

# Muon capture and transport line

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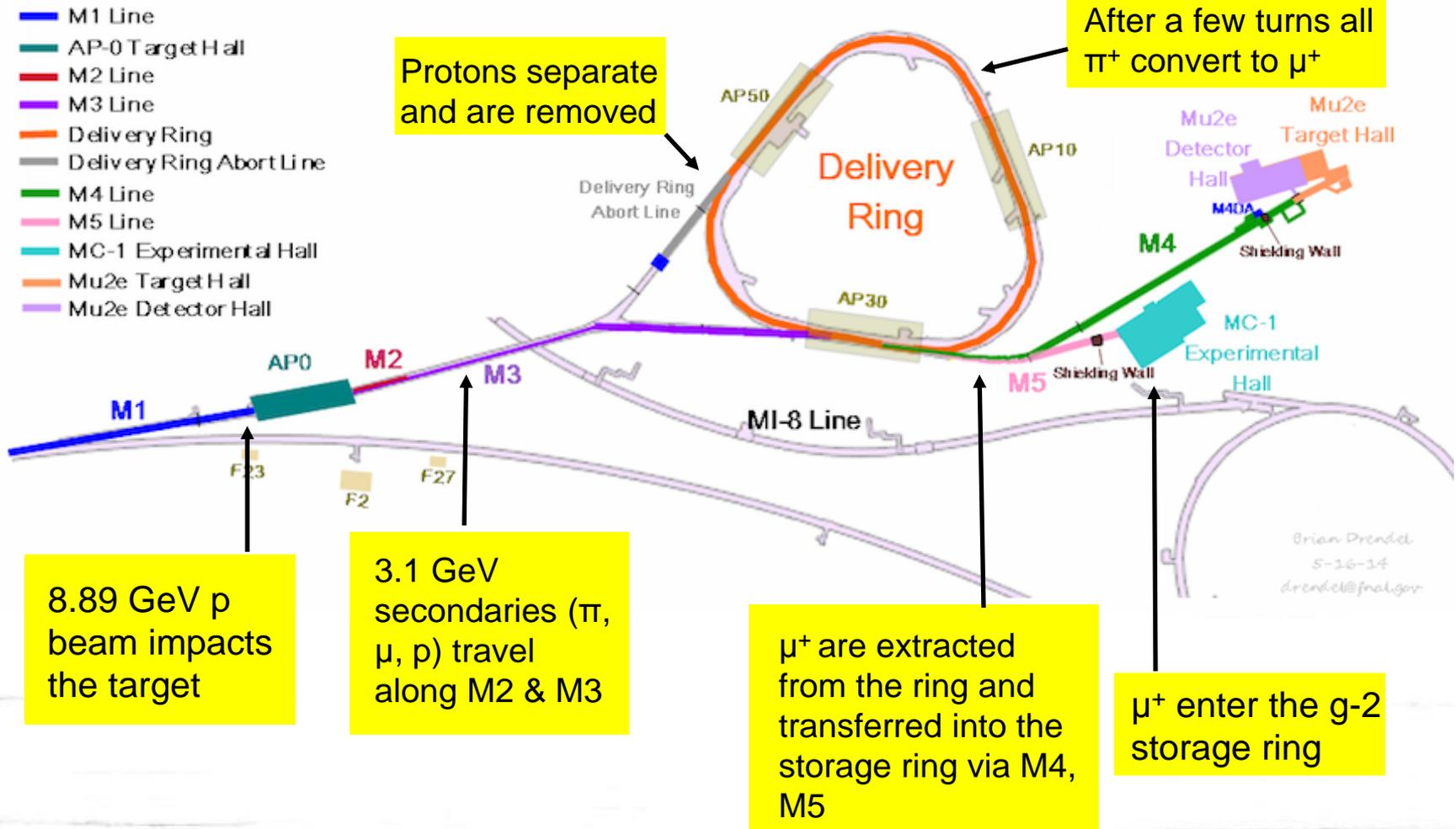
Fermi National Accelerator Laboratory

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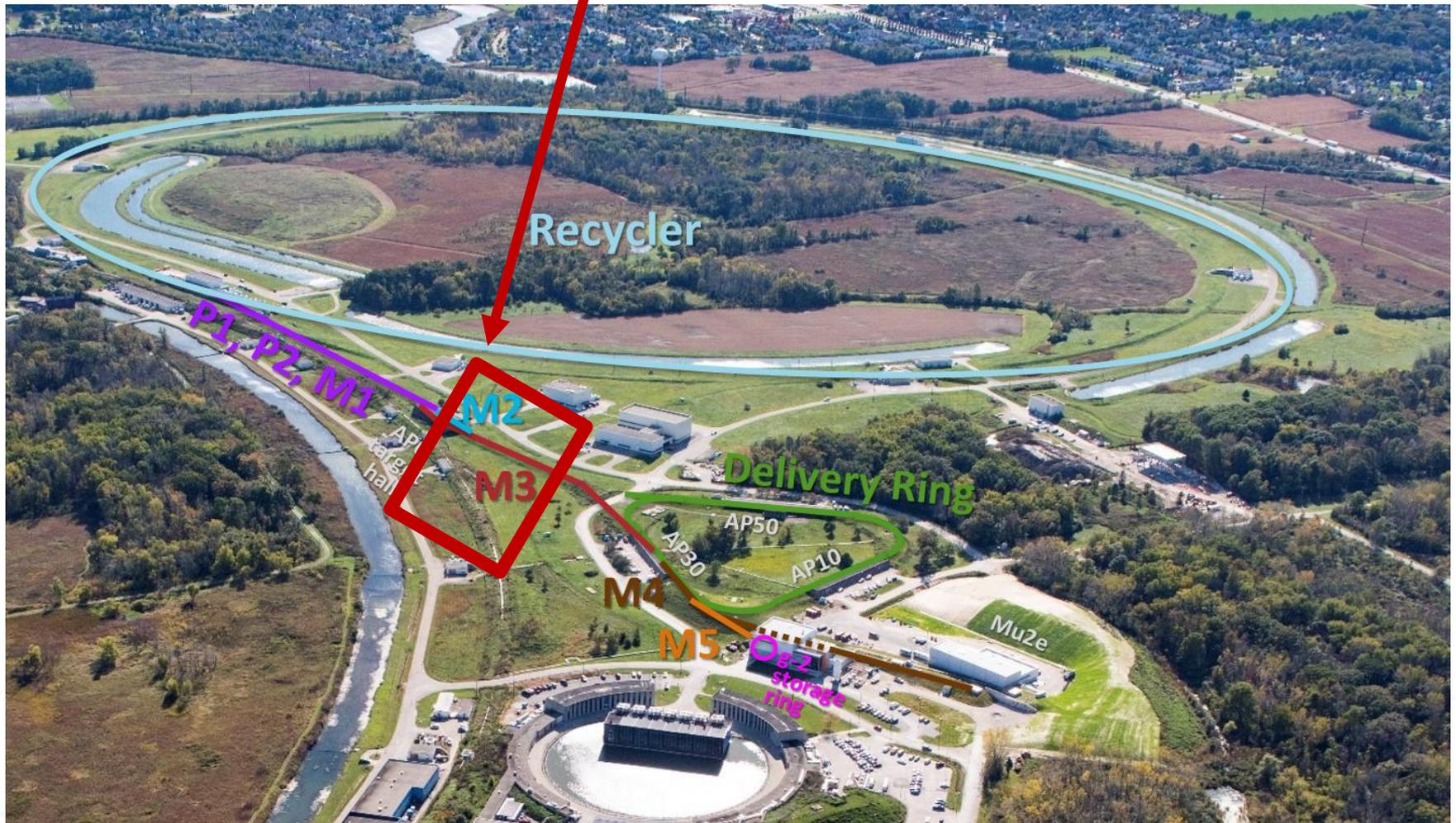
# Outline

