

# Proton and Ion Linear Accelerators

---

**Yuri Batygin<sup>1</sup>, Sergey Kurennoy<sup>1</sup>, Sebastian Szustkowski<sup>1</sup>,  
Salvador Sosa Guitron<sup>1</sup>, Vyacheslav Yakovlev<sup>2</sup>**

<sup>1</sup>Los Alamos National Laboratory

<sup>2</sup>Fermi National Accelerator Laboratory

**U.S. Particle Accelerator School**

**July 15 – July 26, 2024**





# Proton and Ion Linear Accelerators

## RF linacs: cavities, structures, EM design

Sergey Kurennoy, LANL

USPAS, July 19, 2024

Lecture 10

LA-UR-17-24573

# Content

- Why linacs & RF together?
- Reminder: basics of linacs
- RF cavities
- Accelerating structures: RFQ, DTL, CCL, etc.
- Electromagnetic (EM) design of accelerating structures. Tools.

Sources:

T.P. Wangler. *RF linear accelerators*, Wiley-VCH, 2<sup>nd</sup> Ed., 2008.

*Handbook of Accelerator Physics and Engineering*. 3<sup>rd</sup> Ed., Eds. A. Chao *et al.* World Scientific, 2023.

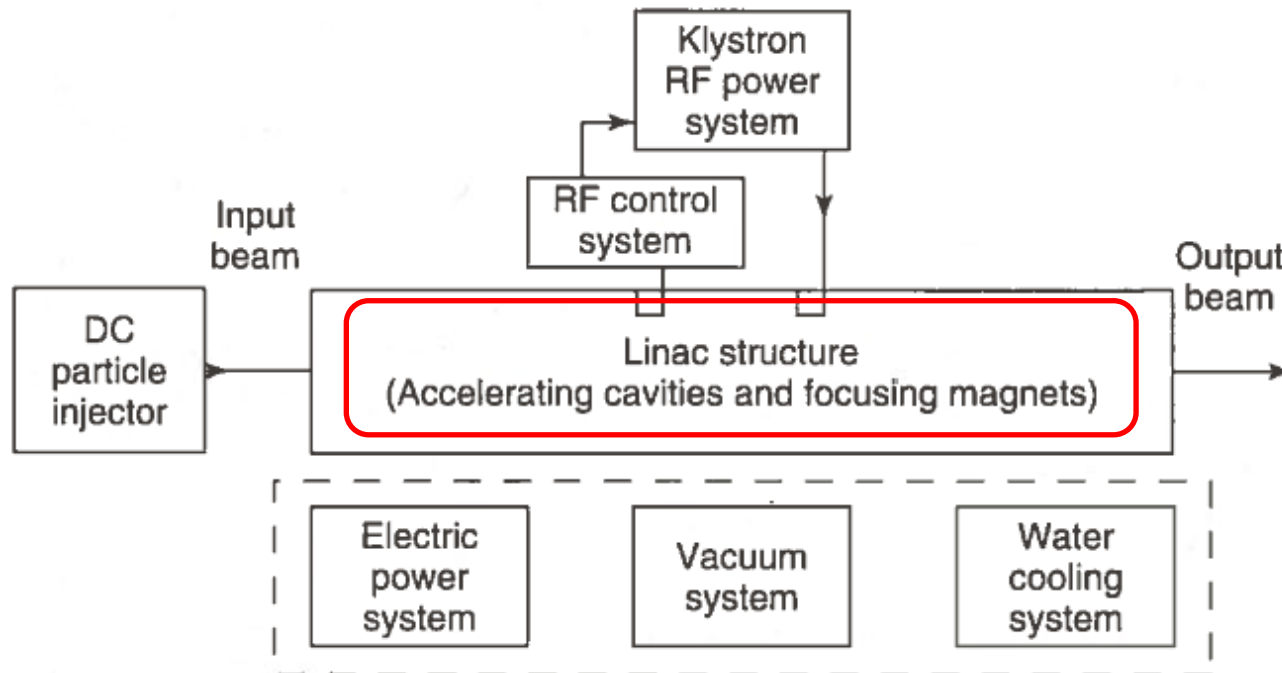


# Linacs

**Linear accelerator (linac)** – a device that accelerates charged particles in a straight line.

## Linac types:

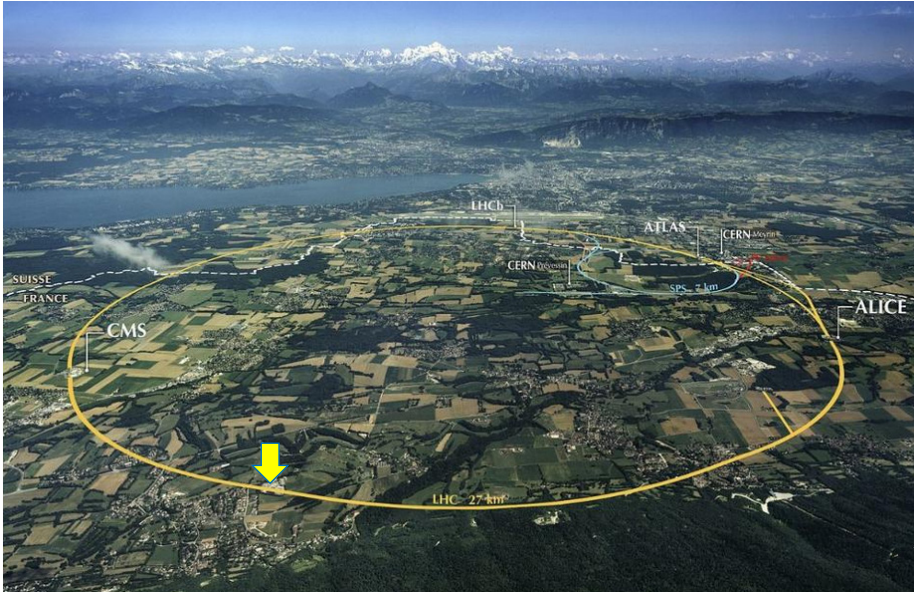
- **Electrostatic** – electric field is produced by a fixed voltage (e.g., old TV tubes)
- **Induction** – electric field is produced by changing magnetic flux
- **Radio-Frequency (RF)** – fields are produced by external sources of RF power



RF linac schematics



# Why linacs & RF together?



**LHC RF section = 2 short linacs!**

**SLAC** – electron linac (1968): 3 km, & RF acceleration “section” ~3 km.

**240** 2856-MHz klystrons (design - 960), each with 50-MW peak power (x2 with pulse compression), provide total voltage up to ~50 GV (SLC, 1989).

**LHC** – circular p-p collider (2008): 27 km, but RF acceleration section <100 m. 8 SC 400.8-MHz RF cavities per ring; 8-16 MV; each cavity is only ~2 m long and powered by one klystron (**16** klystrons total).



# Why linacs & RF together?

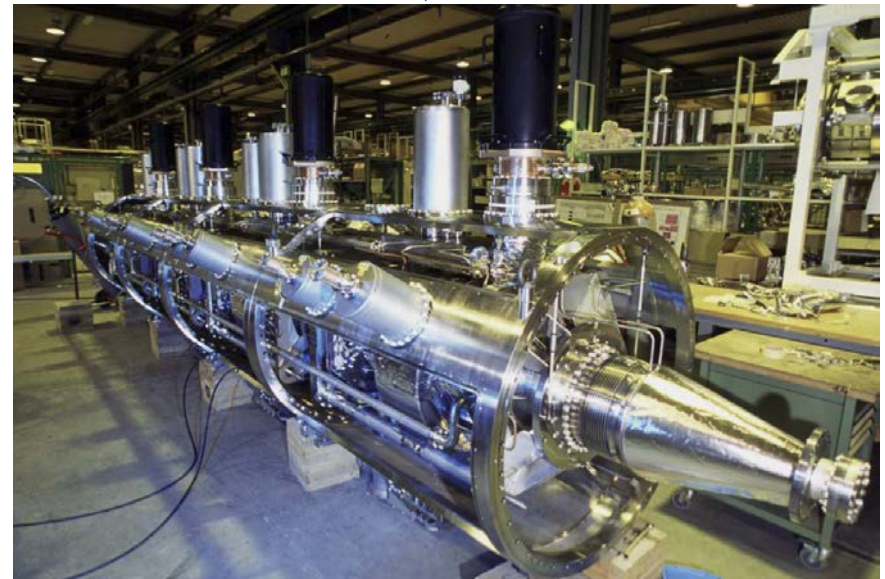


← **SLAC** klystron gallery

**SLAC** linac (30' below)

**960** traveling-wave structures (x3m)

**LHC** 4 RF cavities in cryo-module



# Why linacs & RF together?

LANSCE (LAMPF) linac (1972)



