

# Delivery Ring

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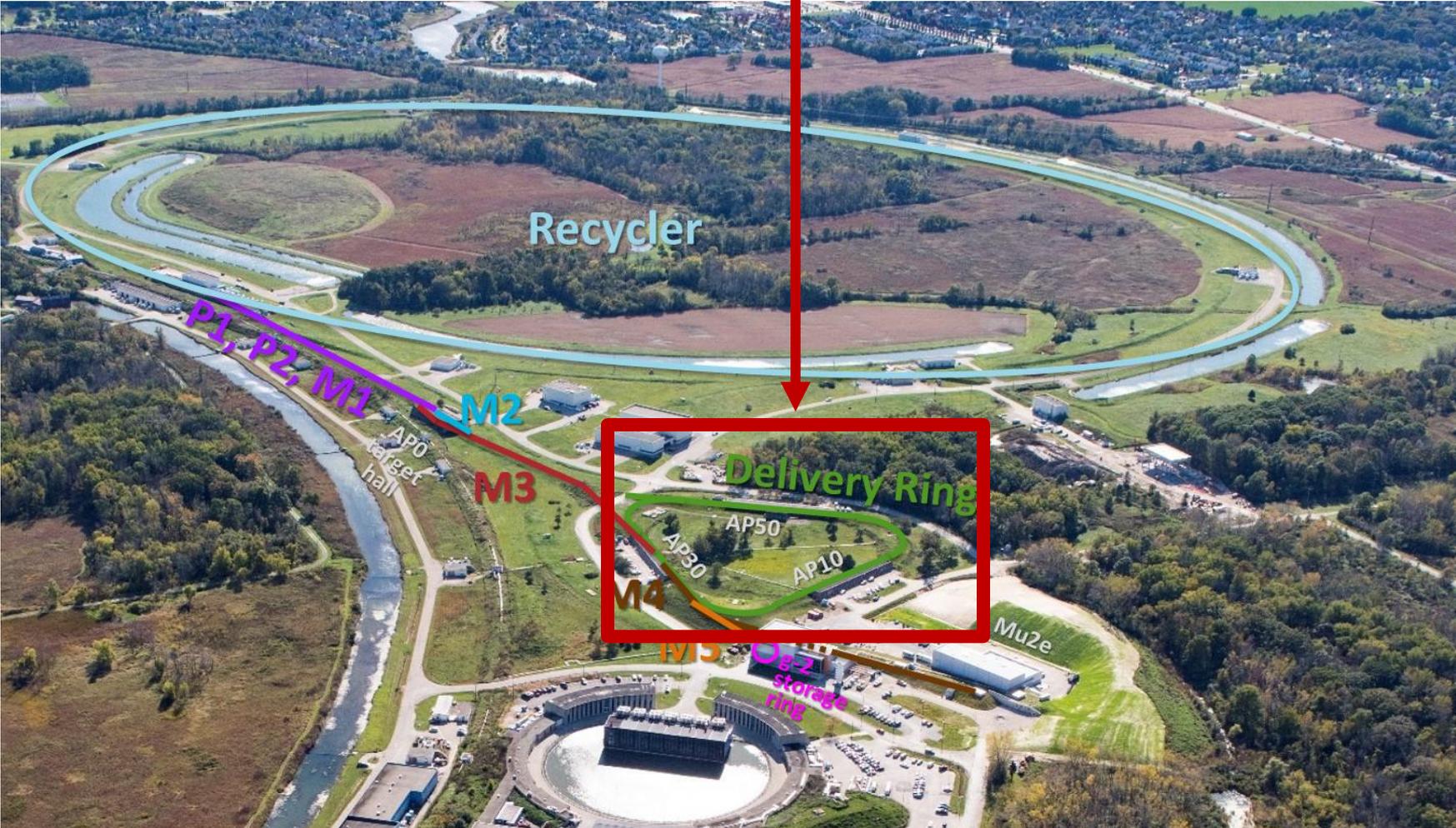
Diktys Stratakis  
Fermi National Accelerator Laboratory

USPAS 2019  
January 23, 2019

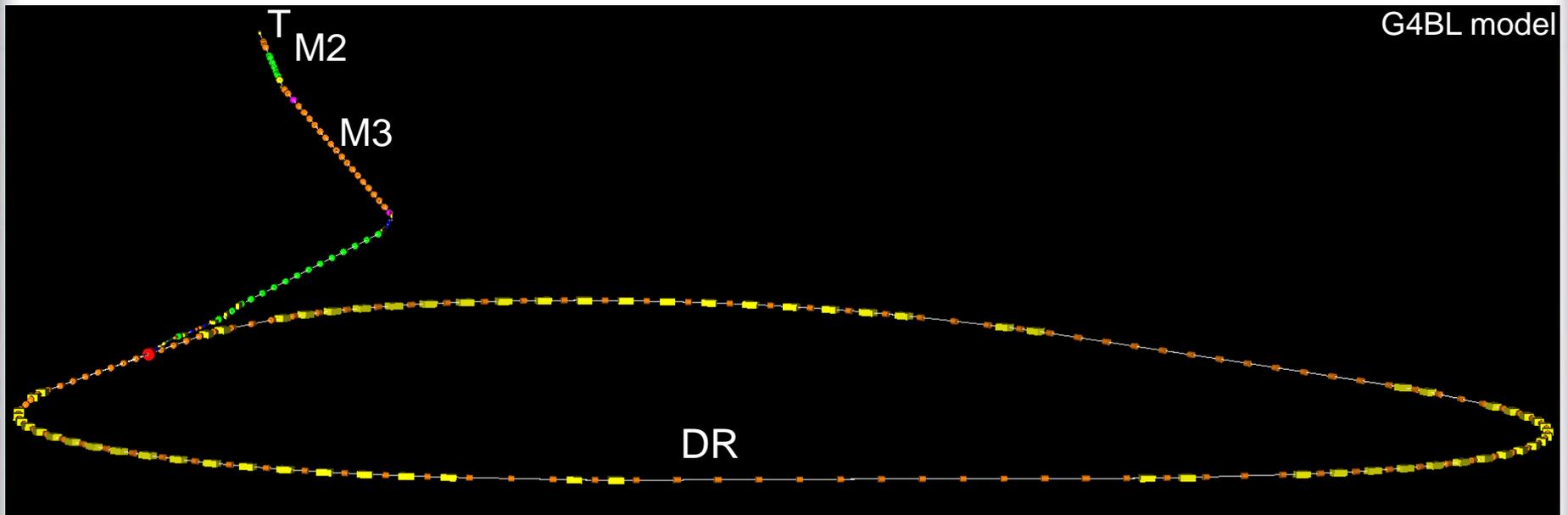
# Outline

- Injection and extraction
- Beamline optics and performance
- Proton removal in the DR
- Triggers of errors in the DR

# Deliver Ring (DR)



# Simulation model



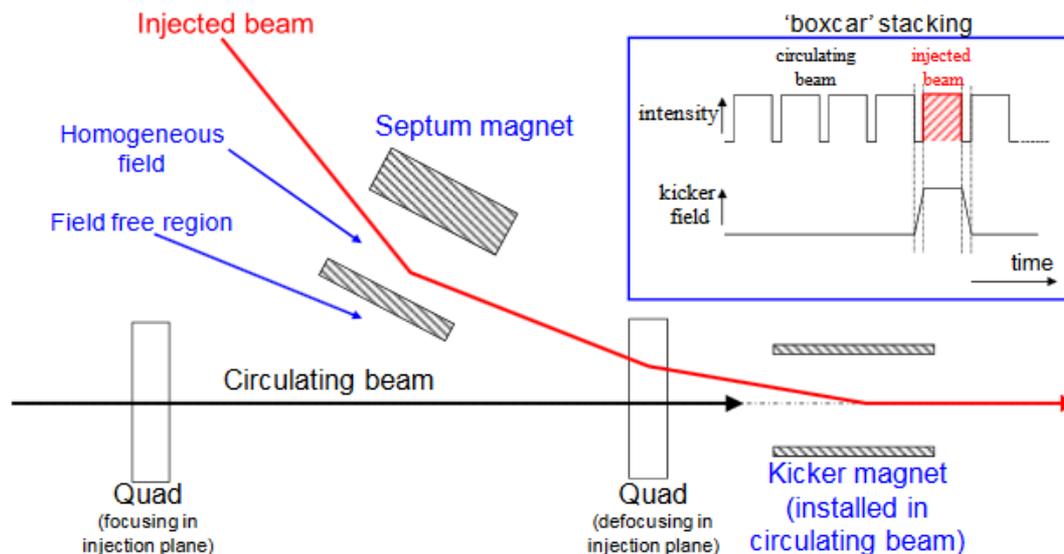
- M2 & M3 lines will carry the secondary beam from the target (T) to the delivery ring (DR)
- Loop four times until  $\mu^+$  yield peaks and all p are removed

# Injection & extraction

- What makes a good injection?
  - Inject a particle beam into a circular accelerator at the appropriate time
  - Minimize loss and place injected particles onto the correct trajectory, with the correct phase-space parameters
- What makes a good extraction?
  - Extract the particles from an accelerator to a transfer line or a beam dump, at the appropriate time
  - Minimize loss and place the extracted particles onto the correct trajectory, with the correct phase-space parameters
- Both are important for good performance of an accelerator
- For g-2, we are interested for single turn (fast) injection and extraction