- Muon and pion capture
- Lattice and optics design
- Expected performance
- Polarization

# Muon Campus overview

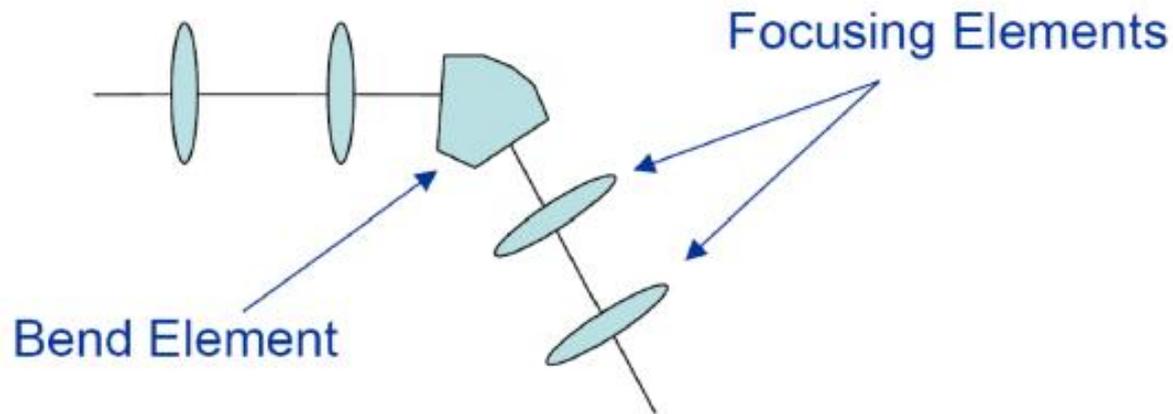


# Muon capture and transport (M2-M3)



# Muon capture & transport line optics

- The capture and transport of secondary beam is done with magnets
- Mainly two types of magnets: bending magnets (dipoles) and focusing magnets (quadrupoles)



# Dipole magnets

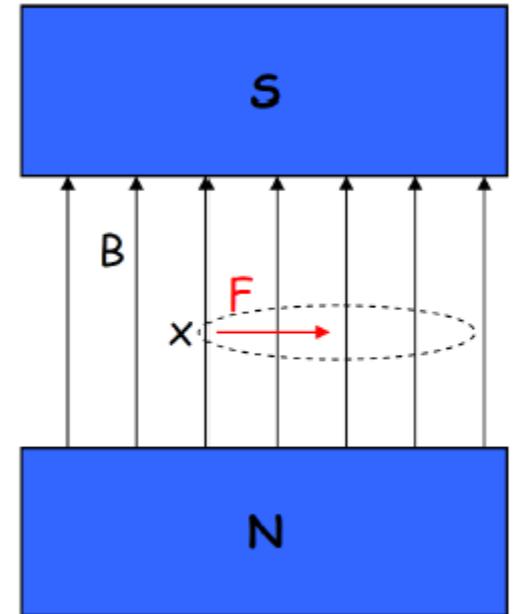
- Recall that the Lorentz force on a particle:

$$F = ma = e(E + v \times B) = \frac{mu^2}{r}$$

- In the absence of an E-field and assuming that B and v are perpendicular:

$$\frac{1}{r} = \frac{eB}{p}$$

- In an accelerator, dipoles are used to bend the beam trajectory. By using the appropriate field, one can tune the system so that particles of certain momentum can be transported only



# Quadrupole magnets

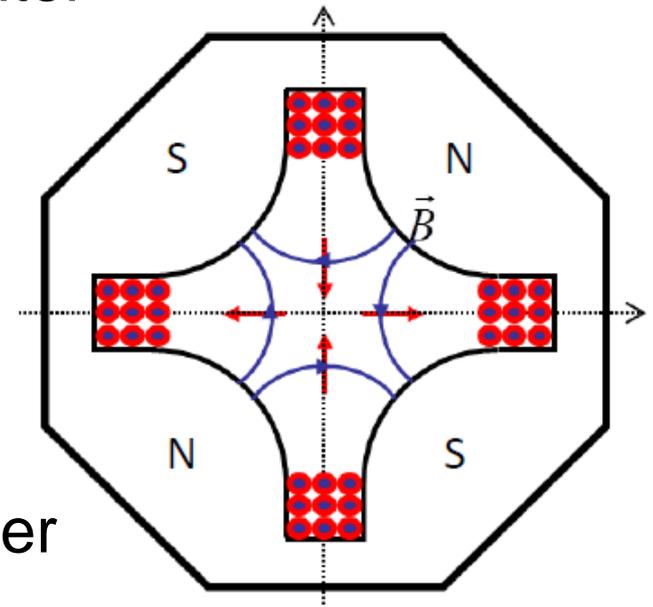
- Quad magnet has four poles and imparts a force proportional to distance from center
- Magnetic Field:

$$B_x = -Gy \text{ and } B_y = Gx$$

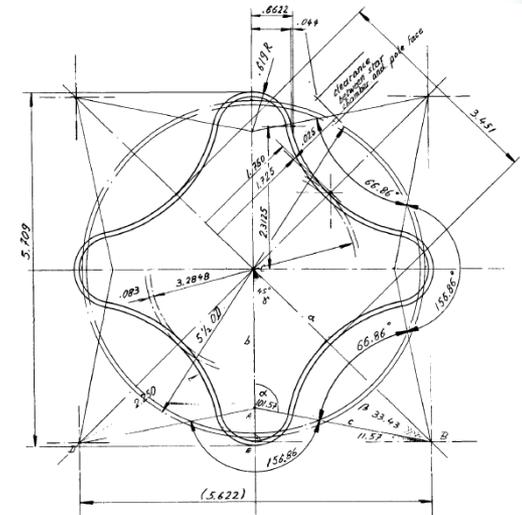
- Magnetic Force:

$$F_x = -qvGx \text{ and } F_y = qvGy$$

- Focus in one plane, defocus in the other
- Accelerators consist of a sequence of identical “FODO” cells which combine a focusing & defocusing quad, separated by a drift

