 0.79$      $\kappa \sim 0.34$
- 4 layers, 5 blocks, special grading 43%



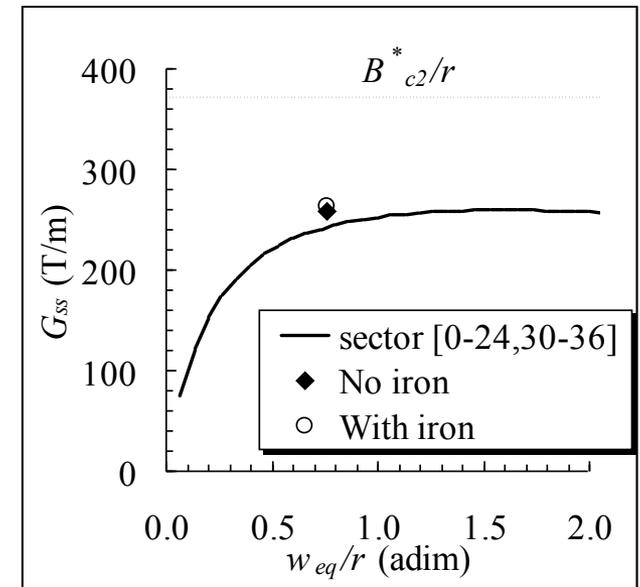
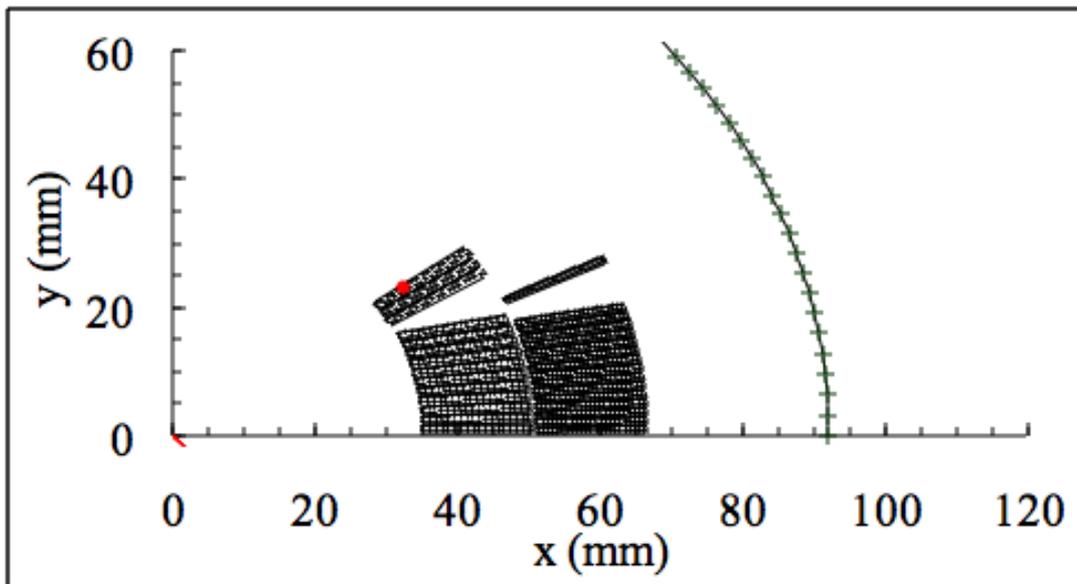
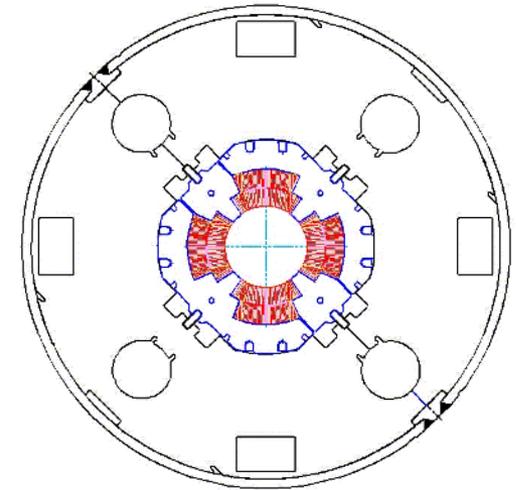