**800 m, 800 MeV**  
Protons (p) and  
hydrogen ions (H<sup>-</sup>)



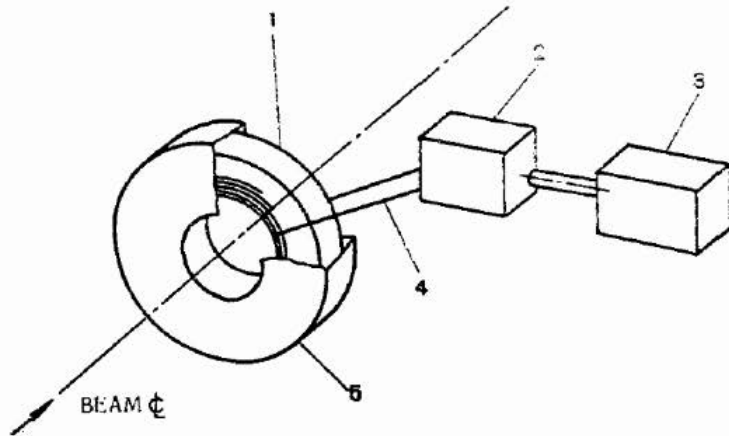
## Drift-tube linac (DTL)

62 m, 0.75-100 MeV  
 $\beta = v/c = 0.04-0.43$   
4 201.25-MHz tubes ( $\leq 3$  MW)

## Coupled-cavity linac (CCL)

731 m, 100-800 MeV  
 $\beta = v/c = 0.43-0.84$   
44 805-MHz klystrons (1 MW)

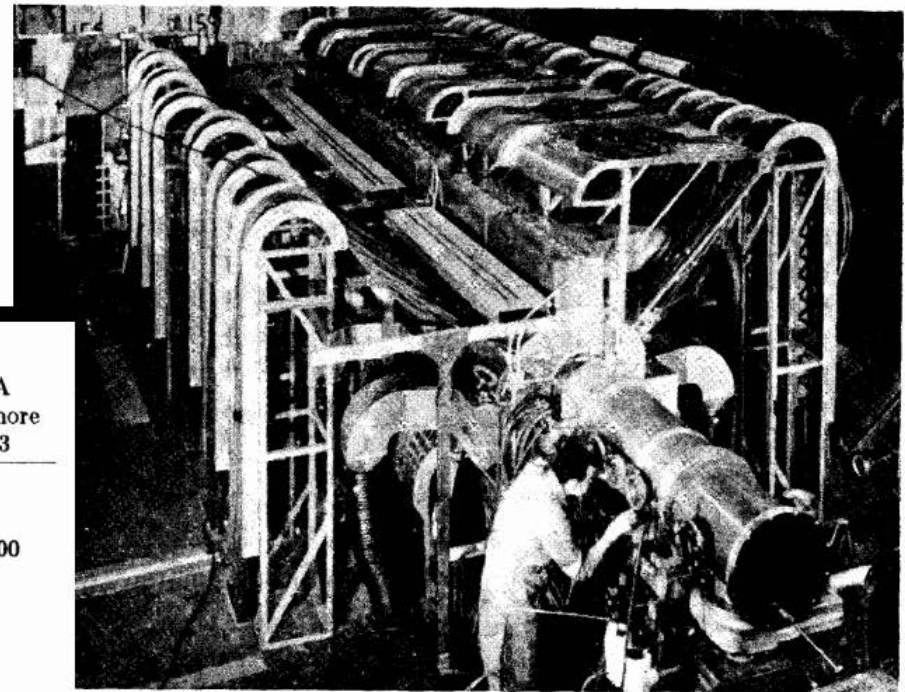
# Induction Accelerator



$$\oint \vec{E} \cdot d\vec{l} = -\frac{1}{c} \int_s \frac{d\vec{B}}{dt} \cdot d\vec{s},$$

Fig. 1. Induction accelerator principle:

1 — laminated iron core; 2 — switch; 3 — pulse forming network; 4 — primary loop; 5 — secondary (case).



Overhead view of the Astron accelerator as it appeared when first put into operation.

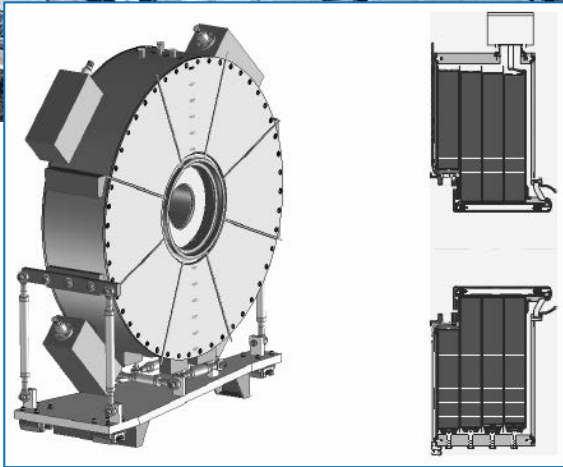
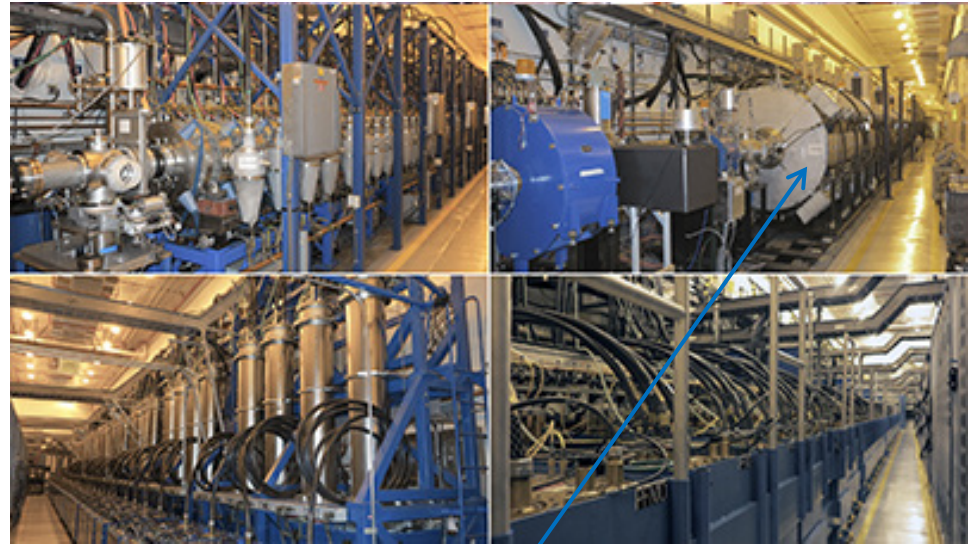
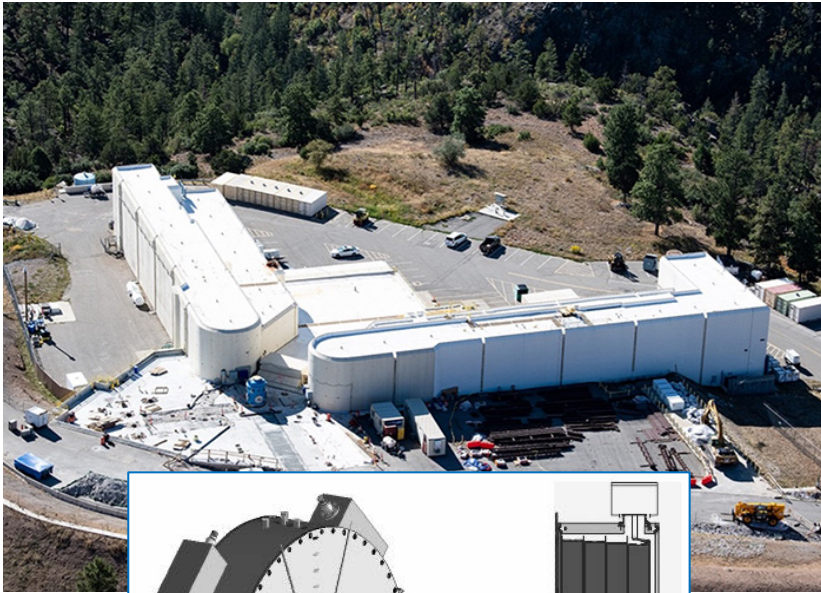
Table 3. Parameters for Typical Induction Accelerators

Accelerator	Astron Injector Livermore 1963	ERA Injector Berkeley 1971	NEP 2 Injector Dubna 1971	ATA Livermore 1983
Kinetic energy, MeV	3.7	4.0	30	50
Beam current on target, A	350	900	250	10,000
Pulse duration, ns	300	2-45	500	50
Pulse energy, kJ	0.4	0.1	3.8	25
Rep rate, pps	0-60	0-5	50	5
Number of switch modules	300	17	750	200





# DARHT at LANL – two linear induction accelerators



Induction cells of Axis 2:

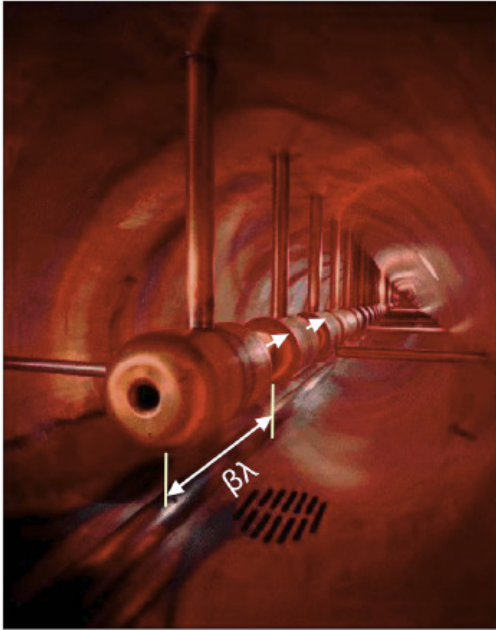
Beam pipe diameter 12" (8 cells) and 10" (66 cells)