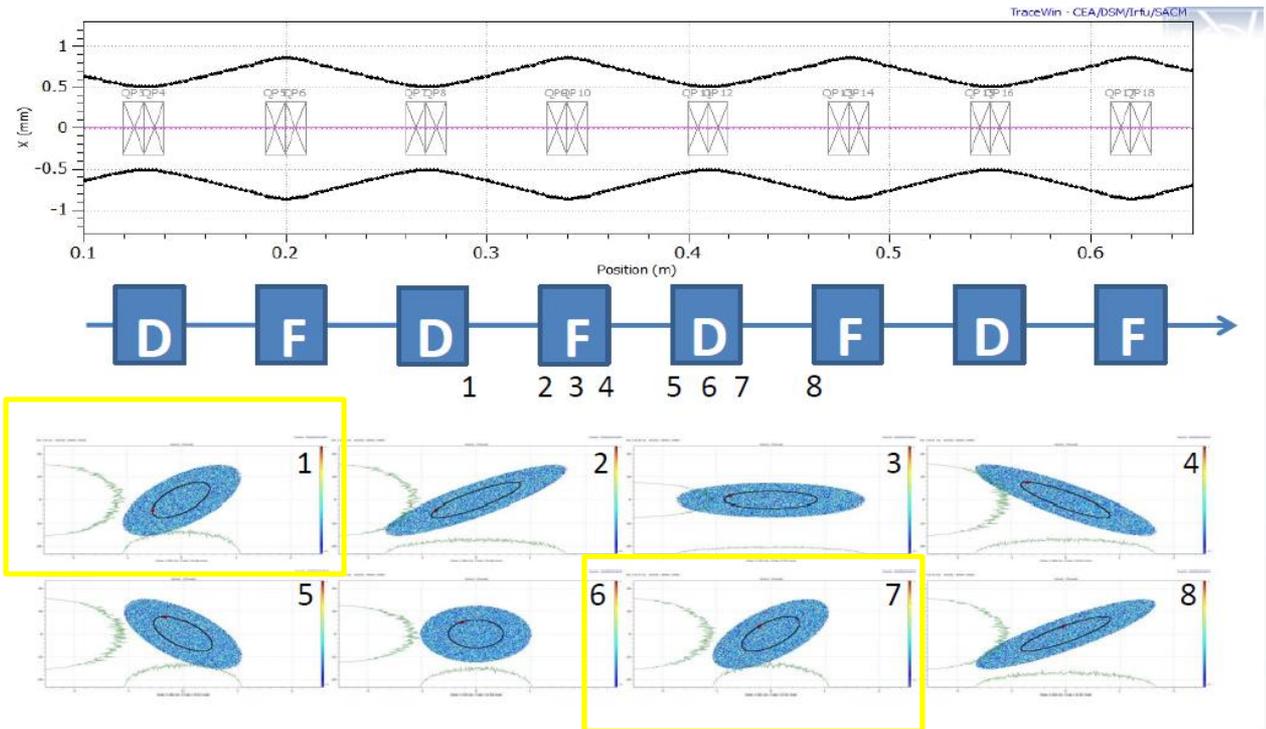
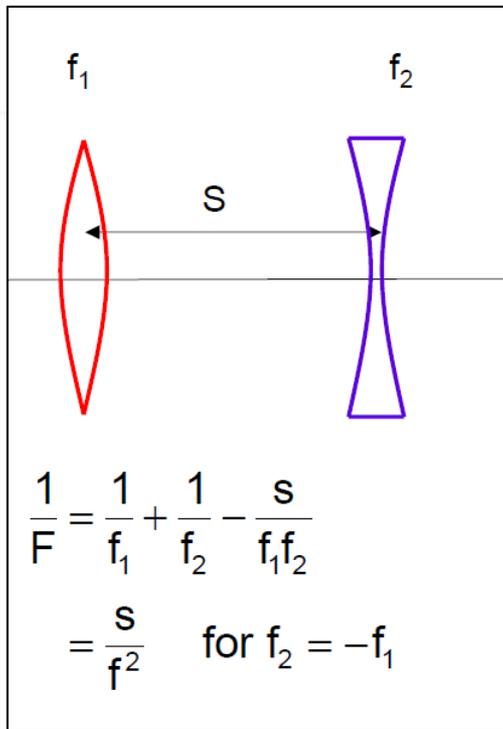


# Muon Campus quad magnets



- Most Muon Campus quads have special vacuum chambers that conform to the poles in order to extend the aperture and therefore maximize capture