# Review of quadrupole layouts - LHC



## LHC MQXB

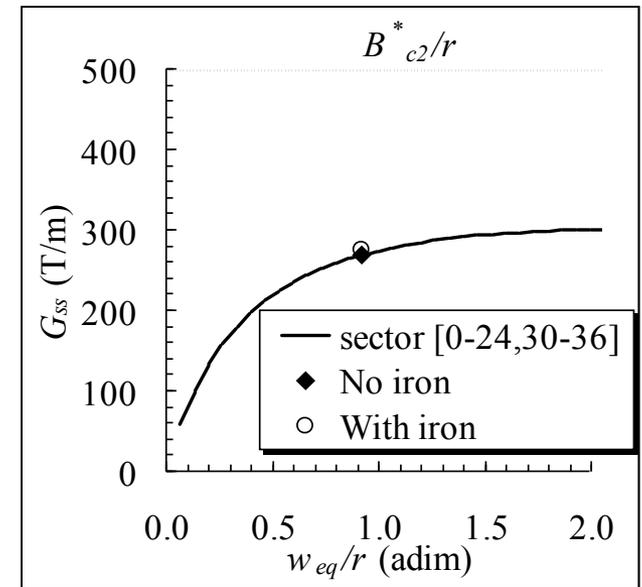
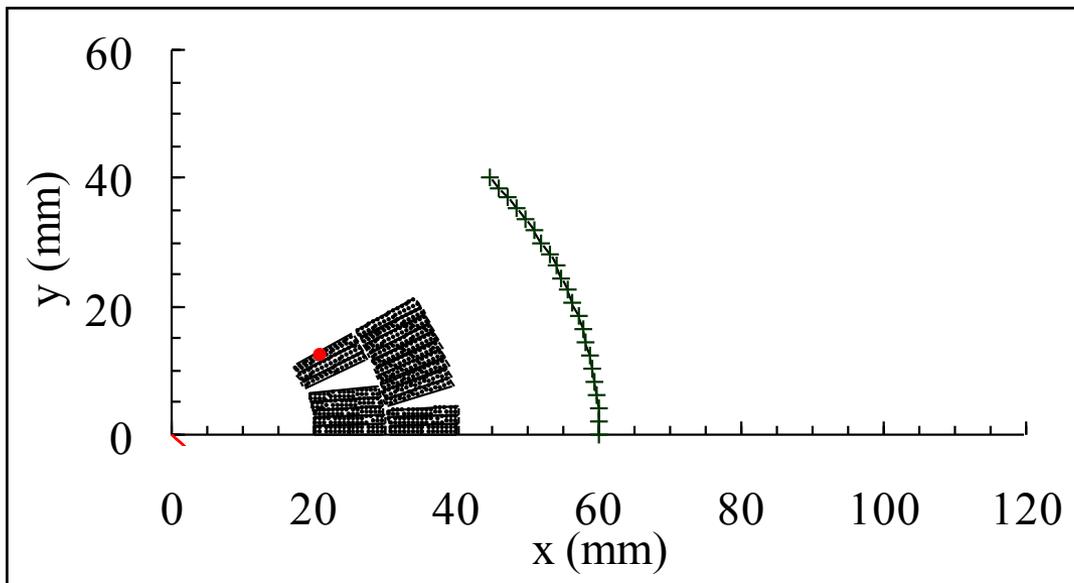
- Large aperture quadrupole in the LHC IR
- 8 magnets built in 2001-2006
- Nb-Ti, 1.9 K
- $w/r \sim 0.89$      $\kappa \sim 0.33$
- 2 layers, 4 blocks, grading 24%





## SSC MQ

- Main quadrupole of the ill-fated SSC
- Nb-Ti, 1.9 K
- $w/r \sim 0.92$      $\kappa \sim 0.27$
- 2 layers, 4 blocks, no grading