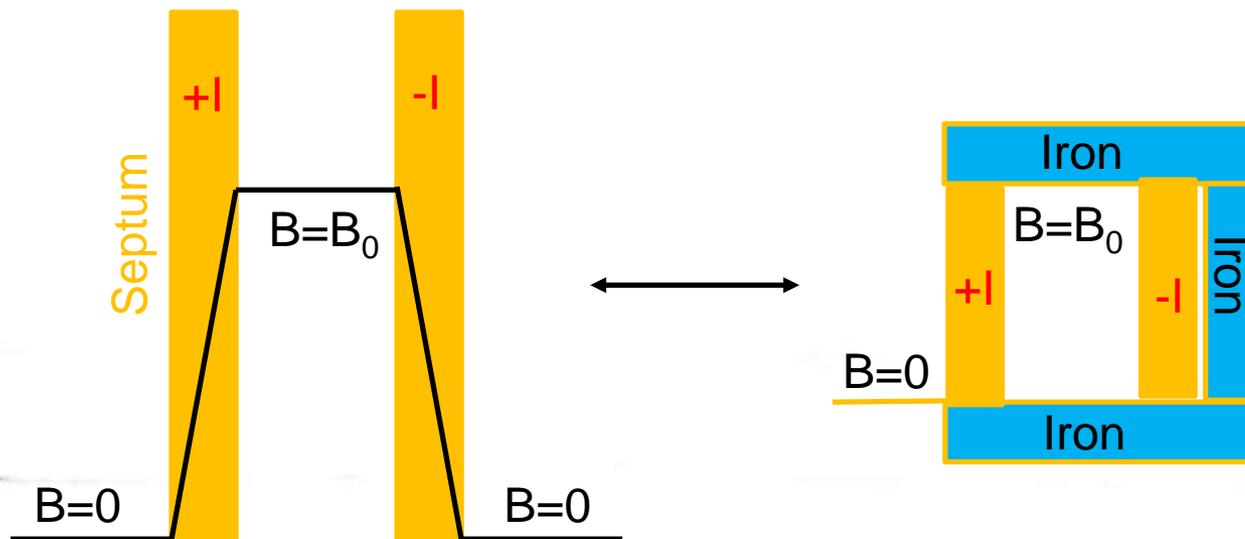
# Injection mechanism

- Requires a combination of septa and kicker magnets
- Septa:
  - Can be magnetic or electrostatic
  - Have two vacuum chambers
  - Provide slower field rise/fall times but stronger field compared to kickers
- Kickers:
  - One vacuum chamber (like dipoles)
  - Fast field rise/fall times ( $\ll 1 \mu\text{s}$ ) but weaker field compared to kickers



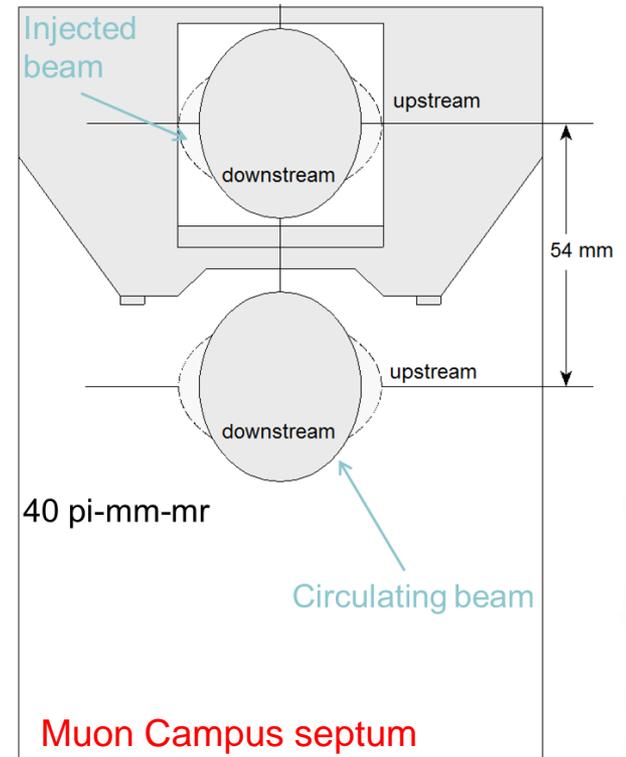
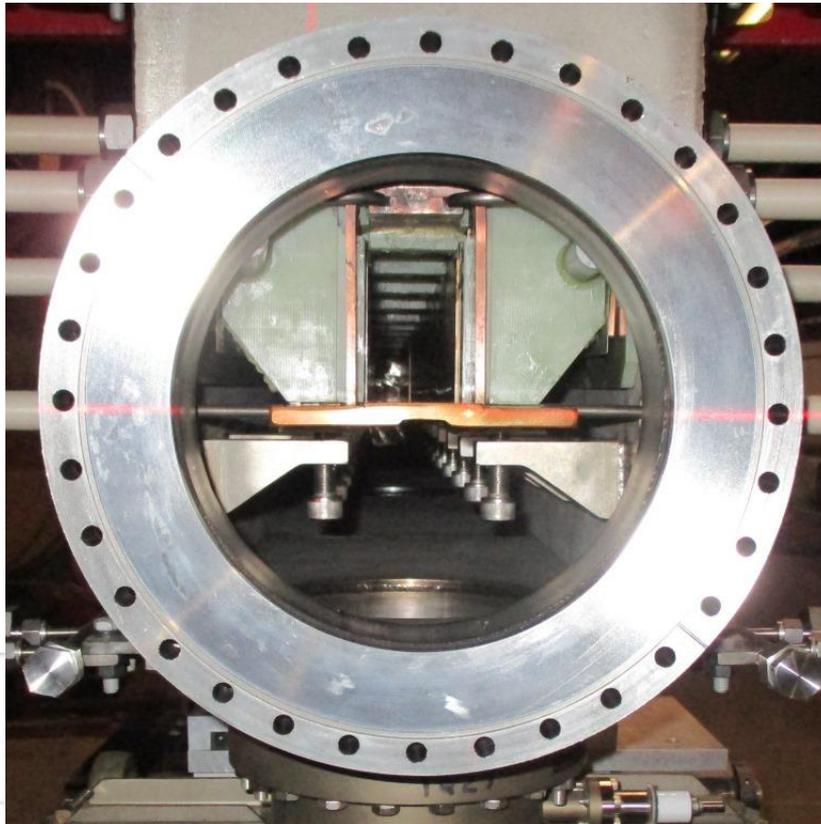
# Magnetic septum

- The deflected beam goes through homogeneous B-field established between magnetic coils. The circulating beam passes next to the main magnetic circuit and “sees” no B-field.
- It uses current (I) to separate field regions



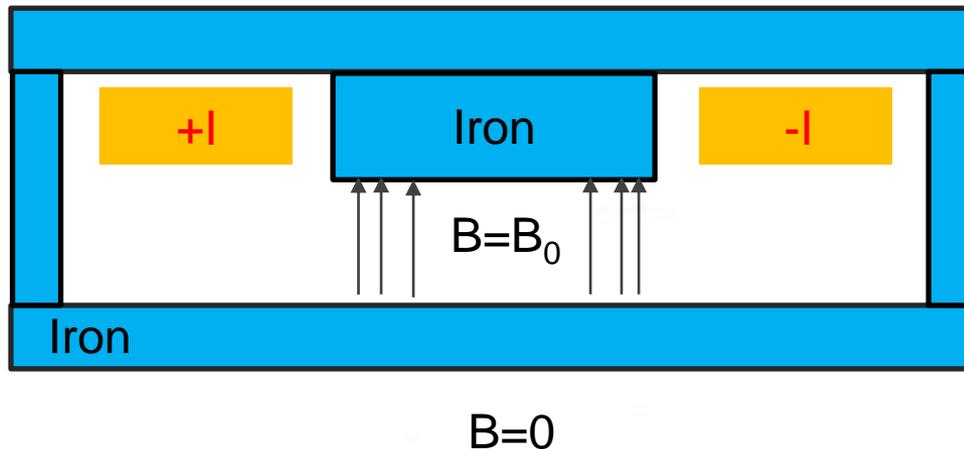
# Muon Campus magnetic septum

- For the Muon Campus, a magnetic septum is used to inject beam to the DR and to abort the proton beam