## Dual-Axis Radiographic Hydrodynamic Test (DARHT) facility:

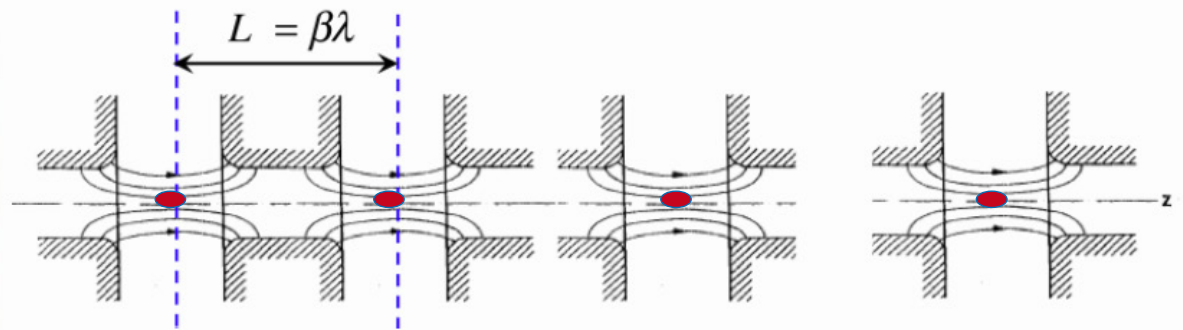
- Axis 1 (1999): 60-ns pulse, **2 kA**, 20 MeV e-beam → high-Z target → X-rays (64 cells)
- Axis 2 (2008): 1.6- $\mu$ s long flat-top pulse (4 short pieces cut), **2 kA**, 17 MeV (74 cells)



# Resonance acceleration principle



Alvarez accelerating structure



Field distribution in RF structure:  $E_z(z,r,t) = E_g(z,r)\cos(\omega t)$

Time of flight between RF gaps  $t_{flight} = T_{RF\ period} = \frac{1}{f}$

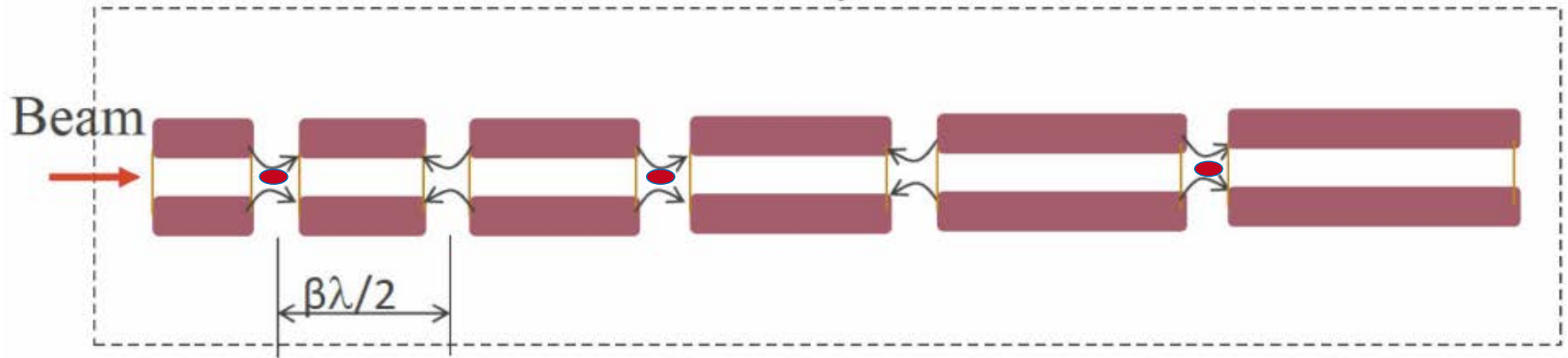
Distance between RF gaps  $L = n\beta c T_{RF\ period} = n\beta\lambda$

RF Frequency  $f$

- Synchronism between the accelerating field and particles is due to the linac spatial structure: particles arrive at the gaps when the electric field is in the accelerating phase, and are hidden from the field inside drift tubes during the decelerating phase.
- The above example is a 0-mode accelerating structure (Alvarez DTL): the gap fields work in phase,  $\Delta\varphi = 0$ . BTW,  $t_{flight} = mT_{RF}$ , where  $m = 2,3,\dots$  will work too ( $m\beta\lambda$ -mode).
- Note: all these tricks are for ions at  $\beta \ll 1$ ; for electrons, things are much simpler.



# Resonance acceleration: $\pi$ -mode

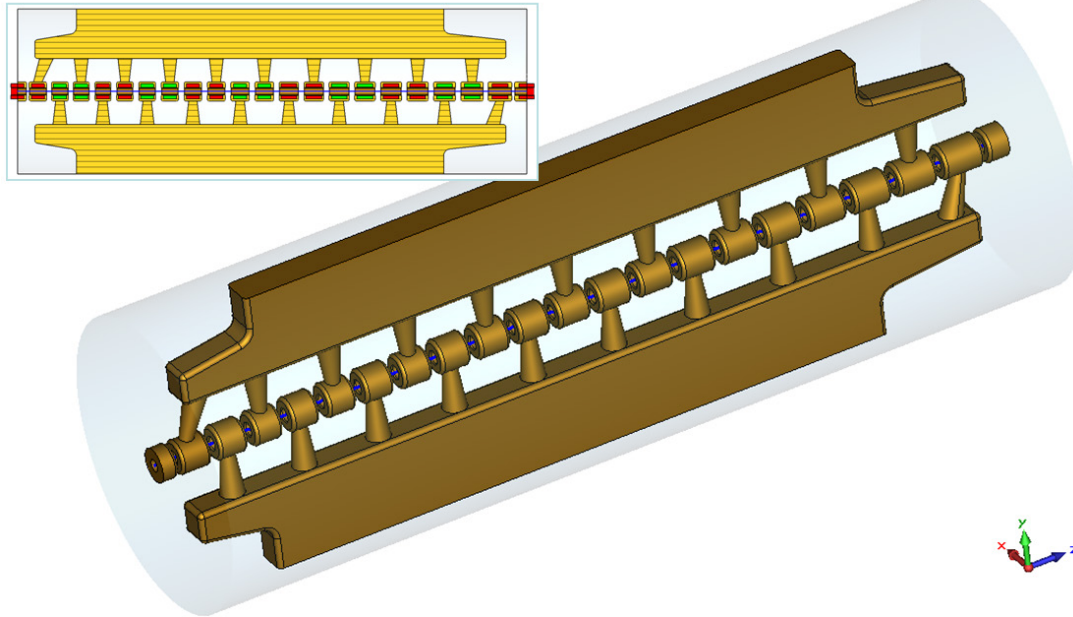


Accelerating structure with  $\pi$  - type standing wave.

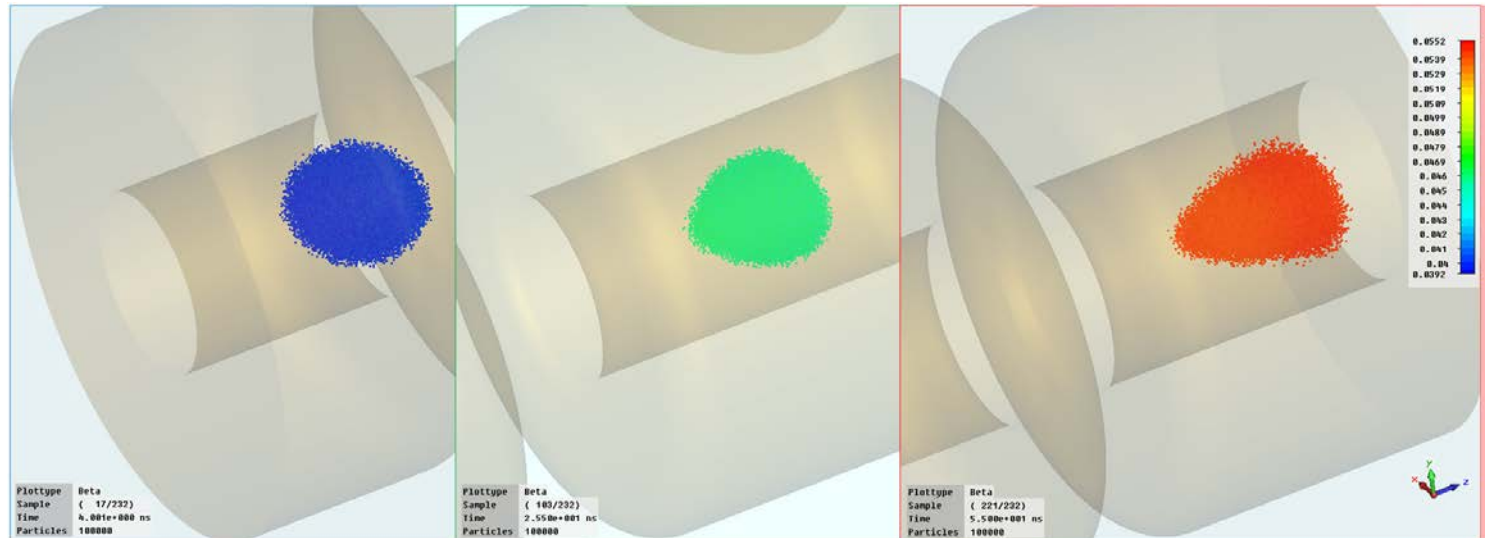
- This is a  $\pi$ -mode accelerating structure (e.g., Wideroe DTL): the fields in the adjacent gaps are in opposite phases,  $\Delta\varphi = \pi$ .
- Particles accelerated in a gap should arrive to the next gap in one half of the RF period (strictly speaking,  $(n+1/2)T_{\text{RF}}$ ) so that its electric field changes to the accelerating phase.
- Still there is a “synchronism” between the RF field and the linac spatial structure.
- In principle, one can accelerate simultaneously a beam of opposite charge (with the same particle mass) with its bunches shifted by  $\pi$  in phase.