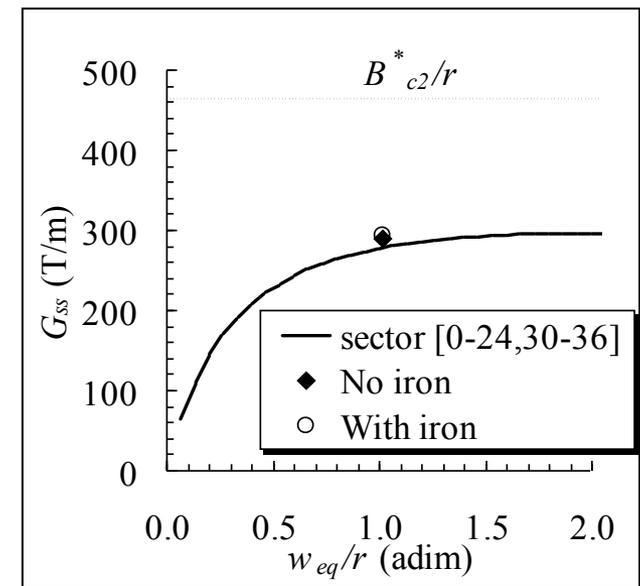
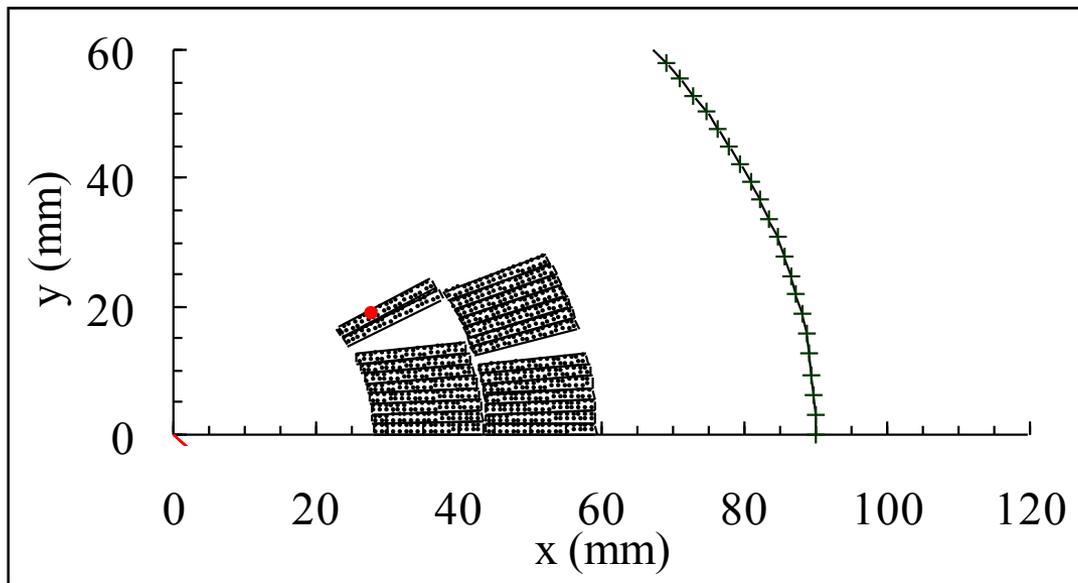
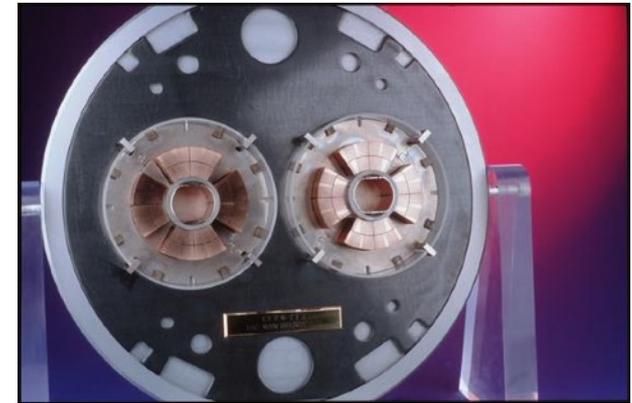




# Review of quadrupole layouts - LHC

## LHC MQ

- Main quadrupole of the LHC
- 400 magnets built in 2001-2006
- Nb-Ti, 1.9 K
- $w/r \sim 1.0$      $\kappa \sim 0.250$
- 2 layers, 4 blocks, no grading