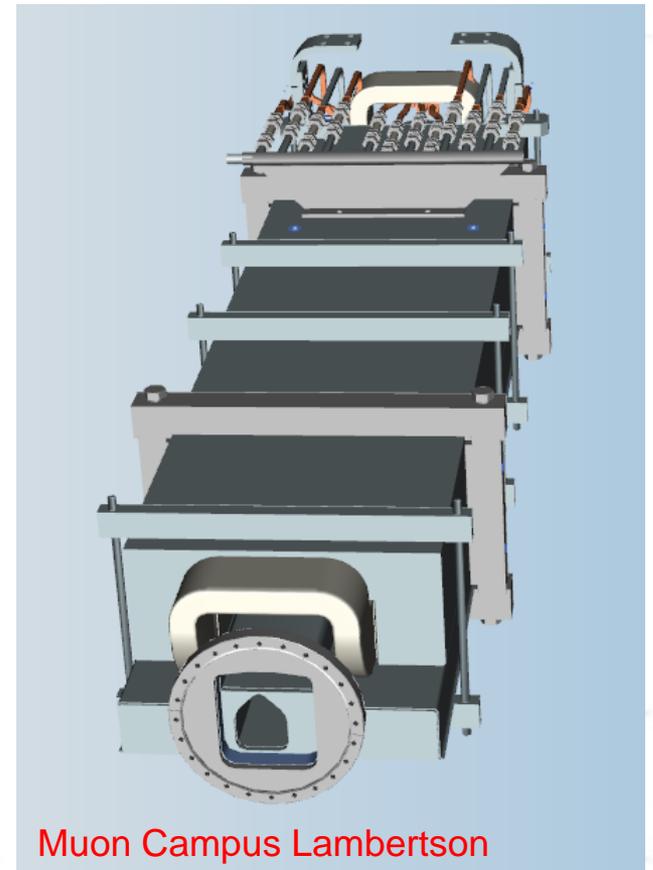
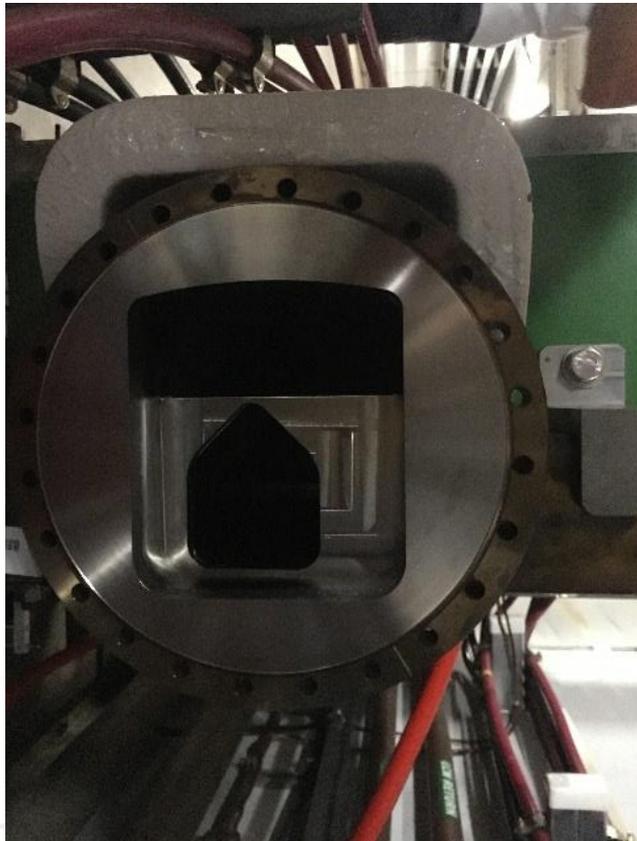
# Lambertson septum

- Two field regions like a magnetic septum. BUT there is magnetic material that separates the two field regions
- A kicker magnet is used to deflect the beam vertically first and then the Lambertson magnet deflects the beam horizontally or vice versa



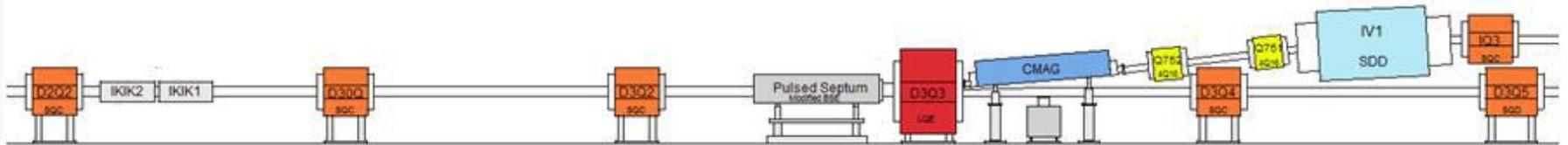
# Muon Campus Lambertson septum

- For the Muon Campus, a magnetic septum is used to extract the beam out of the DR

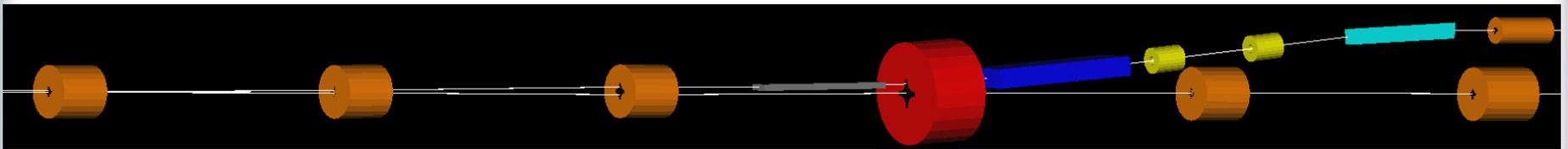


# Injection to the Delivery Ring

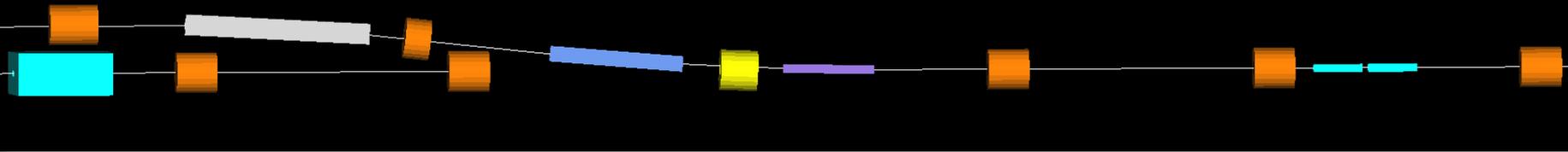
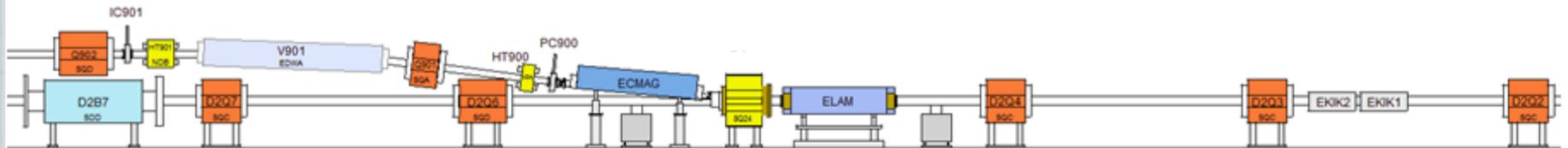
- Conceptual design