# Focusing Defocusing (FODO) lines



- The beam is matched if after every period the Twiss parameters are identical

# Muon Campus beam lines

Muon campus M3 line



Quadrupole magnet

Muon campus Delivery Ring



Dipole magnet

# Optics considerations

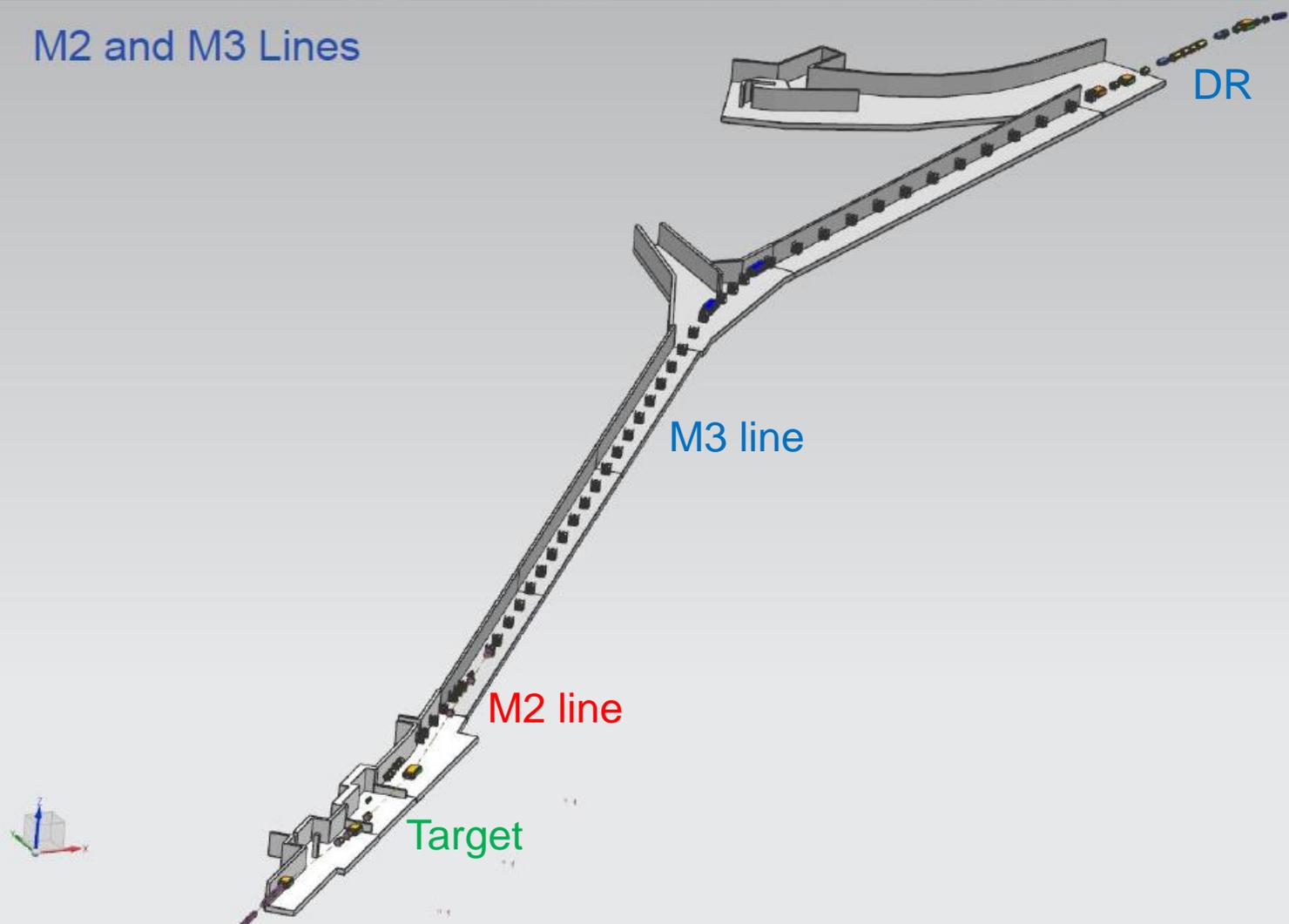
- M2-M3 lines are 280 m long. Exponential decay law predicts:

$$N = N_0 e^{-(t_{M2M3})/\gamma\tau_\pi} = 0.3N_0 \rightarrow 70\% \text{ of } \pi^+ \text{ decay}$$

- “Selected pions” from target dipole have a wide momentum spread  $\sim 10\%$
- Daughter muons have equal or lower momentum and even larger momentum spread
- They do not come from a single spot
- The optics of the channel must transport both  $\pi^+$  and  $\mu^+$
- Considerable momentum acceptance is needed