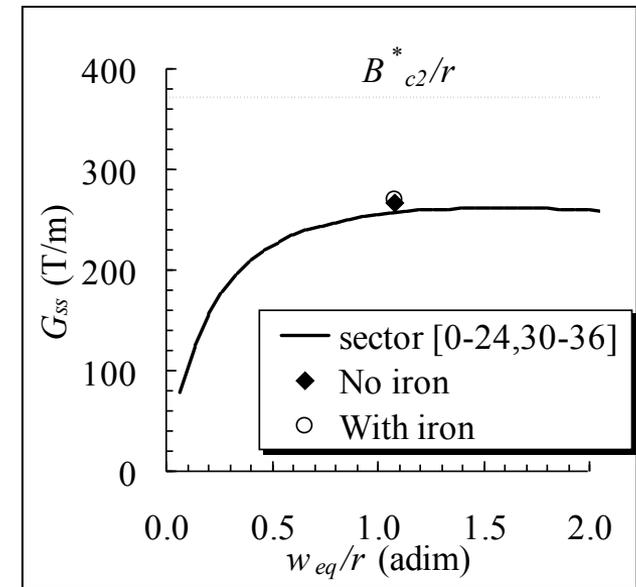
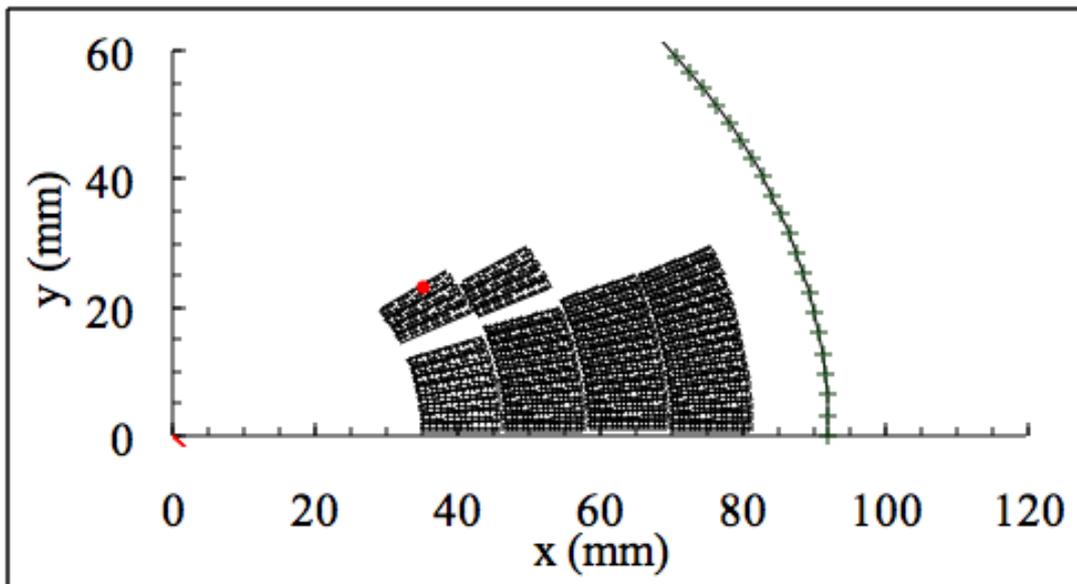
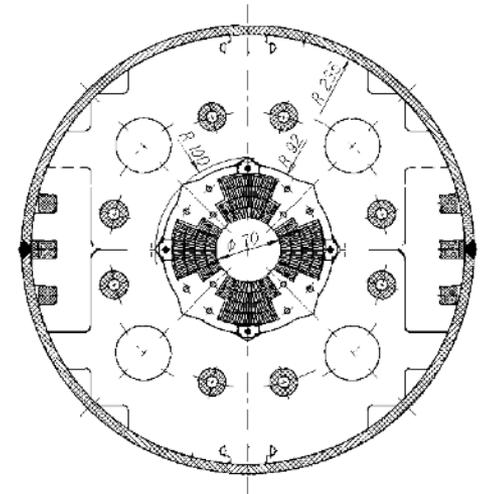