- Simulation model

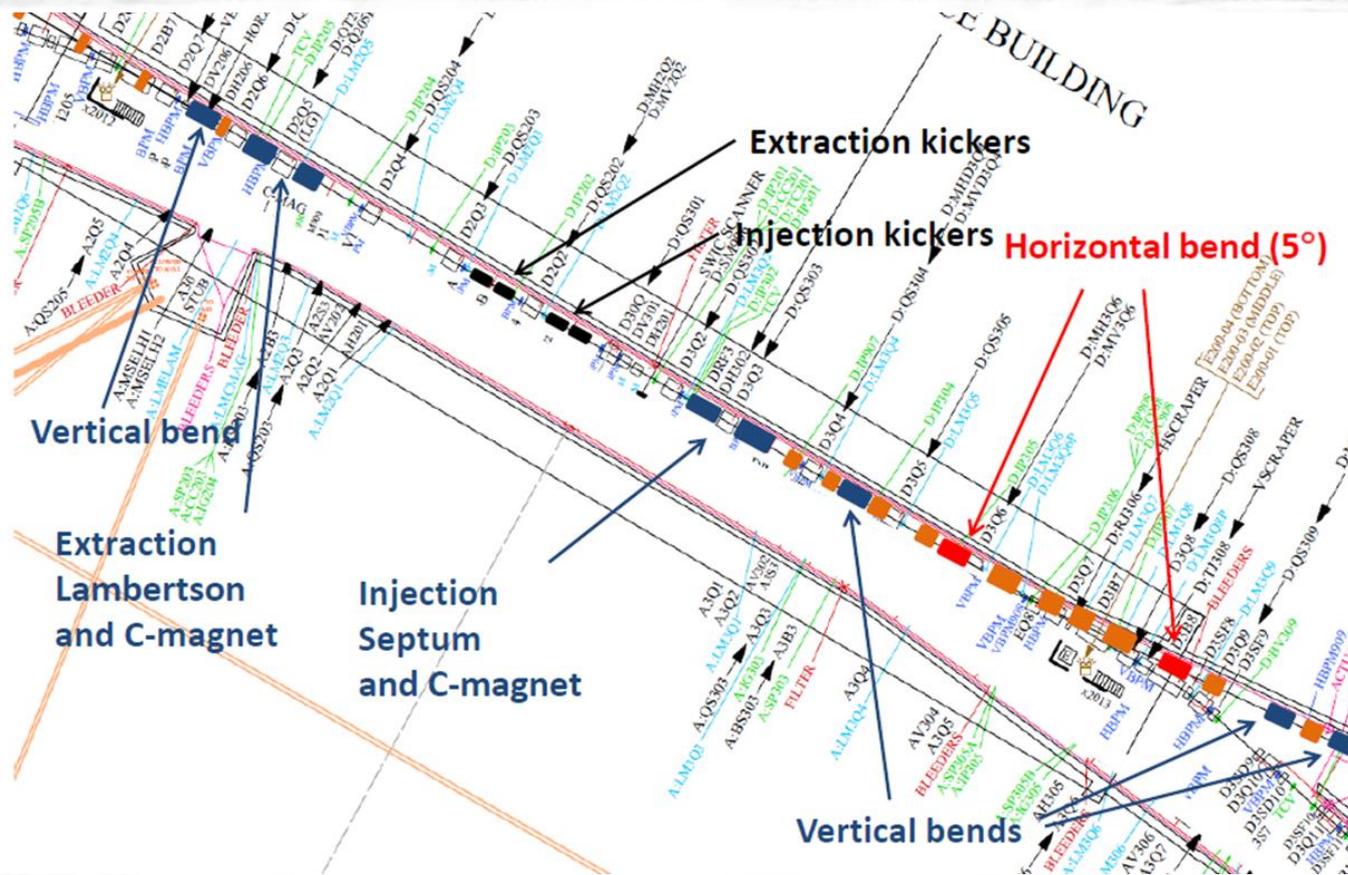


# Extraction from the Delivery Ring



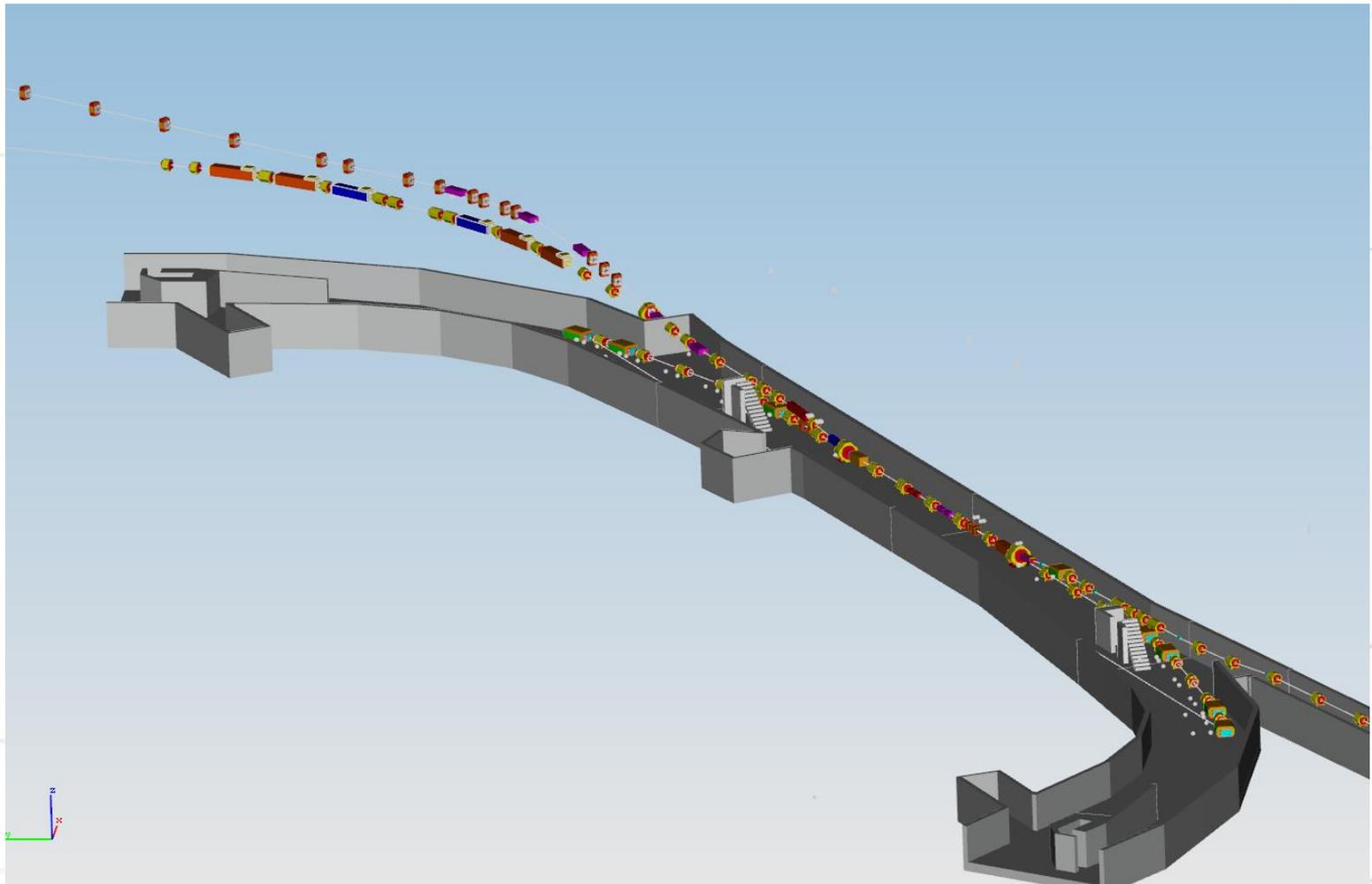
- Beam is extracted with a pair of horizontal kickers
- Subsequently, a Lambertson and C-magnet pair will be used to bend the beam upward out of the Delivery Ring

# Straight D30 section



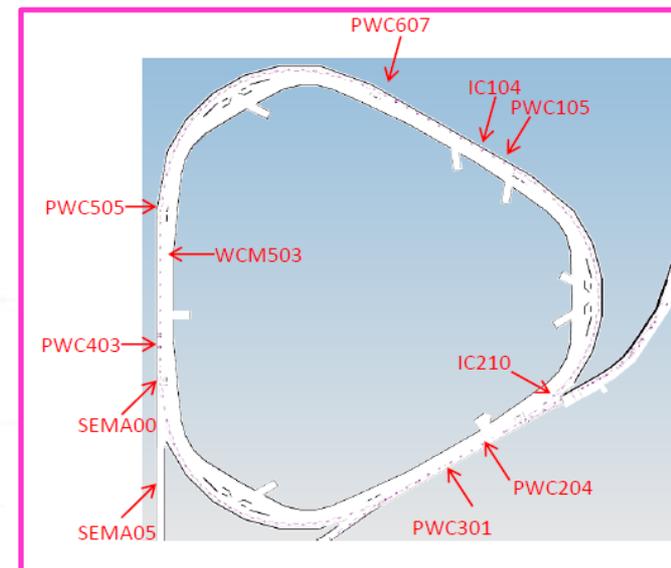
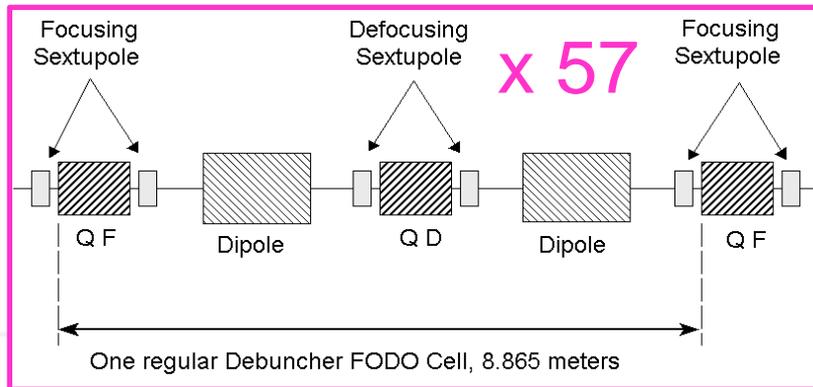
- Injection into and extraction out of the DR happens at the same straight section and contains the smallest apertures.