# Schematic layout

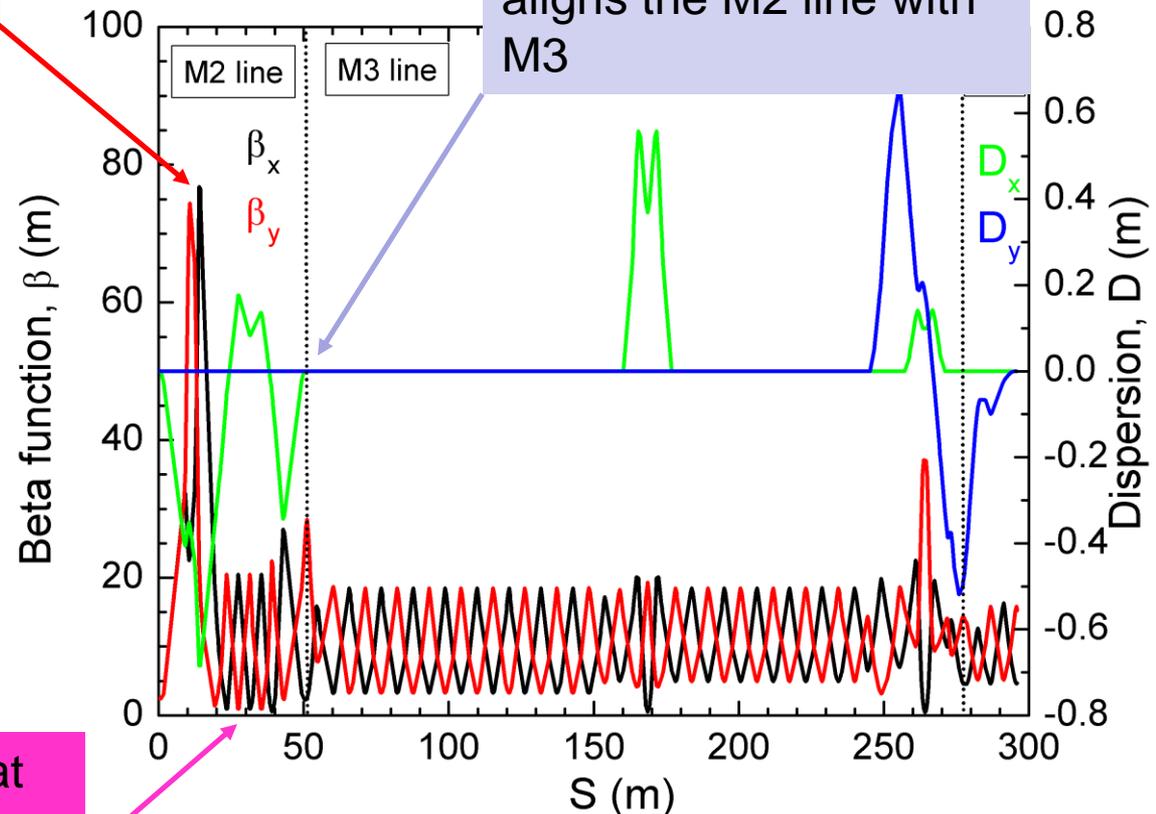
M2 and M3 Lines



# Muon capture & transport line (M2)

4 quads to match the target generated beam distribution

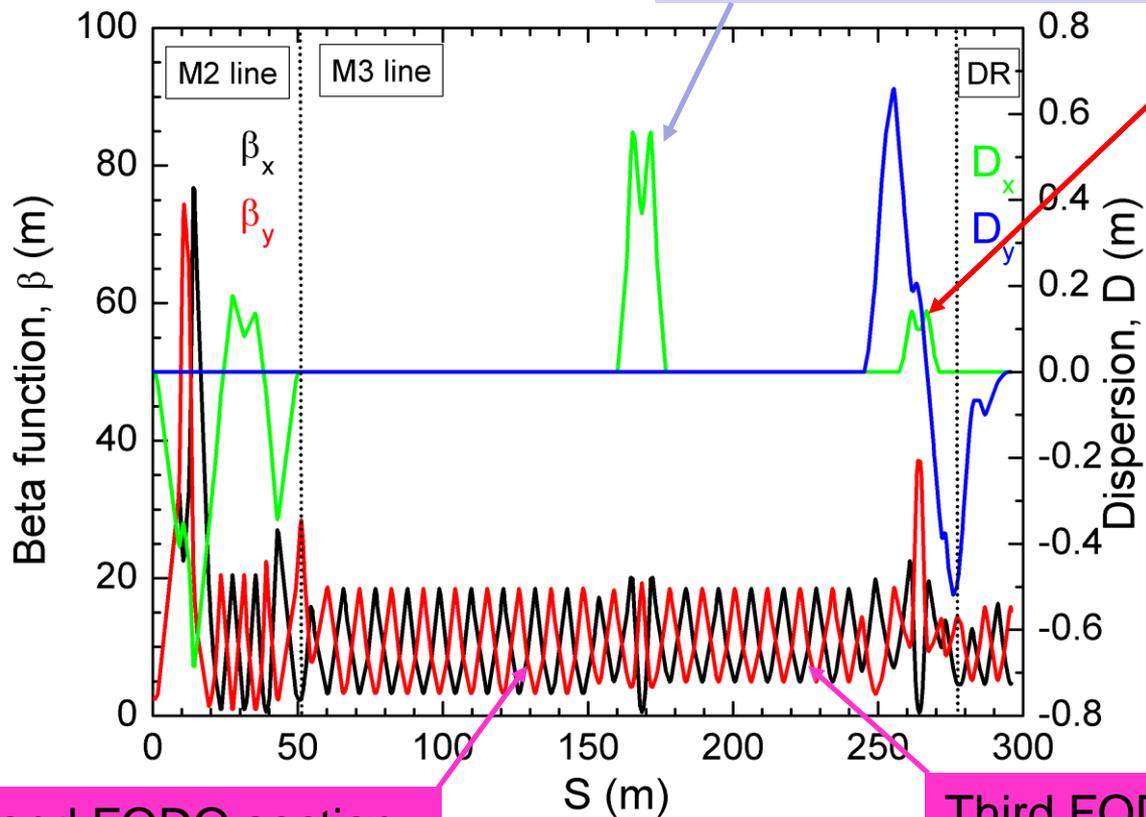
Second 3° bend that cancels dispersion and aligns the M2 line with M3



First FODO section at 120° phase advance

# Muon capture & transport line (M3)

Two 9.25 horizontal bending magnets to align with the DR injection leg

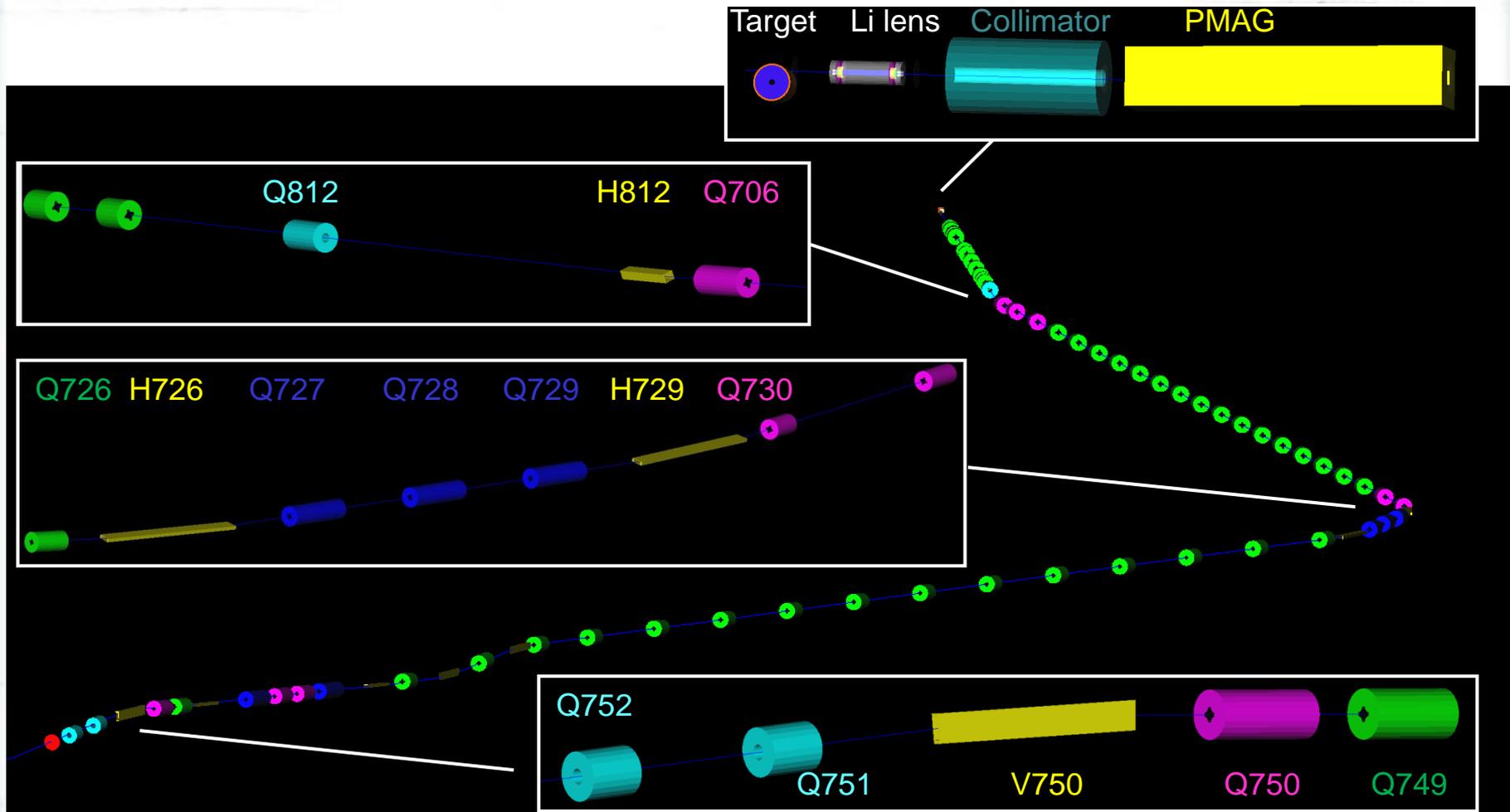


Series of horizontal and vertical bending to align with the injection leg of the DR