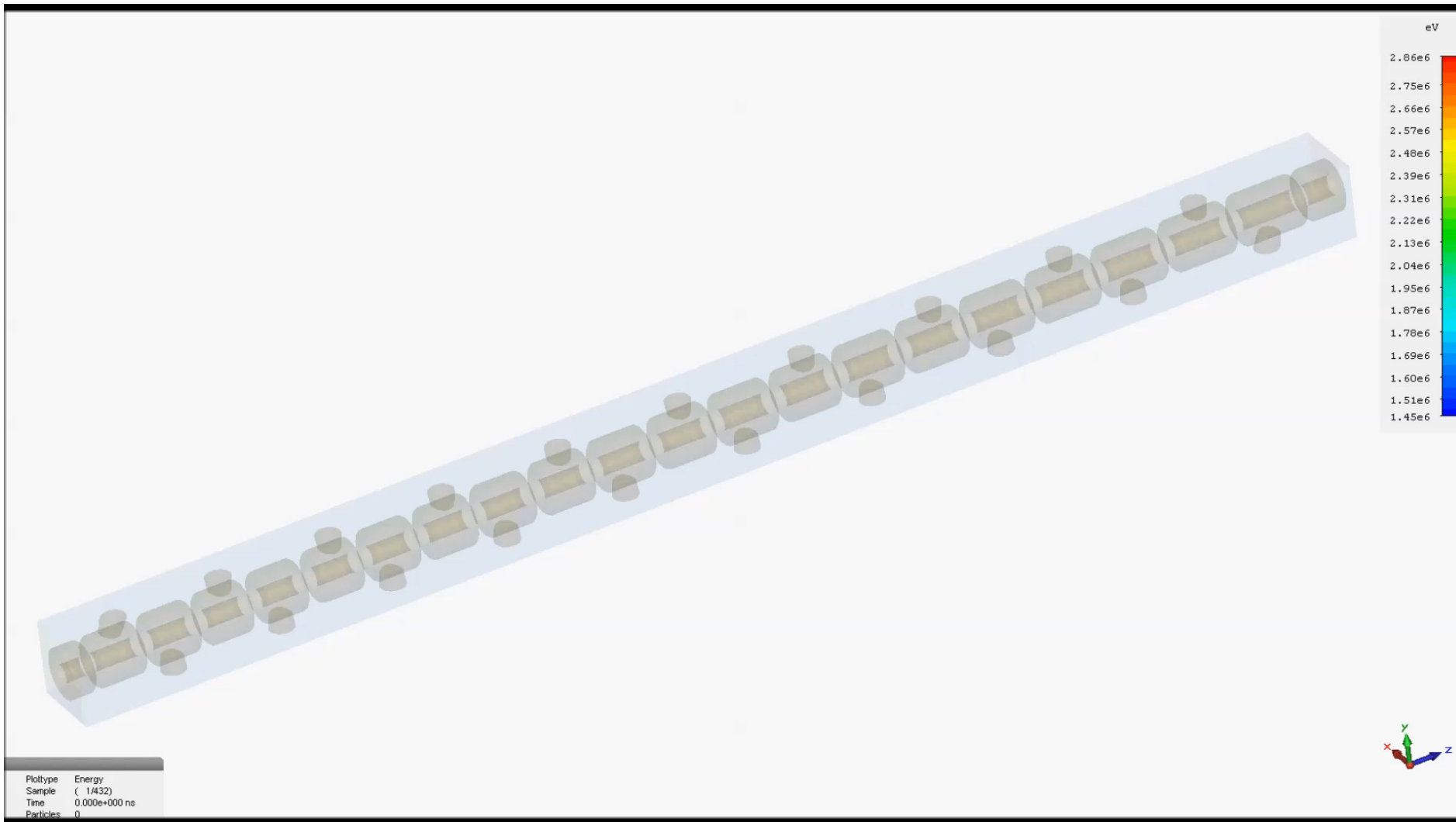
# Example: Inter-digital H-mode (IH) structure



IH-PMQ structure for deuterons from  $\beta=v/c=0.04$  to  $0.055$ :  
 $f=201.25$  MHz,  $I=50$  mA  
 $L=73.5$  cm,  $a=0.5-0.55$  cm.  
CST Studio simulations: RF fields (MWS), PM quadrupole fields (EMS), and beam dynamics (Particle Studio).



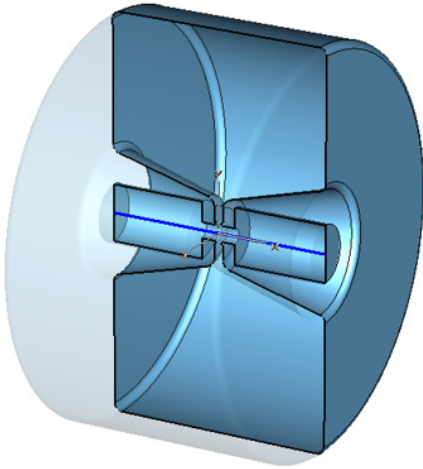
# Inter-digital H-mode (IH) structure



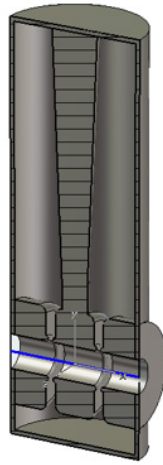
10 bunches of 10K particles ( $d$ ) are accelerated in the cavity



# Buncher cavities

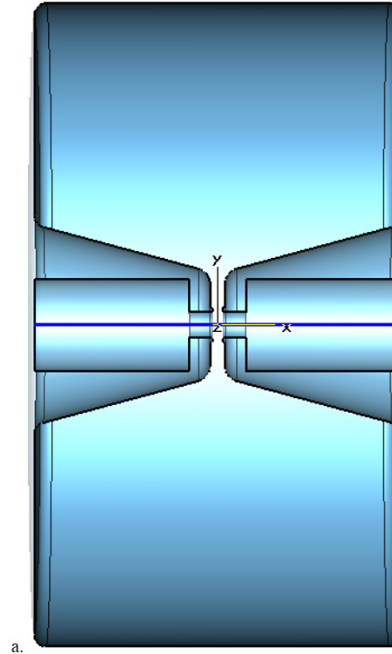


a.

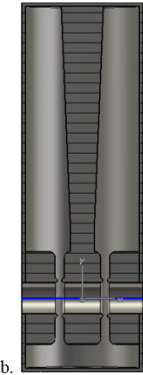


b.

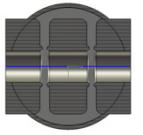
Two buncher cavities: (a) re-entrant and (b) coaxial quarter-wave ( $\lambda/4$ ) types. Right – on the same scale.



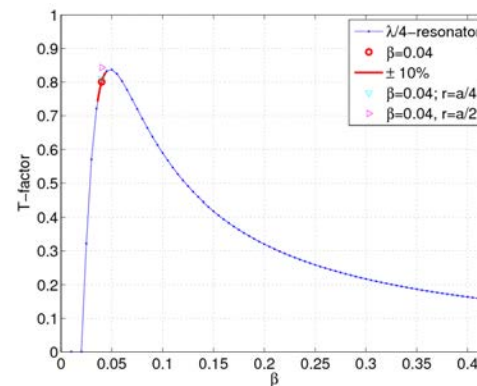
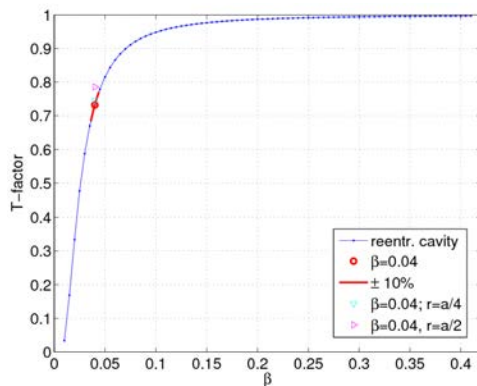
a.



b.



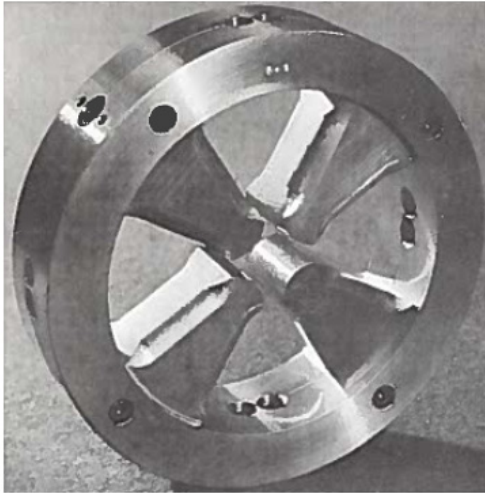
c.