# Straight D30 section

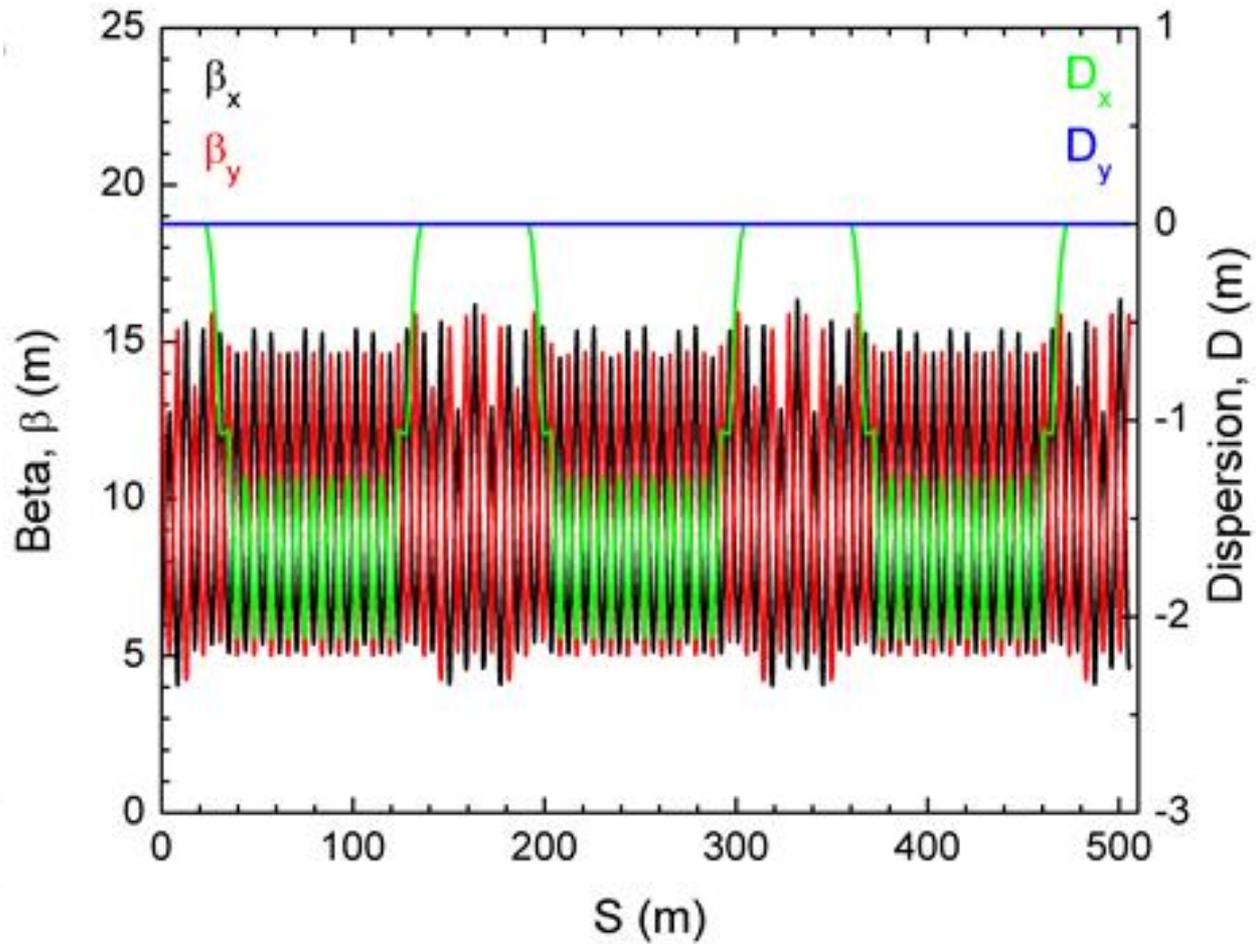


# Delivery Ring lattice

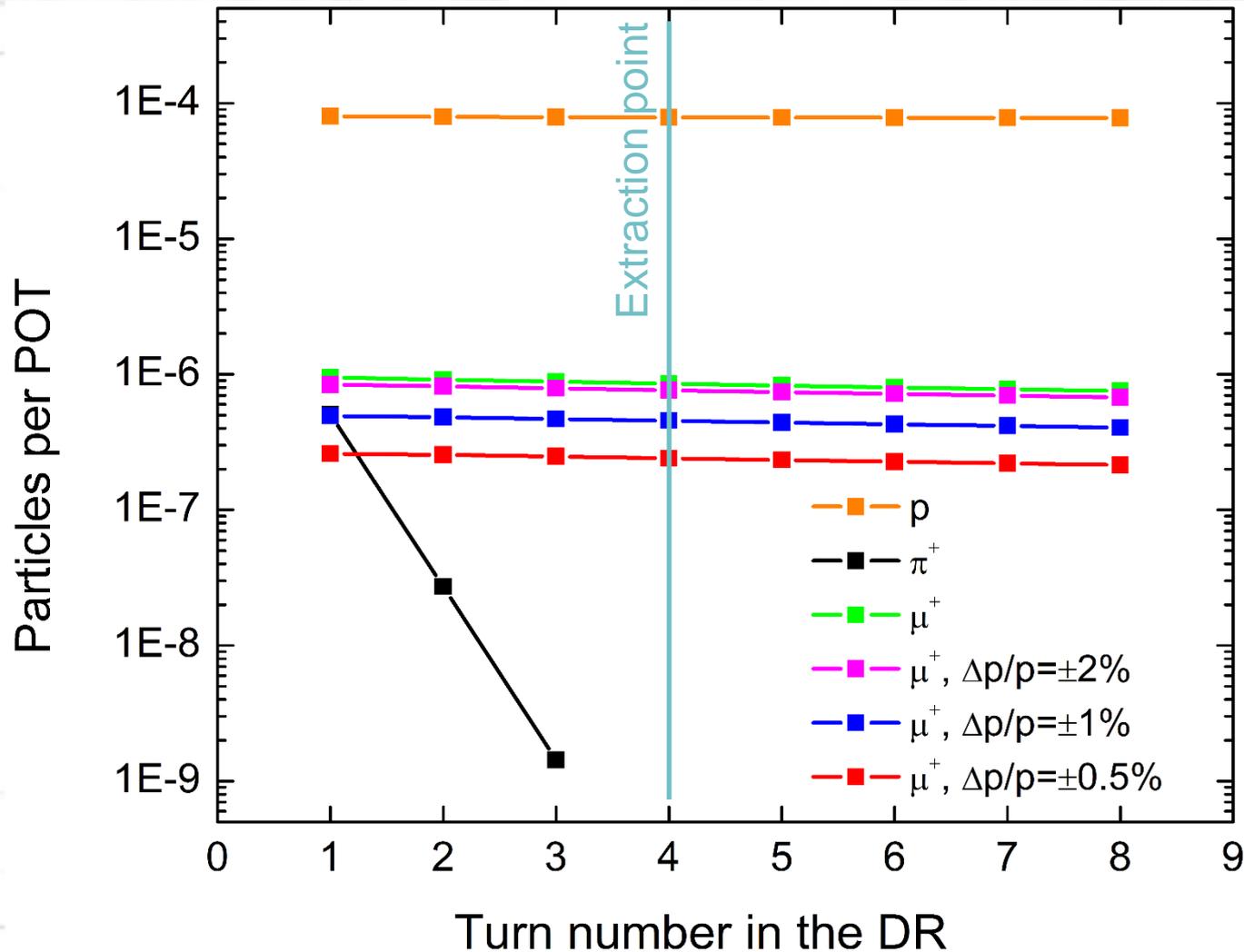
- Features of the DR
  - Three long dispersion free straight sections together with 3 arc sections
  - 57 FODO cells and 66 dipoles
  - Ideal particle will follow a particular trajectory, which closes on itself after one turn (closed orbit)



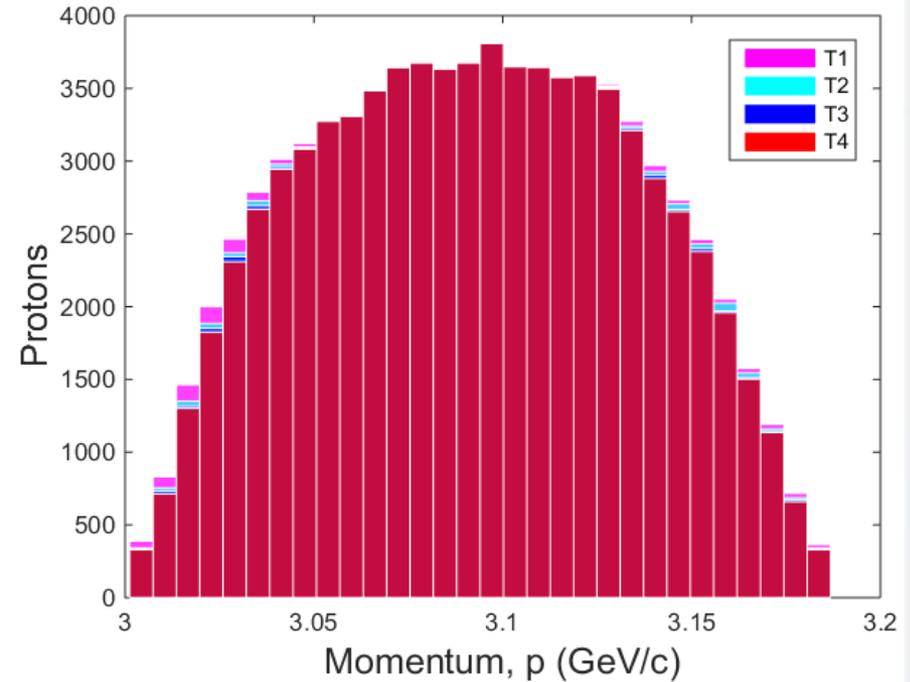
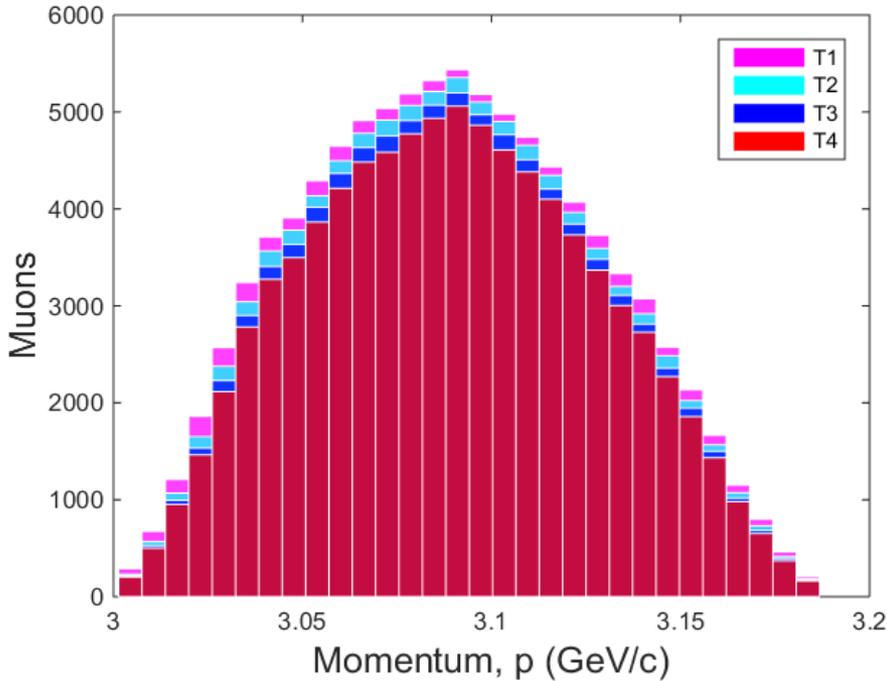
# Delivery Ring optics