Second FODO section at 90° phase advance

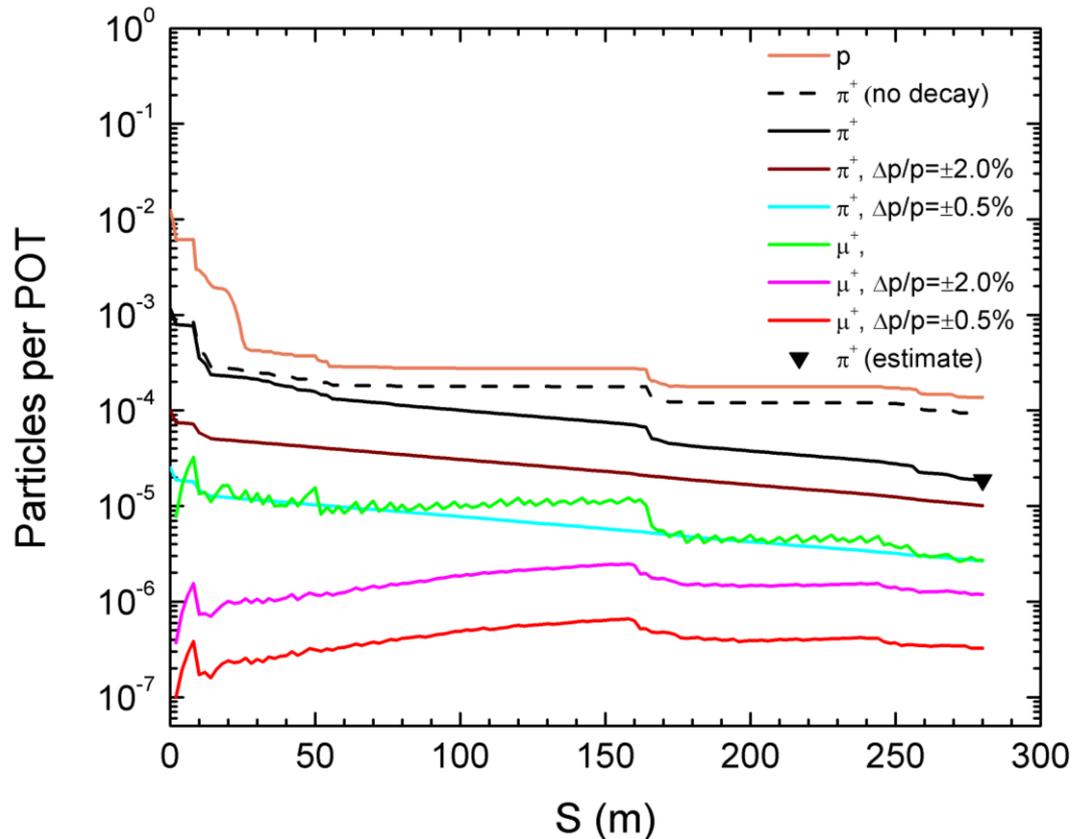
Third FODO section at 72° phase advance

# Model for the M2-M3 beamlines



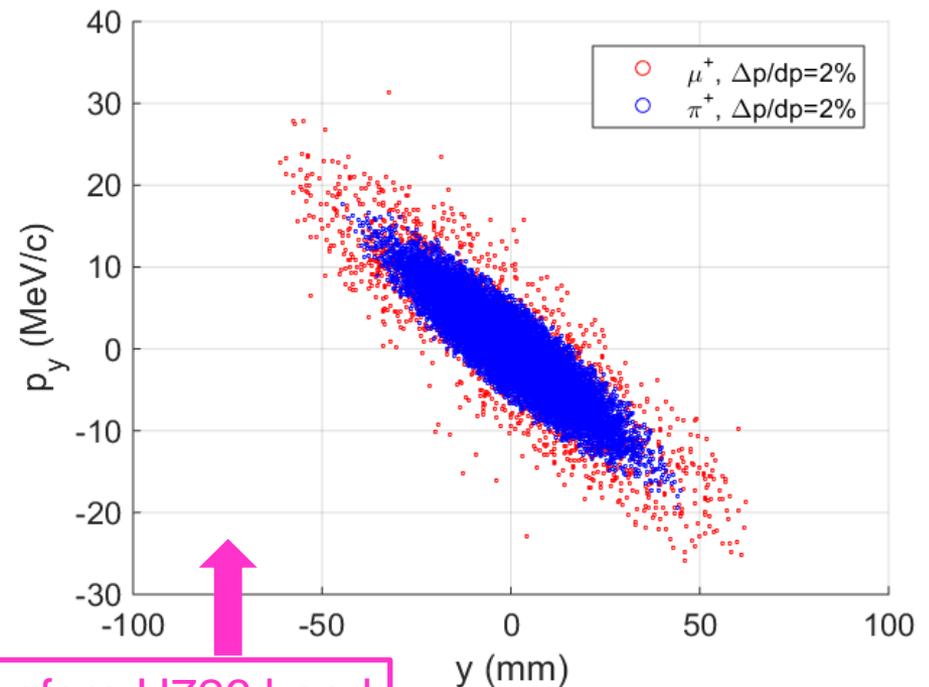
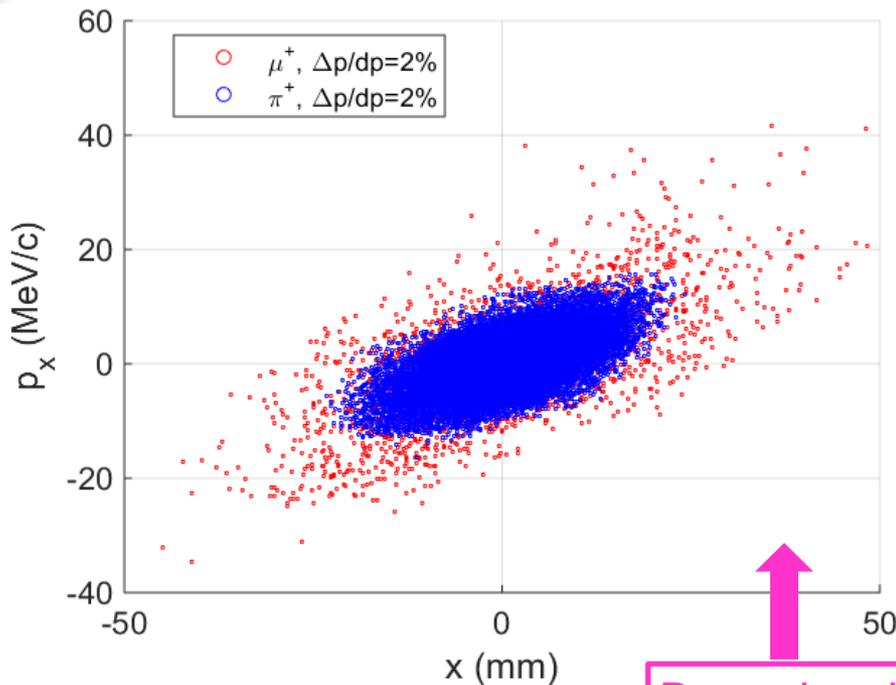
# Expected performance