Transit-time factors for two cavities vs velocity



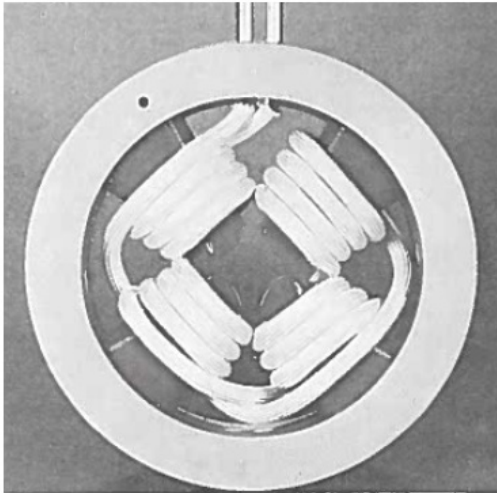
# Linac electromagnetic quadrupoles – LANSCE DTL



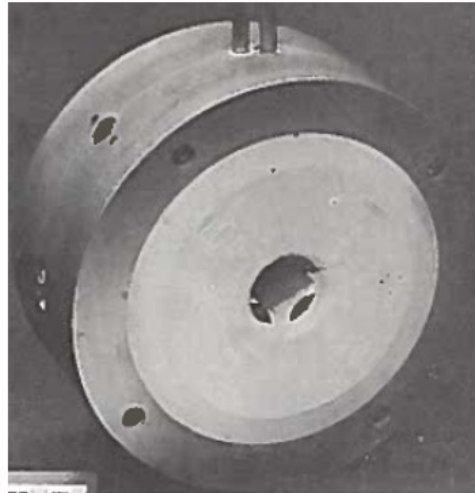
(a)



(b)



(c)



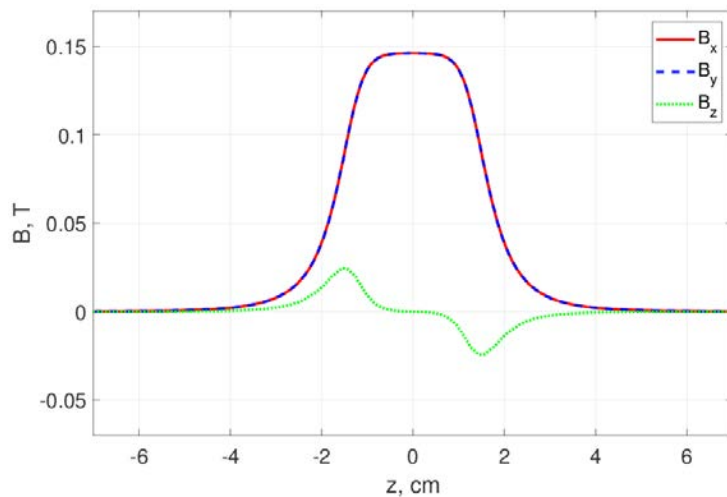
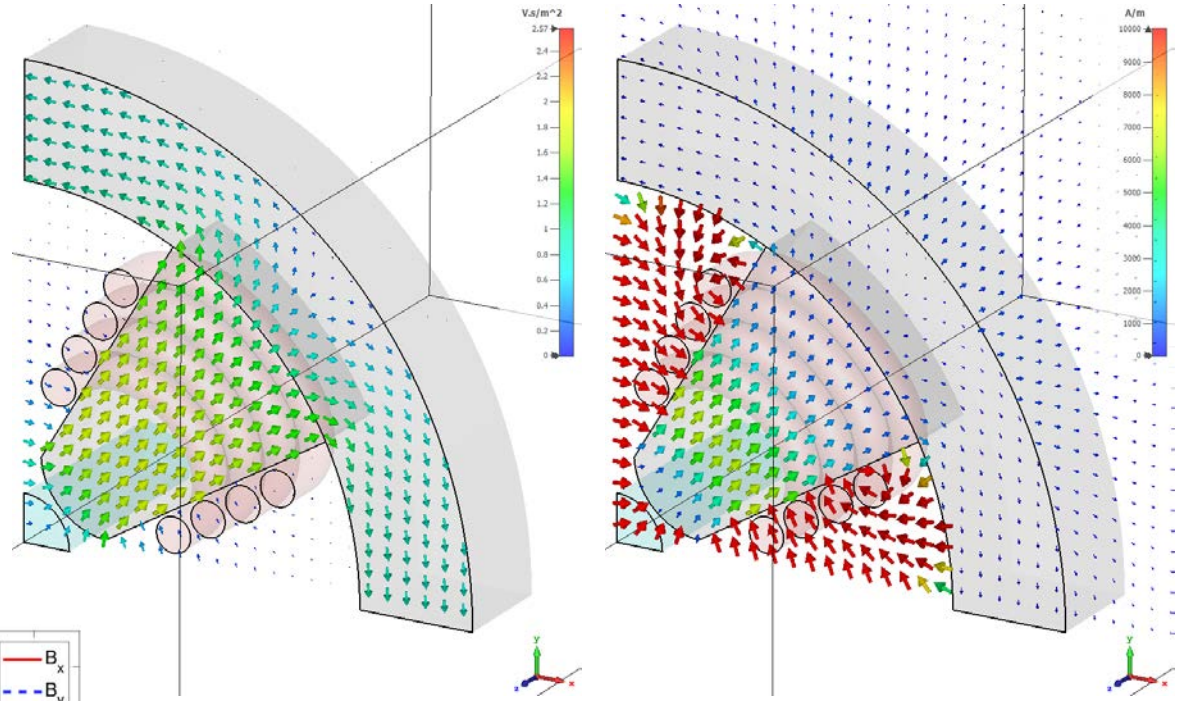
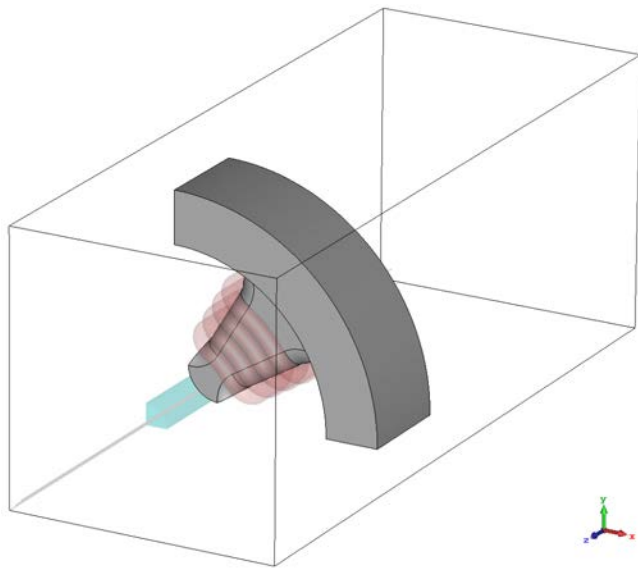
(d)

DTL tank 1 EM quadrupoles are installed inside drift tubes:  
(a) yoke and pole pieces (iron);  
(b) current coil (copper, hollow);  
(c) coil assembled with iron;  
(d) quadrupole fully assembled.

EM quadrupole gradients are adjusted by changing current:  
gradient  $G=73.5$  T/m at  $\sim 562$  A.  
 $GL = 2.59$  T in Q1.



# LANSCCE DTL EM quadrupoles – material replacement

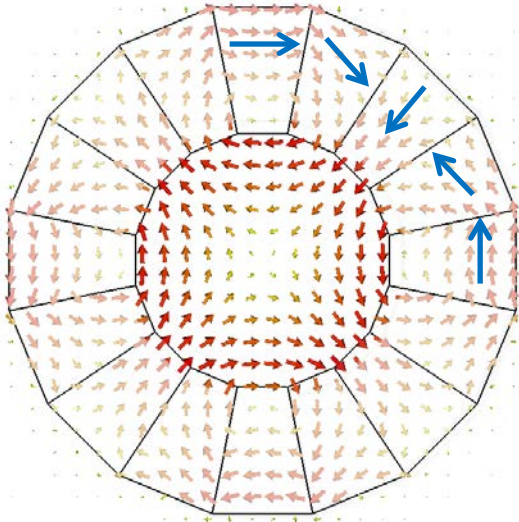


The design strength in Q1 with C1006 steel is achieved at higher current,  $\sim 586$  A.