# Performance of the Delivery Ring



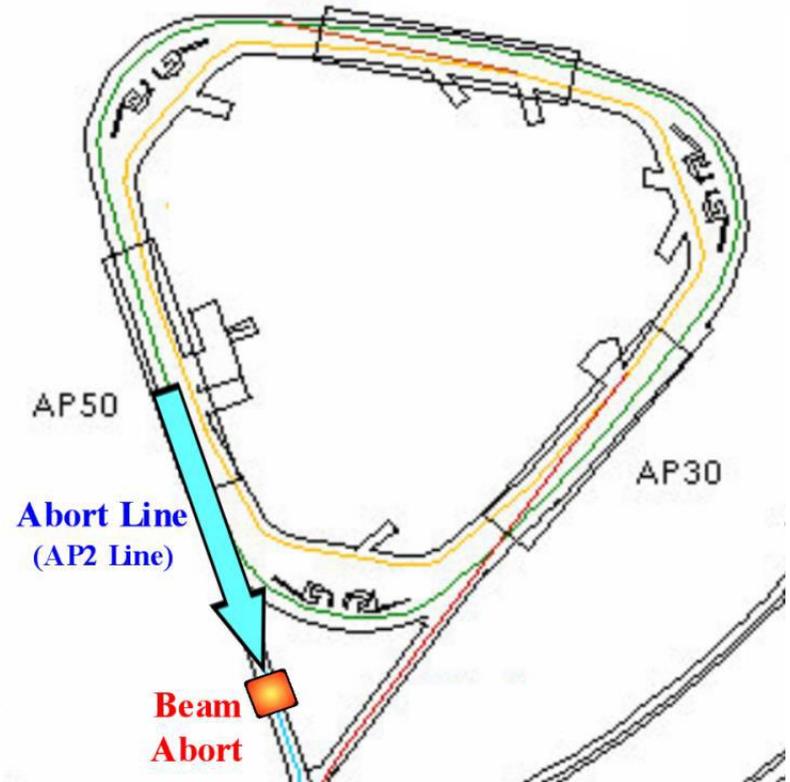
# Performance of the Delivery Ring



- Muon beam is peaked near “magic” momentum with  $\Delta p/p = \pm 1.5\%$

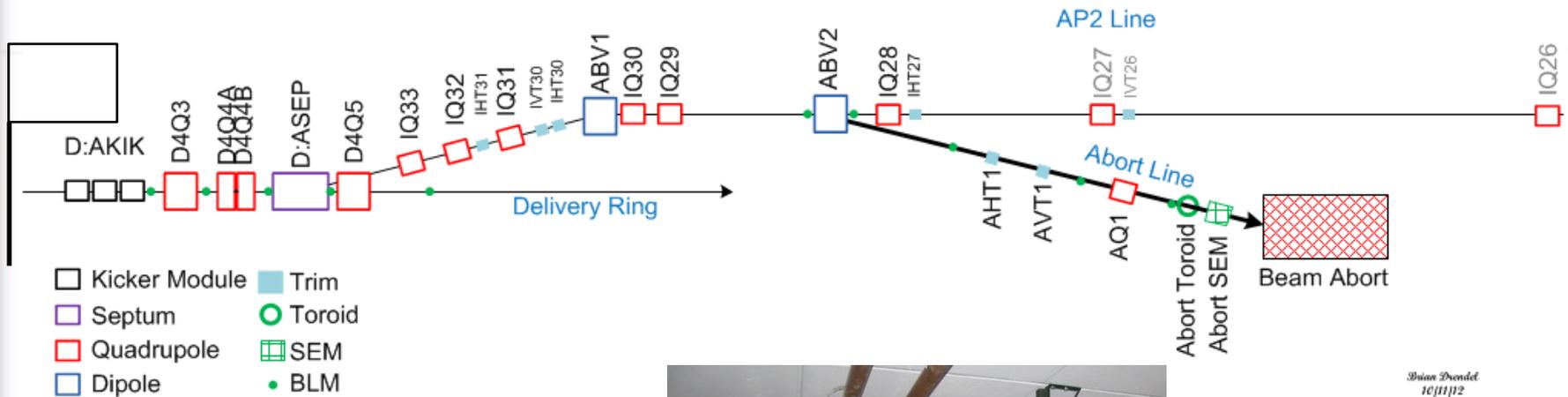
# Proton removal

- Proton beam is removed by means of kicker magnet
- The kicker rise time is  $\sim 180$  ns
- Multiple revolutions are required to provide enough kicker gap between muons and protons

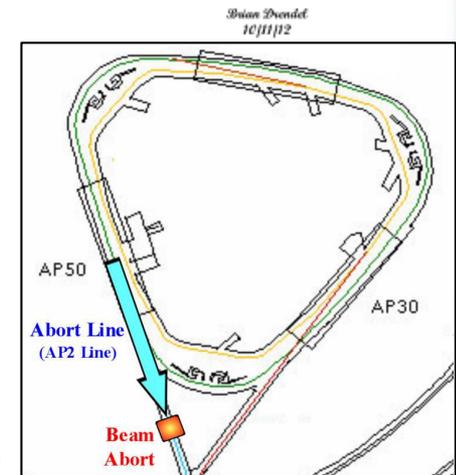


# Abort line

## Vertical Profile of the Delivery Ring Abort Line



Kicker rise time ~180 ns

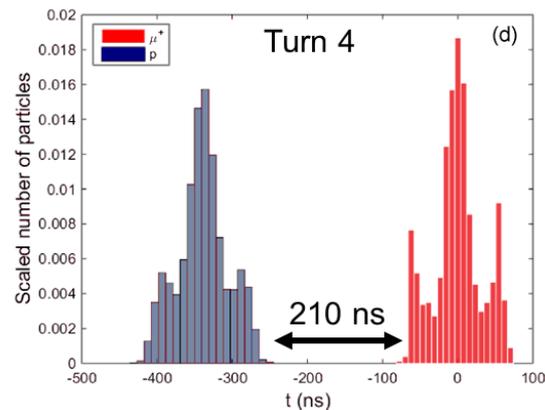
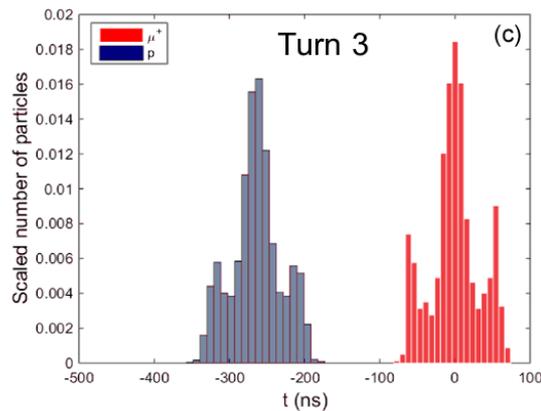
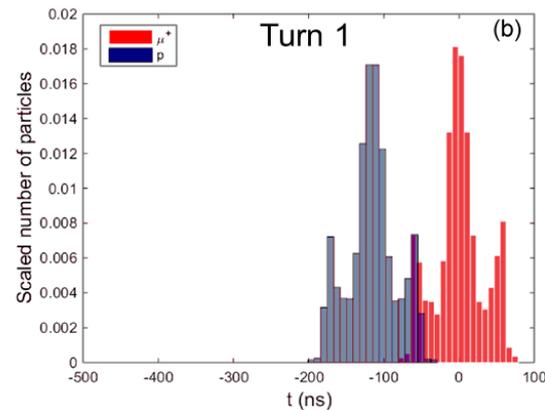
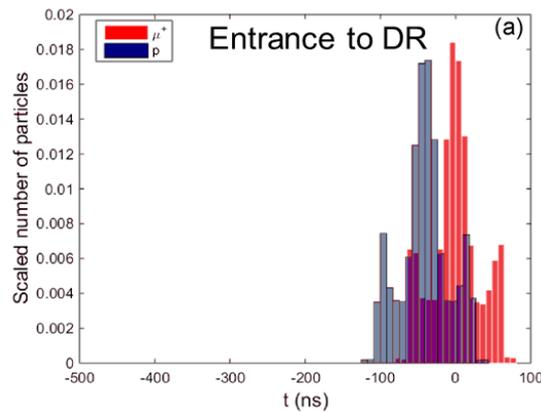