# Review of quadrupole layouts - LHC



## LHC MQXA

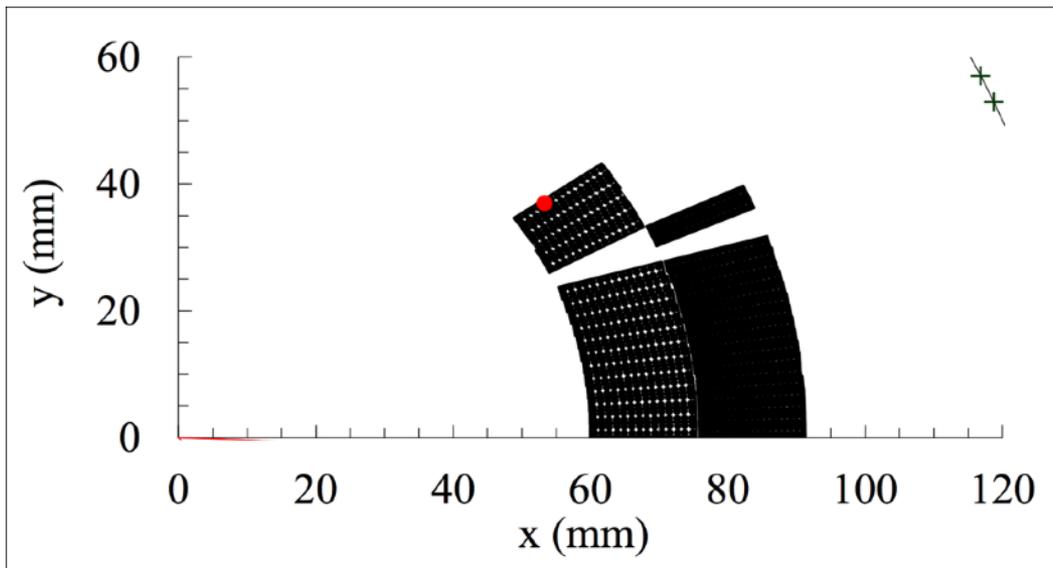
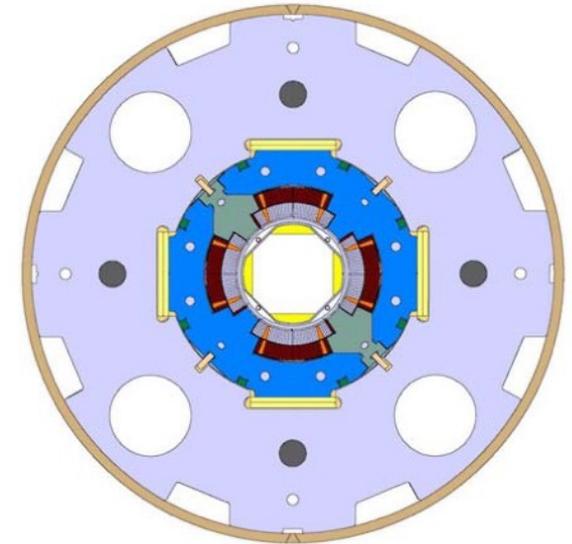
- Large aperture quadrupole in the LHC IR
- 18 magnets built in 2001-2006
- Nb-Ti, 1.9 K
- $w/r \sim 1.08$      $\kappa \sim 0.34$
- 4 layers, 6 blocks, special grading 10%





## LHC MQXC

- Nb-Ti option for the LHC upgrade
- LHC dipole cable, graded coil
- 1-m-long model built in 2011-2 to be tested in 2012
- $w/r \sim 0.5$     $\kappa \sim 0.33$    2 layers, 4 blocks