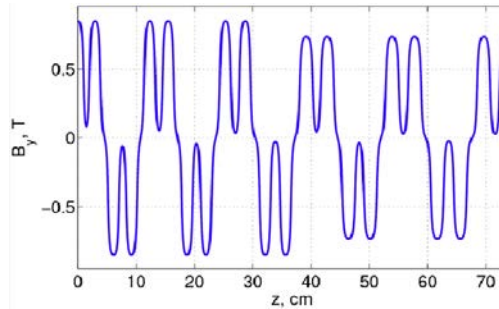
# Permanent-magnet quadrupoles



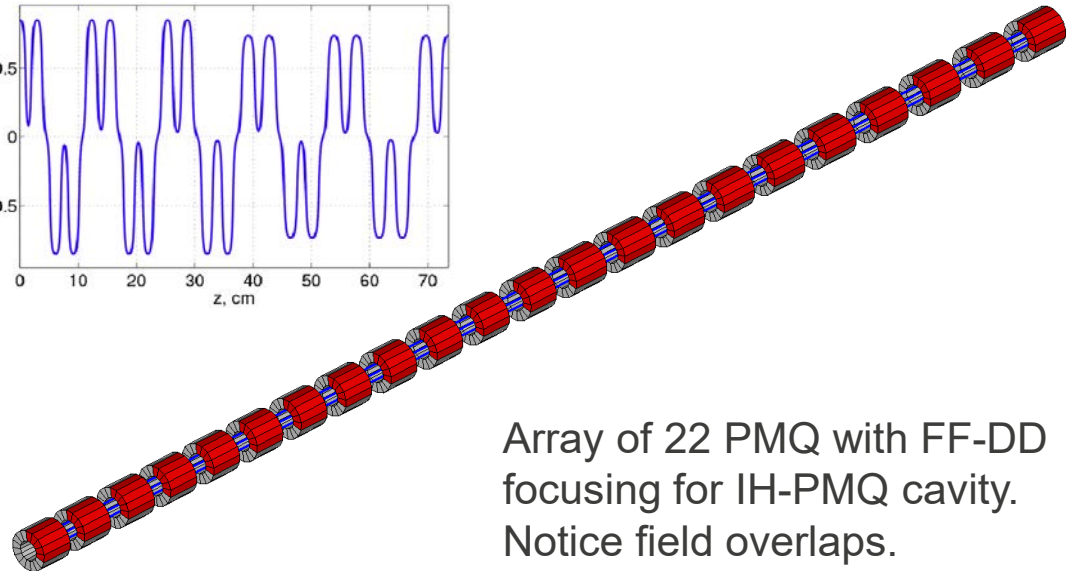
Magnetic field in the cross section of  $M=16$  PMQ calculated with CST EM Studio. For  $r_{in} = 5.5$  mm,  $r_{out} = 11$  mm,  $G = 170$  T/m; length  $L=19$  mm.

Permanent-magnet quadrupoles are assembled from segments of PM materials, usually SmCo or NdFeB, with properly oriented magnetization vectors in segments. The gradient of such a quadrupole with  $M = 16$  segments (typically  $M = 12, 16$ ), the remnant field  $B_r$  ( $\sim 1$  T), and radii  $r_{in}$  and  $r_{out}$ , is

$$G = 2B_r \left( \frac{1}{r_{in}} - \frac{1}{r_{out}} \right) K_2; \quad K_2 = \cos^2 \frac{\pi}{M} \frac{\sin(2\pi / M)}{2\pi / M} \cong 0.937.$$



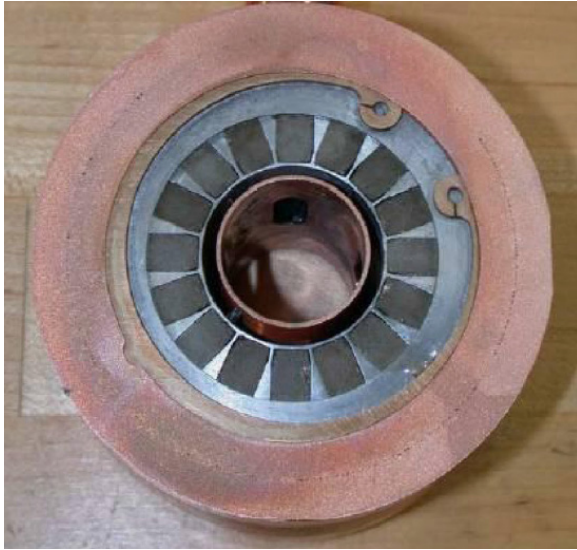
Permanent-magnet quadrupoles are installed in the DTL of the Spallation Neutron Source (SNS).



Array of 22 PMQ with FF-DD focusing for IH-PMQ cavity. Notice field overlaps.



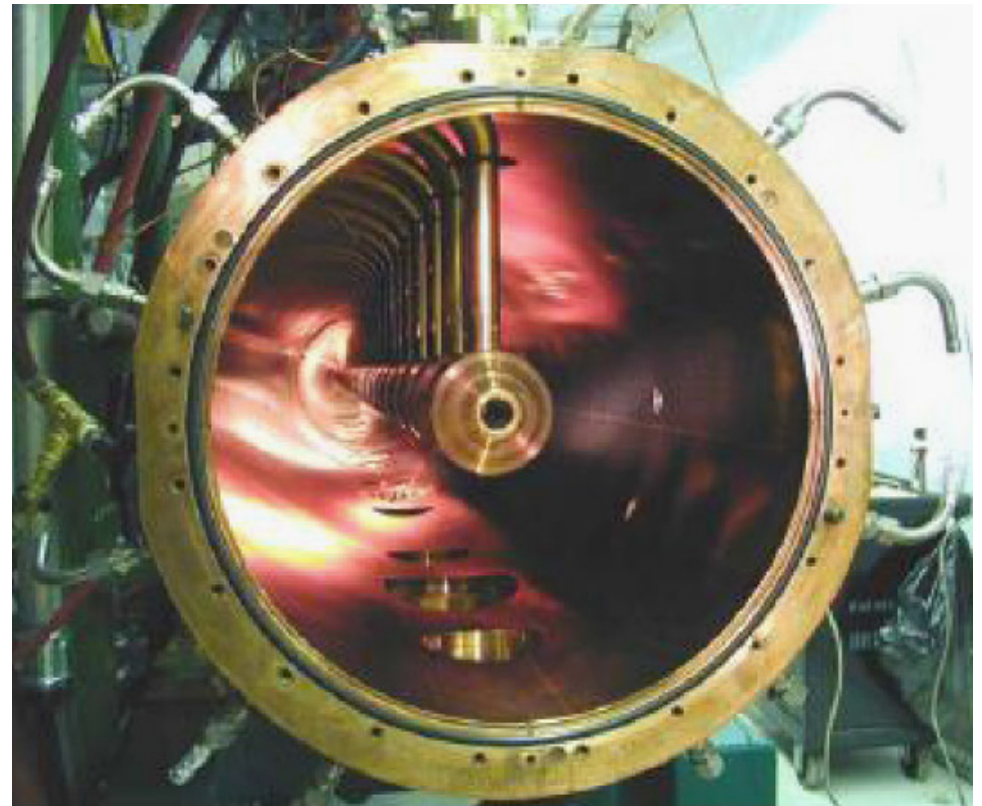
# Permanent-magnet quadrupoles in SNS



Cut of the SNS DTL drift tube with PMQ. The bore aperture diameter is 2.5 cm.

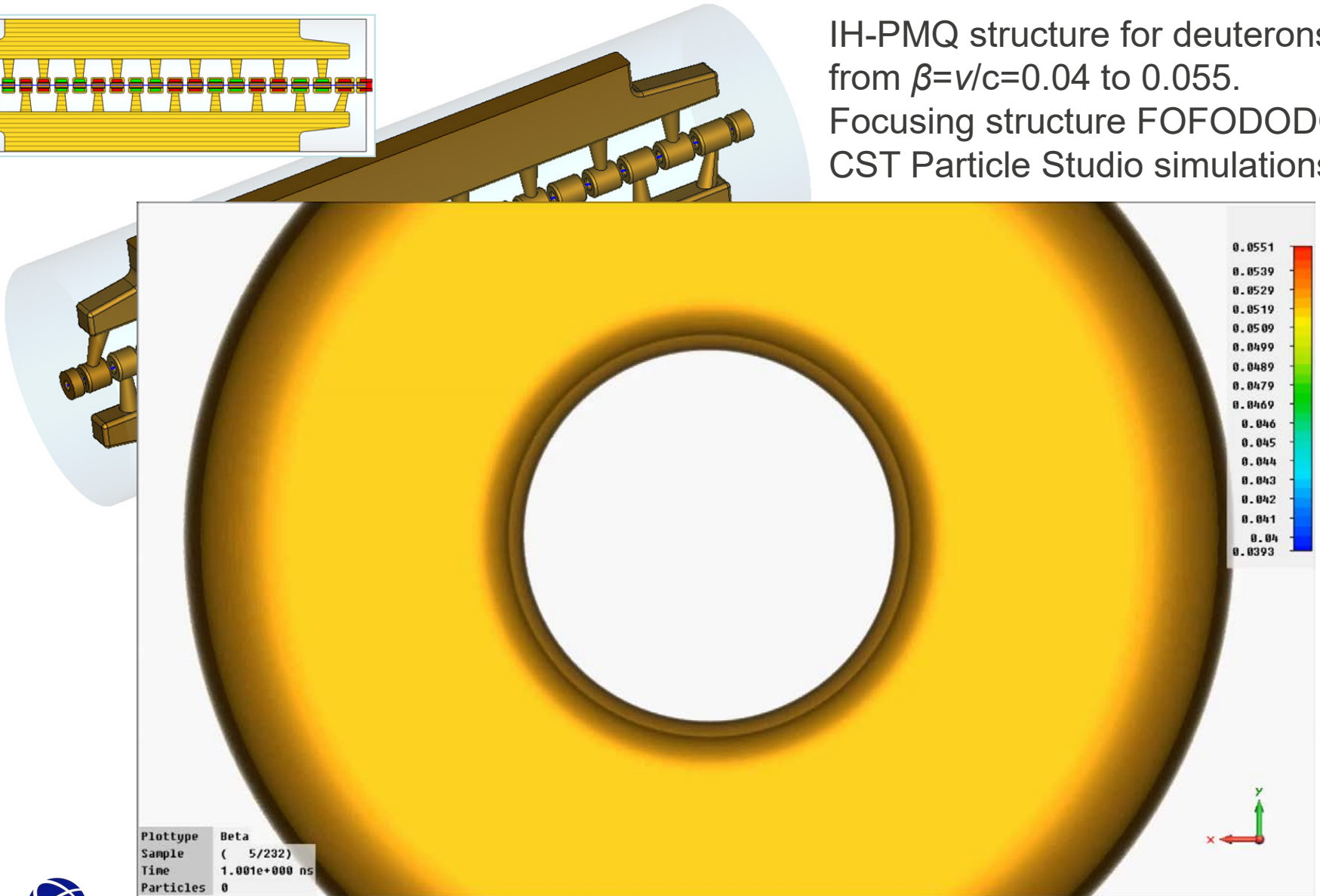
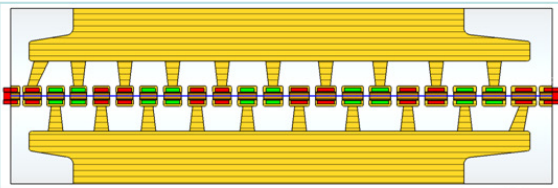
SNS DTL tank 3 with PMQs inside drift tubes (DTs). Some DTs contain beam position monitors (BPM). FFODDO focusing structure.