Brian Dondel  
10/11/12

# Bunch separation

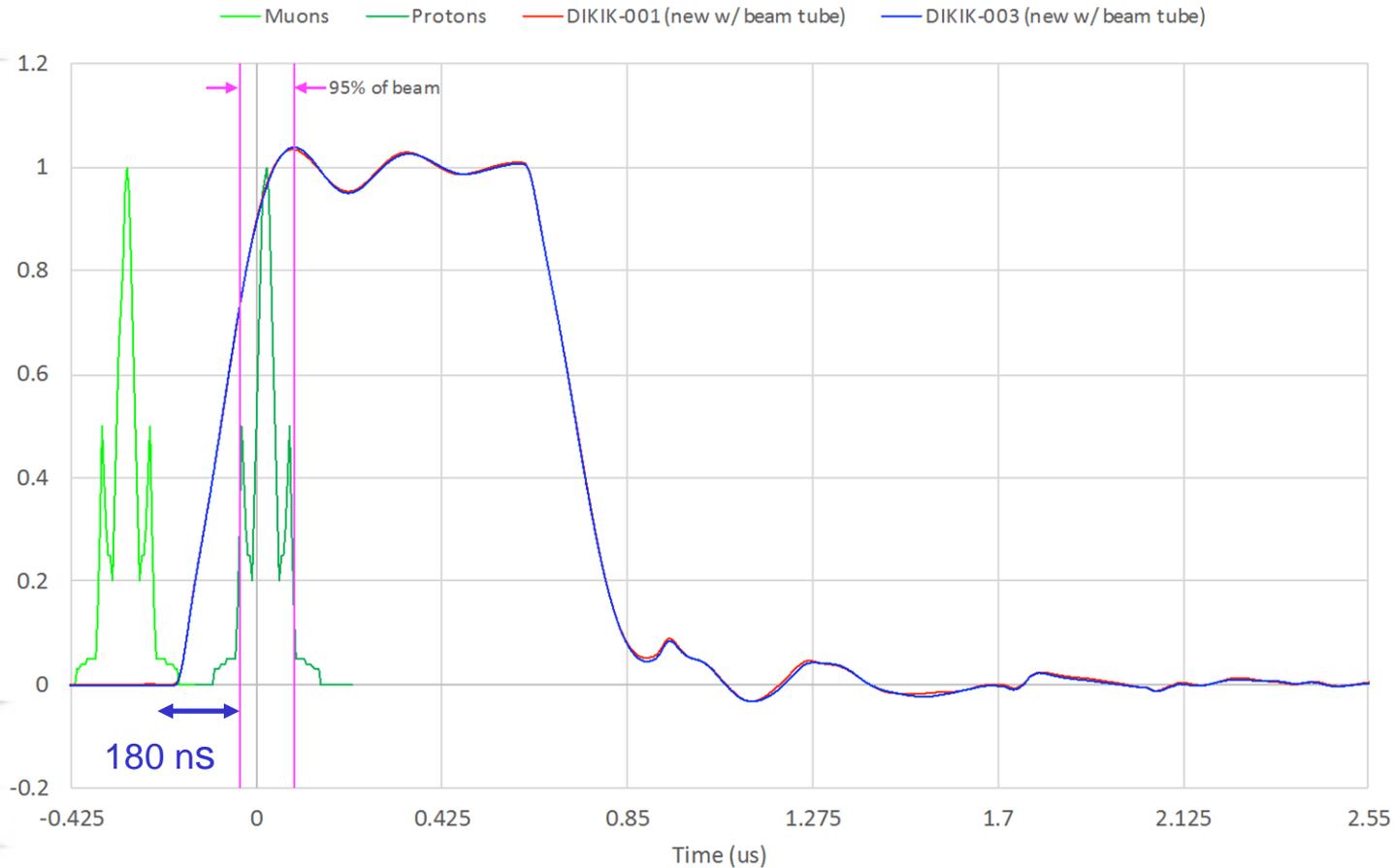
- Revolution times for 3.1 GeV/c beam:

$\mu^+, \beta = 0.999, T = 1685.5 \text{ ns}$   $e^+, \beta = 0.999, T = 1684.5 \text{ ns}$   $p, \beta = 0.957, T = 1760.2 \text{ ns}$