- Secondary beam consist of protons, pions, muons, positrons and deuterons



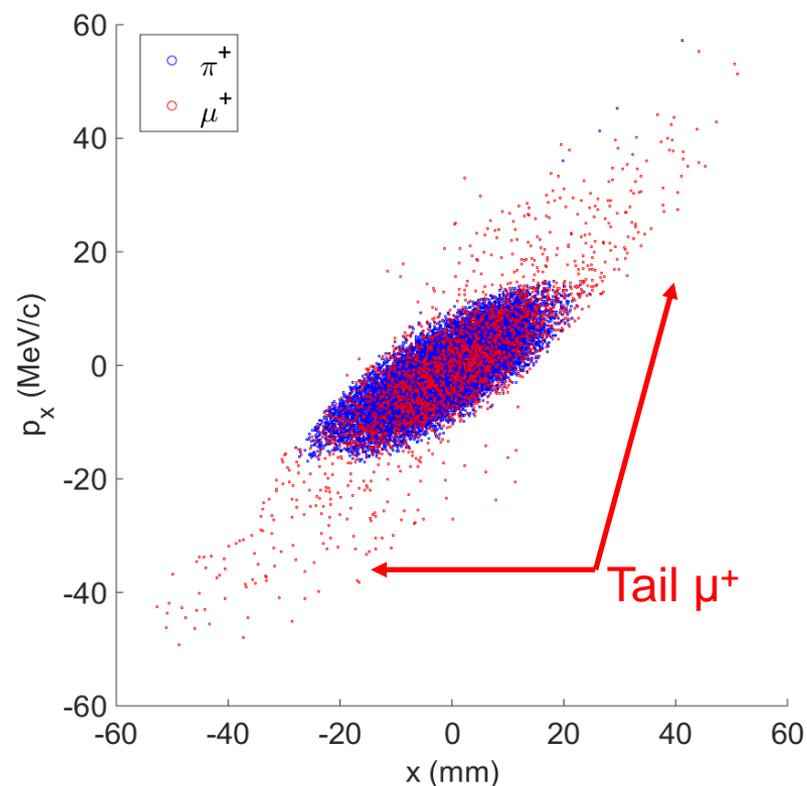
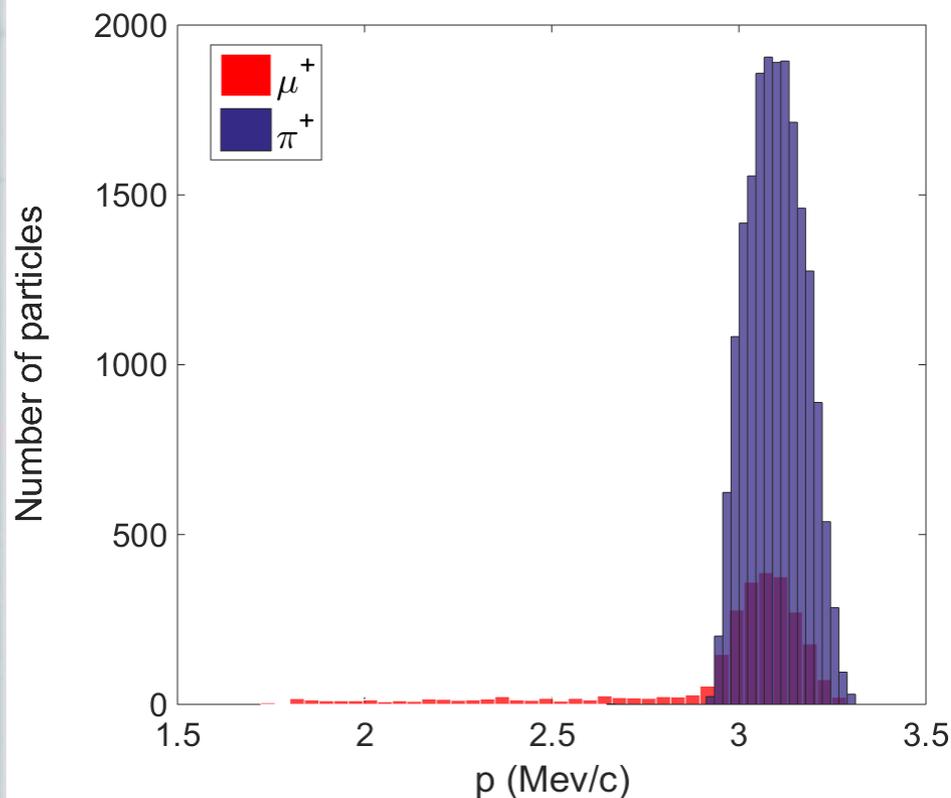
# Phase-space analysis: $\pi$ vs $\mu$

- $\mu^+$  have larger transverse momentum (compared to  $\pi^+$ )
- As a result, muons are lost in apertures between H726 & H729 bends



Beam just before H726 bend

# Muons at the end of M3



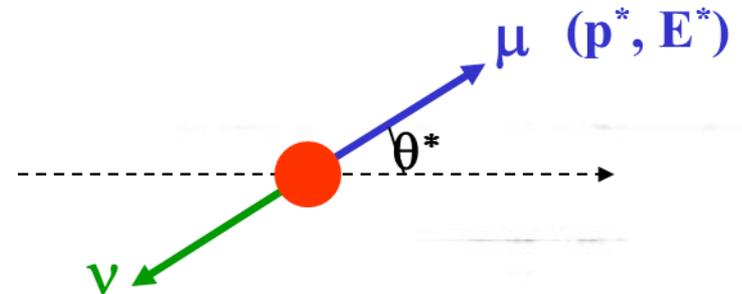
- Distribution contains an order of magnitude more  $\pi^+$  than  $\mu^+$
- Distribution of  $\mu^+$  has a long low-momentum tail

# Energies of newborn muons

- In the pion rest frame:

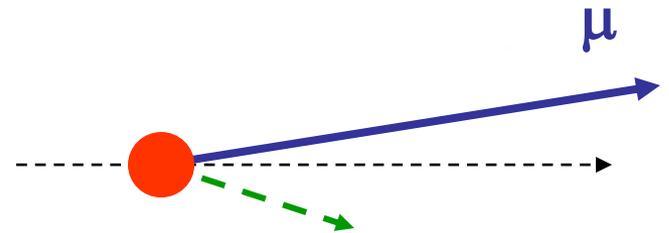
$$p^* = \frac{m_\pi^2 - m_\mu^2}{2m_\pi} = 30 \text{ MeV}/c$$

$$E^* = \frac{m_\pi^2 + m_\mu^2}{2m_\pi} = 110 \text{ MeV}$$



- Boost to laboratory frame:

$$E_\mu = \gamma_\pi (E^* + \beta_\pi p^* \cos\theta^*)$$



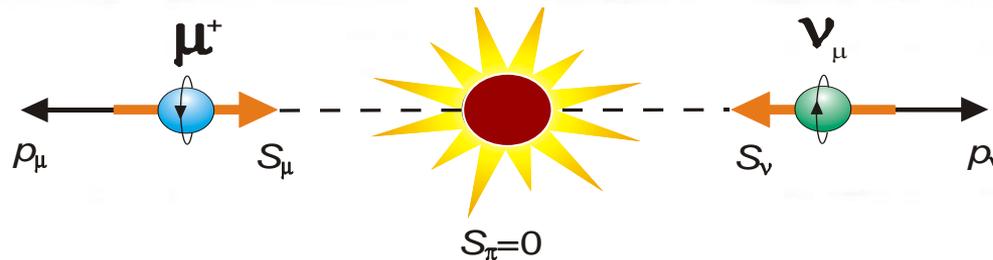
- Limiting cases:

- $\cos\theta = +1 \rightarrow E_{max} = 1.00 \times E_\pi$  (forward decays)

- $\cos\theta = -1 \rightarrow E_{min} = 0.57 \times E_\pi$  (backward decays)

(This will be a homework problem)

# Polarization of newborn muons



- Muons from pion decay are naturally polarized. Their polarization is highly depended on the momentum ratio between the new born muon and its parent pion,  $x = p_\mu/p_\pi$
- Transverse polarization is given by:

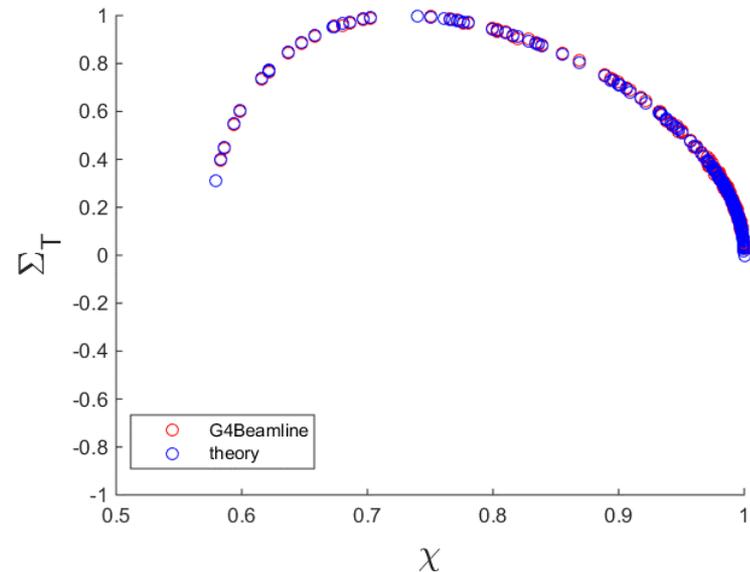
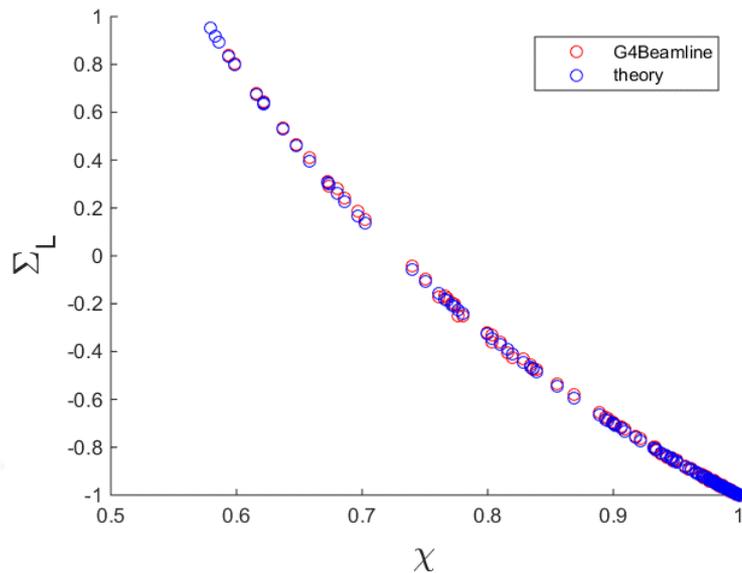
$$P_T = \frac{2b}{x(1-b^2)} [(1-x)(x-b^2)]^{1/2}, \quad b = m_\mu/m_\pi$$

- Longitudinal polarization is given by:  $P_L = \frac{x(1+b^2)-2b^2}{x(1-b^2)}$

(This will be a computer lab problem)

# Polarization in the Muon Campus (1)

- The rms momentum spread of the Muon Campus is  $\sim 2\%$
- Muons from forward decays are surviving and the muon polarization is expected to be  $>90\%$



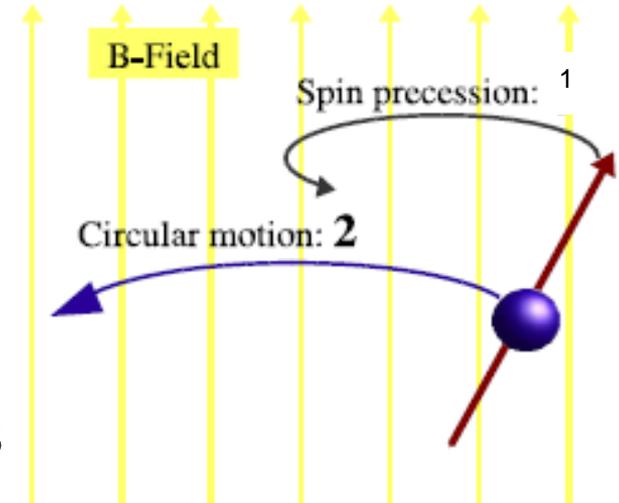
# Spin precession in B-fields (1)

- If we put a muon into motion in a plane transverse to a magnetic dipole field, both momentum and spin precess
- Momentum precession (cyclotron motion):

$$\frac{d\vec{p}}{dt} = e\vec{v} \times \vec{B} \rightarrow \omega_c = \frac{eB}{\gamma mc}$$

- Spin precession (Larmor and Thomas motion):

$$\frac{d\vec{S}}{dt} = \vec{\mu} \times \vec{B} \rightarrow \omega_s = \frac{geB}{2mc} + (1 - \gamma) \frac{eB}{\gamma mc}$$



# Spin precession in B-fields (2)

- Difference between these two outcomes form an anomalous magnetic moment not predicted by pure Dirac theory

$$\omega_a = \omega_c - \omega_s = \left( \frac{g - 2}{2} \right) \frac{eB}{mc} = \alpha_\mu \frac{eB}{mc}$$

- In other words, when a muon passes through a bending magnet, its spin vector rotates slightly more than the bending angle due to precession in the B-field.