Permanent-magnet quadrupoles (PMQ) are installed in the DTL of the Spallation Neutron Source (SNS, Oak Ridge). Now PMQ are also installed in Linac 4 at CERN.



# Example: Inter-digital H-mode (IH) structure with PMQ

IH-PMQ structure for deuterons from  $\beta=v/c=0.04$  to 0.055.  
Focusing structure FOFODODO.  
CST Particle Studio simulations.



Plotype	Beta
Sample	( 5/232)
Time	1.001e+000 ns
Particles	0



# Summary 1

- Linacs and RF are closely related.
- In ion linacs synchronism between accelerated particles and RF is achieved by designing a spatial structure with  $L_c \sim \beta\lambda$ . Fixed velocity profile! Independent-cavity structures can also be used, e.g., in heavy-ion linacs, for more flexibility.
- Longitudinal and transverse beam focusing cannot be achieved simultaneously in RF fields. External transverse beam focusing is usually added.



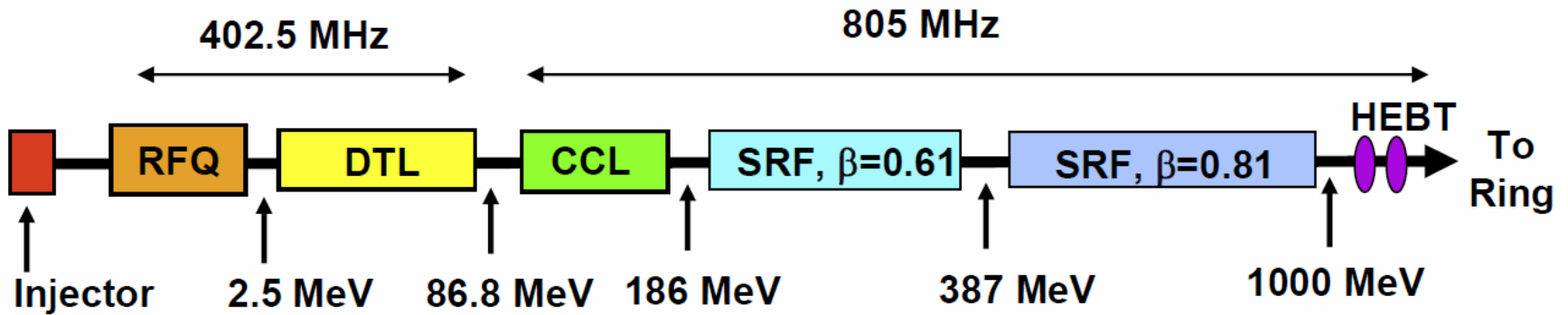
# Linac parts

Linac scheme: particle source + accelerating structure(s)



Electron linacs: electron gun + linac (TW or SW  $\beta=1$  structure); with some tricks.

Ion linacs: ion source (injector) + various structures for different values of  $\beta$ .

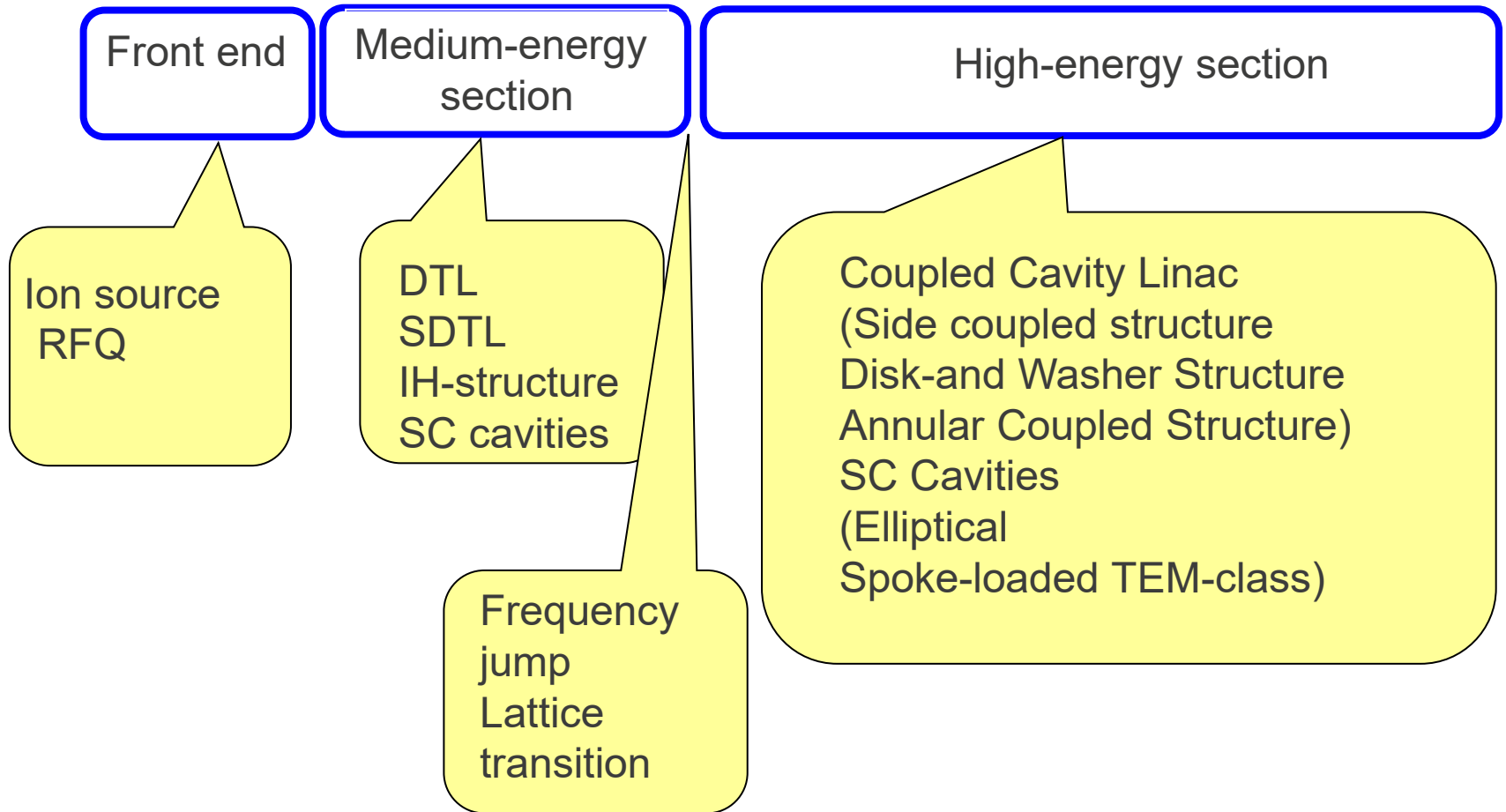


## Scheme of SNS linac:

- RFQ = RF Quadrupole accelerator
- DTL = Drift-Tube Linac
- CCL = Coupled-Cavity Linac
- SRF = SC RF linac
- HEBT = High-Energy Beam Transport