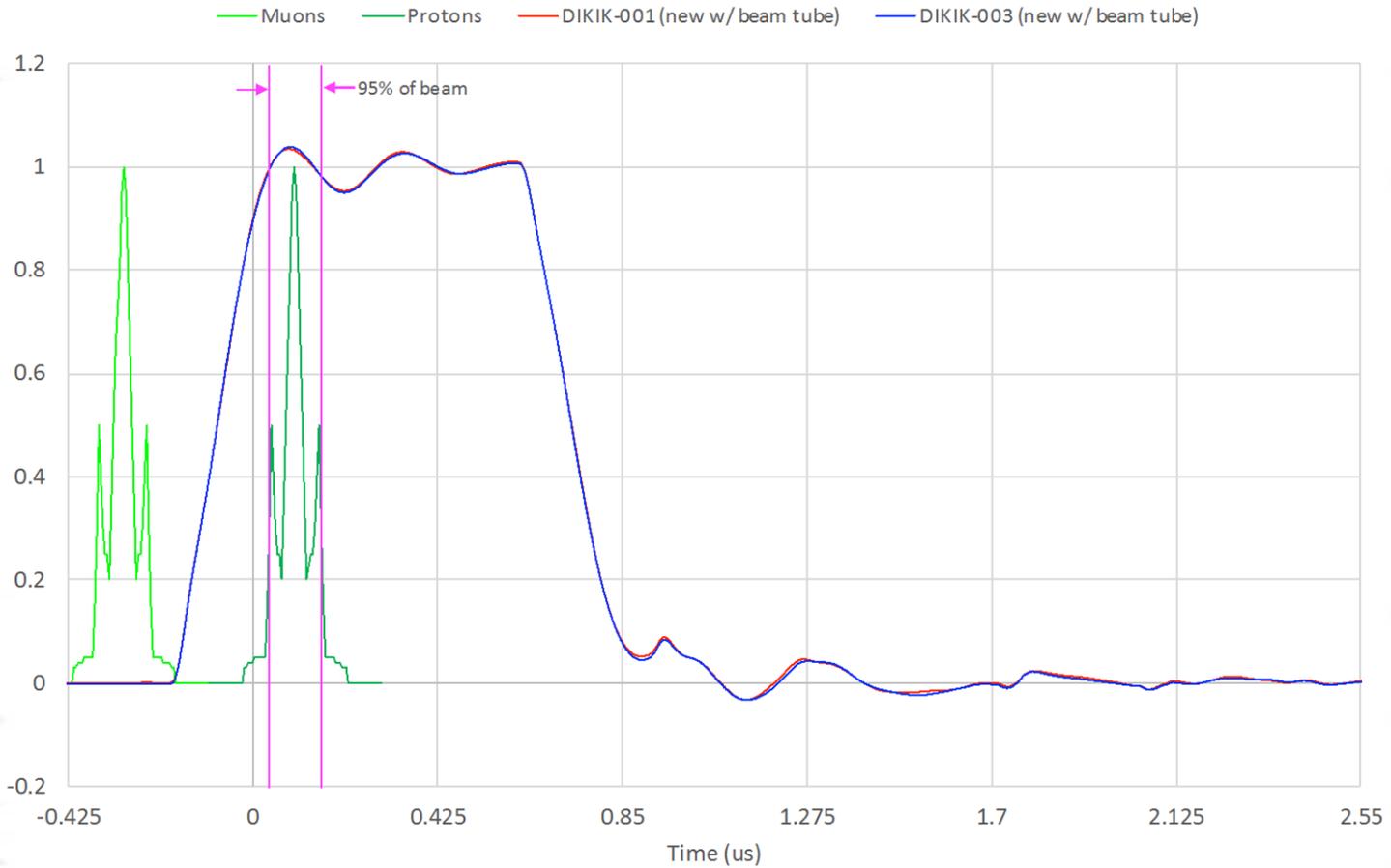


# Proton removal – 4 turns

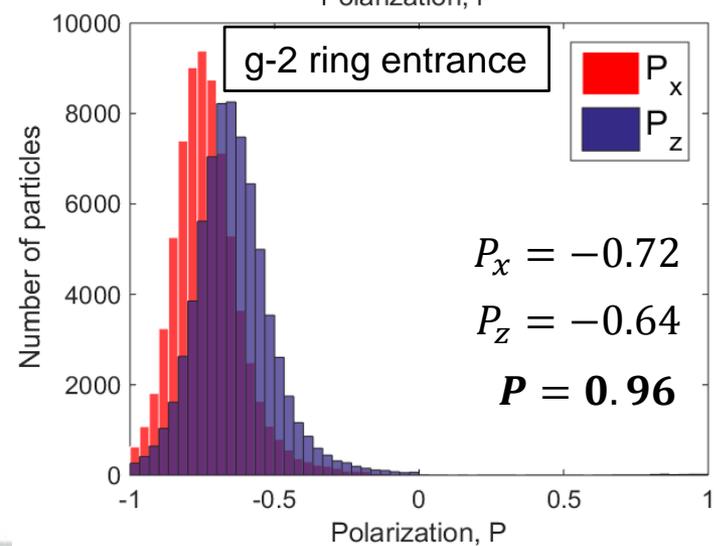
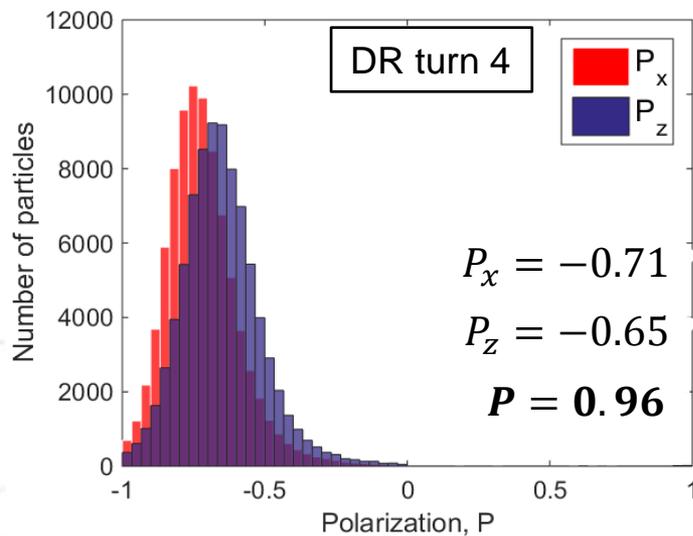
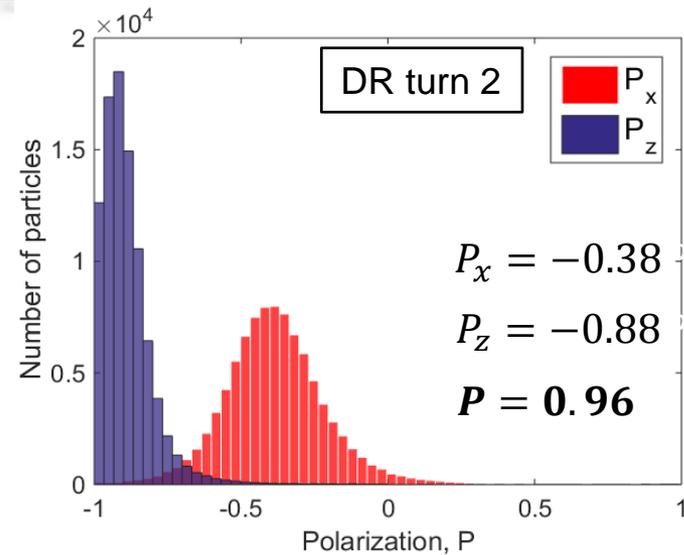
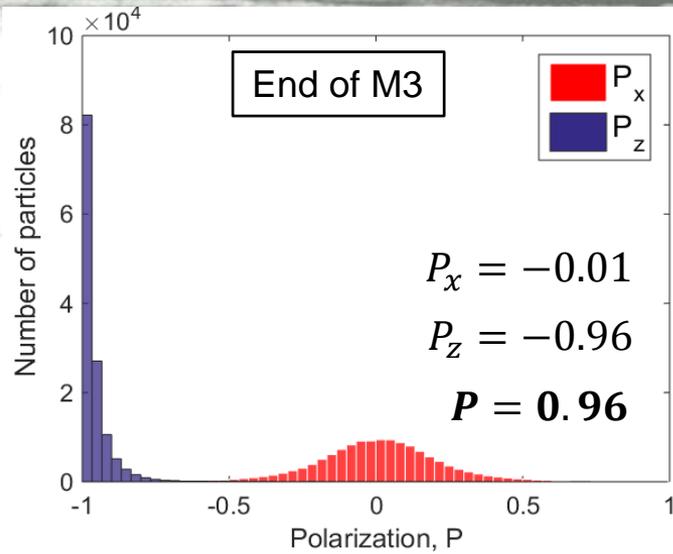
- Recall that kickers have a relative fast rise time ( $\sim 180$  ns)



# Proton removal – 5 turns



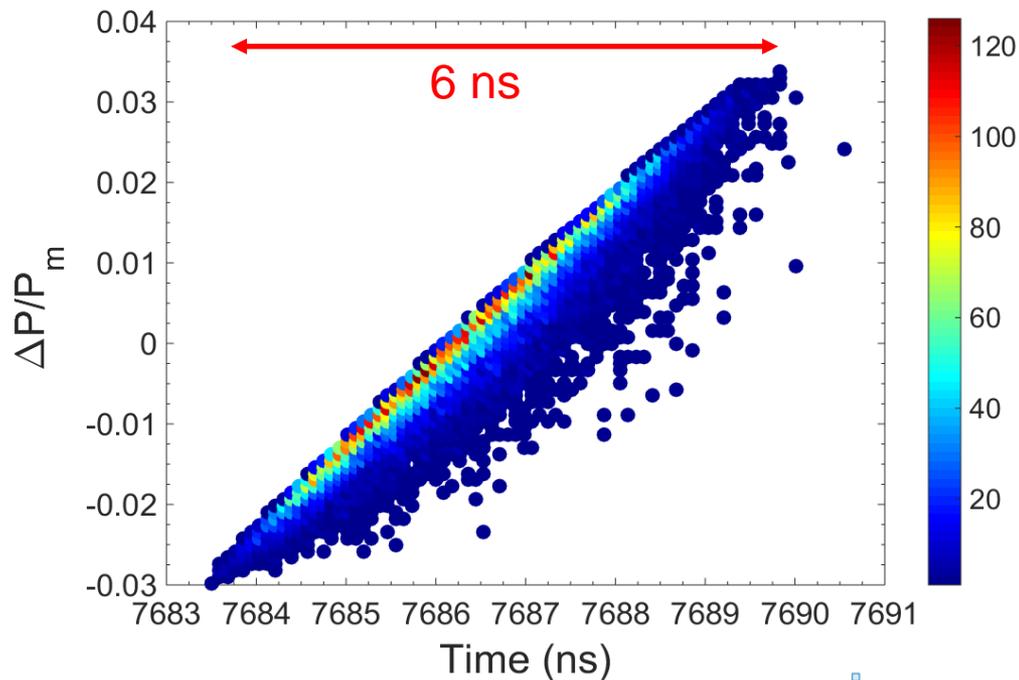
# Spin precession in the DR



# Momentum compaction

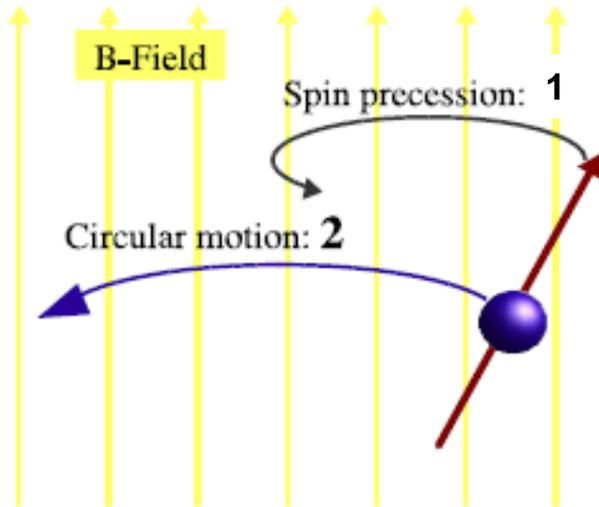
- In a circular machine, a nominal closed orbit is defined for a particle with a nominal momentum  $p_0$
- For a particle with momentum  $p_0 + \Delta p$  the trajectory is different from length  $L_0$  due to the dipole bending radius. We call  $\Delta L$  this extra length and define the momentum compaction as  $\alpha_c = \frac{\Delta L/L_0}{\Delta p/p_0}$
- Time for one turn:  $\tau = \frac{L}{v}$  or  $\frac{\Delta\tau}{\tau} = \frac{\Delta L}{L} - \frac{\Delta v}{v}$
- But  $\frac{\Delta v}{v} = \frac{1}{\gamma^2} \frac{\Delta p}{p}$
- We can re-write the above equations as:  $\frac{\Delta\tau}{\tau} = \left( \alpha_c - \frac{1}{\gamma^2} \right) \frac{\Delta p}{p}$

# Error trigger: Path length



- Momentum compaction is a constant of the machine and for the DR  $a_c = 0.017$
- $$\Delta\tau = \frac{L}{c\beta} \left( a_c - \frac{1}{\gamma^2} \right) \frac{\Delta p}{p}$$
- For the DR,  $L = 505$  m,  $\Delta p/p = 1.5\%$ ,  $\gamma = 29.3$ ,
- After 4 turns:  $\Delta\tau = \sim 1.6$  ns

# Error trigger: Spin-mom. correlations

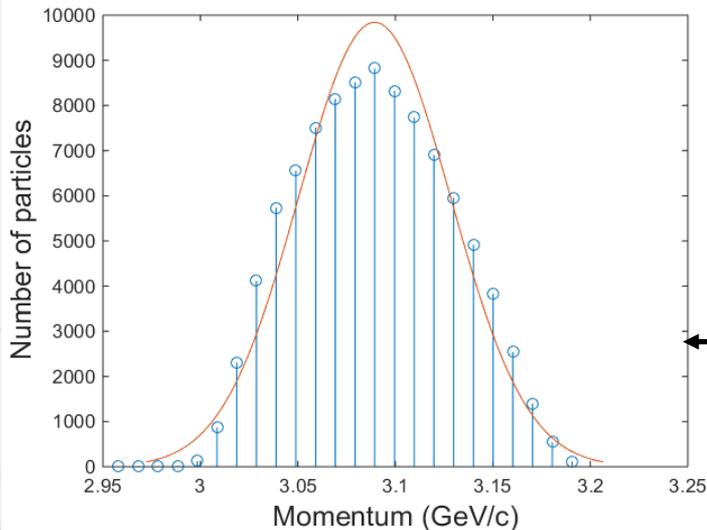


Spin precession relative to momentum:

$$\omega_a = a_\mu \frac{eB}{m_\mu c} = \gamma \alpha_\mu \omega_c$$

Precession after N turns:  $\varphi_a = 2\pi N \gamma a_\mu$

Slope of spin-momentum correlation:  $\frac{d\varphi_a}{dp} = \frac{2\pi N a_\mu}{m_\mu c}$



← Momentum spread after DR turn 1

# Spin-mom. correlations in the DR

$p_m : 3.094 \text{ GeV}/c$