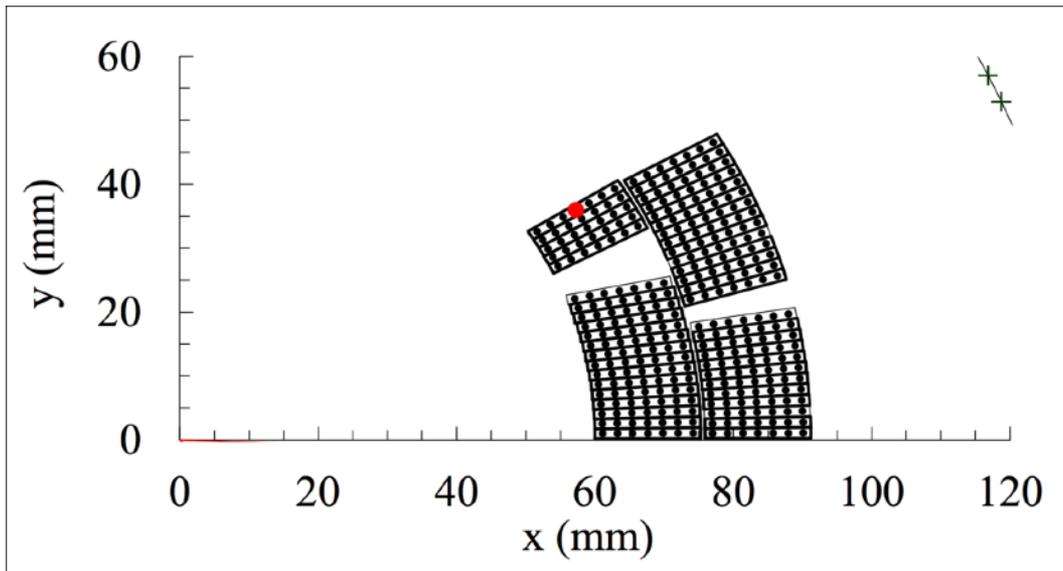




# Review of quadrupole layouts - LARP

## LARP HQ

- 120 mm aperture  $\text{Nb}_3\text{Sn}$  option for the LHC upgrade (IR triplet)
- 1-m-long model tested in 2011, more to come plus a 3.4-m-long
- $w/r \sim 0.5$   $\kappa \sim 0.33$  2 layers, 4 blocks





# CONCLUSIONS

- **Grading** the current density in the layers can give a larger performance for the same amount of conductor
  - 3-5% more in dipoles, 5-10% more in quadrupoles
- The **iron** has several impacts
  - Useful for **shielding**, can considerably increase the field for a given current – the impact on the performance is **small but not negligible**
  - Drawbacks: **saturation**, inducing field harmonics at high field – can be cured by shaping or drilling holes in the right place
- Coil ends – the design must aim at **reducing the peak field**
- **Other lay-outs**: pro and cons
- We shown a gallery of dipole and quadrupole magnetic designs used in the past 30 years



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- P. Schmuser, Ch. 4
- Classes given by R. Gupta at USPAS 2006, Unit 5
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- C. Vollinger, CERN 99-01 (1999) 93-109

## ● Grading

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- L. Rossi, E. Todesco, [Electromagnetic design of superconducting quadrupoles](#) *Phys. Rev. ST Accel. Beams* **9** (2006) 102401.

## ● Coil ends

- S. Russenschuck, CERN 99-01 (1999) 192-199
- G. Sabbi, CERN 99-01 (1999) 110-120

## ● Other designs

- Classes given by R. Gupta at USPAS 2006, Unit 10
- R. Gupta, *et al.*, "React and wind common coil dipole", talk at *Applied Superconductivity Conference 2006*, Seattle, WA, Aug. 27 - Sept. 1, 2006
- P. Ferracin et al, MT19, *IEEE Trans. Appl. Supercond.* **16** 378 (2006)
- Work by G. Ambrosio, S. Zlobin on common coil magnets at FNAL



# REFERENCES



● Plus...

- A whole series of papers about each magnet that has been presented



# ACKNOWLEDGEMENTS



- L. Rossi for discussions on magnet design
- F. Borgnolutti
- B. Auchmann, L. Bottura, A. Devred, V. Kashikin, T. Nakamoto, S. Russenschuck, T. Taylor, A. Den Ouden, A. McInturff, P. Ferracin, S. Zlobin, for kindly providing magnet designs
- P. Ferracin, S. Caspi for discussing magnet design and grading
- A. Jain for discussing the validity of field expansion in the ends