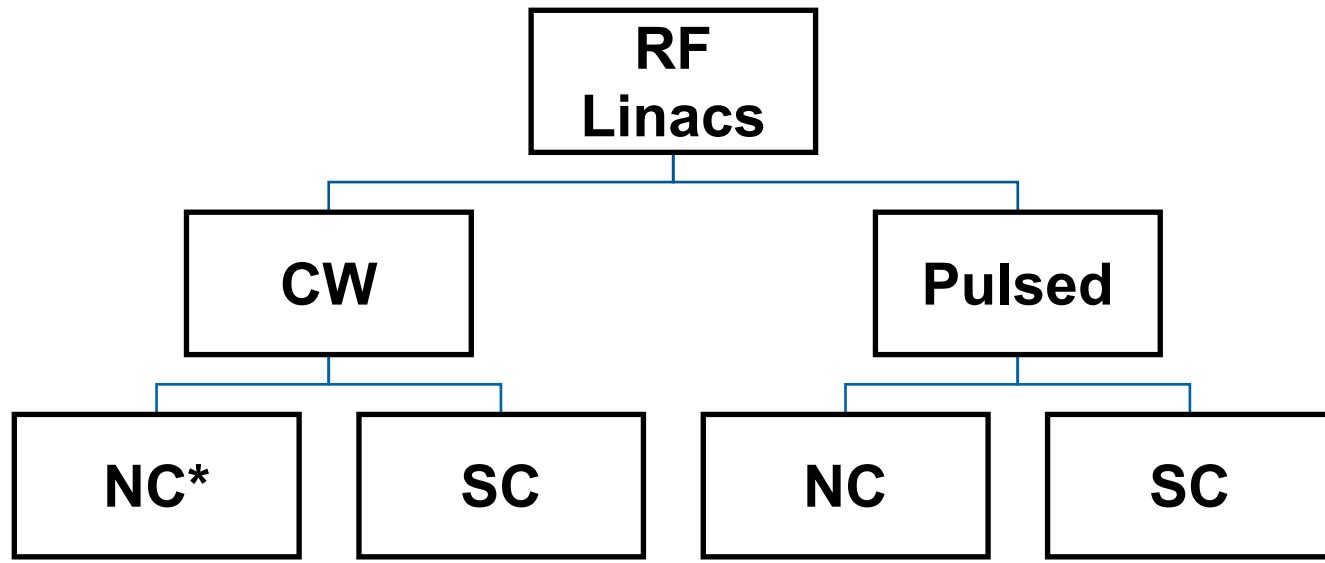
# Typical RF linac structures



From P. Ostroumov (2012)



# RF Linac Types



**ISAC-I**  
**RIKEN inj.**  
**LEDA RFQ**  
**SARAF RFQ**

\*Low-energy,  
 several MeV/u  
 Heavy-ions

**ATLAS**  
**ISAC-II**  
**INFN**  
**SARAF**  
**SPIRAL-2**  
**FRIB**  
 Project X  
 EURISOL  
 ADS projects

**LANSCE**  
**Synchrotron**  
**Injectors**  
 (FNAL, KEK,  
**CERN, IHEP....)**  
**MMF (Moscow)**  
**SNS**

**SNS**  
 CERN-SPL  
 ESS

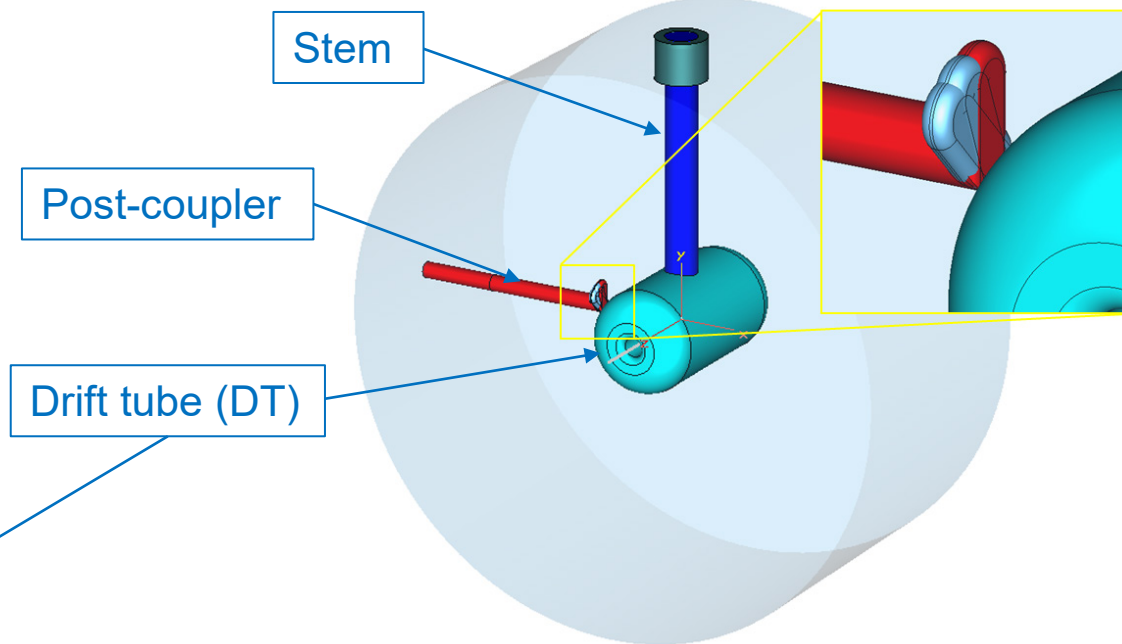
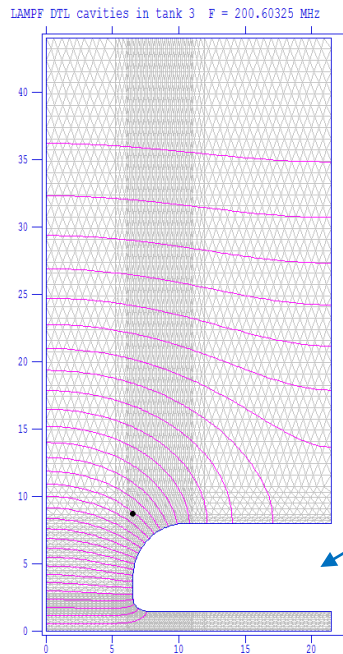
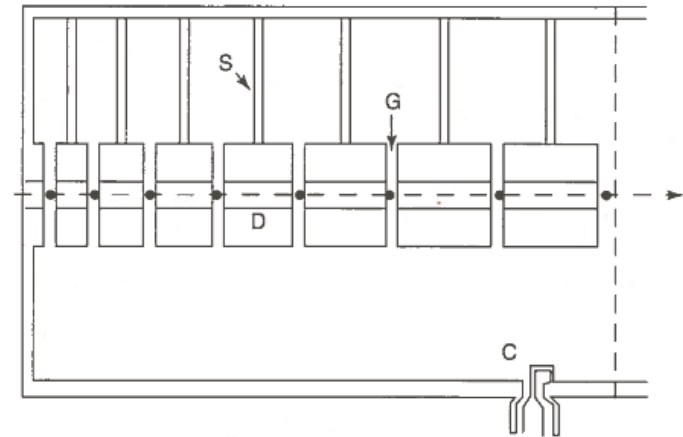
From P. Ostroumov (2012)



# Drift-Tube Linac (DTL)

Alvarez DTL structure (1946):

- $TM_{010}$ -like mode ( $E_z$ ,  $E_r$ ,  $B_\theta$ )
- DTs hide the beam bunches during the decelerating phase of electric field
- cell length  $L_c = \beta\lambda$
- long cavities (tanks) are more efficient
- field stabilization by post-couplers in long tanks

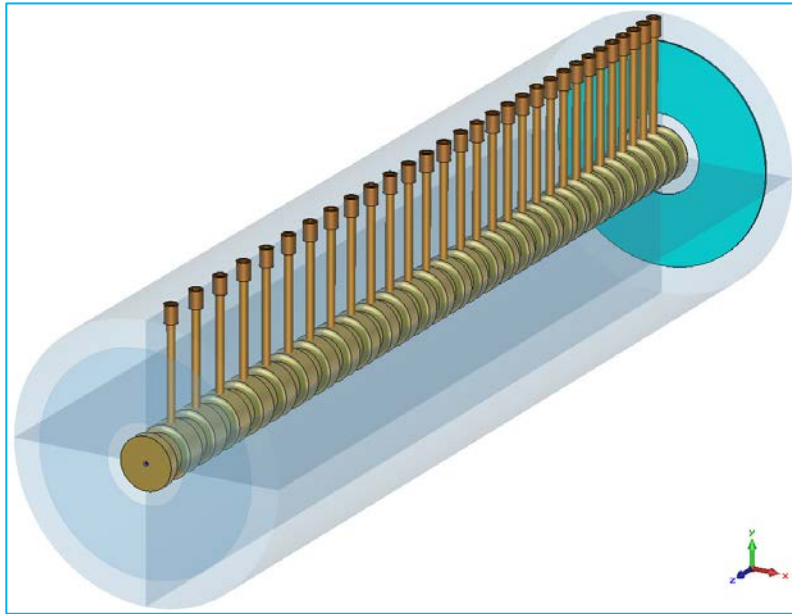


Electric field lines (Superfish, left) and CST model of cell 98 (1<sup>st</sup> in T3) of the LANSCE DTL.





# LANSCE DTL (1968)



CST model of Tank 1

Usually, the average longitudinal field  $E_0$  is constant (flat) along the tank length but in T1 it is ramped (increasing). Tilt tuners.

Table 4.1 DTL parameters for the LANSCE proton accelerator.

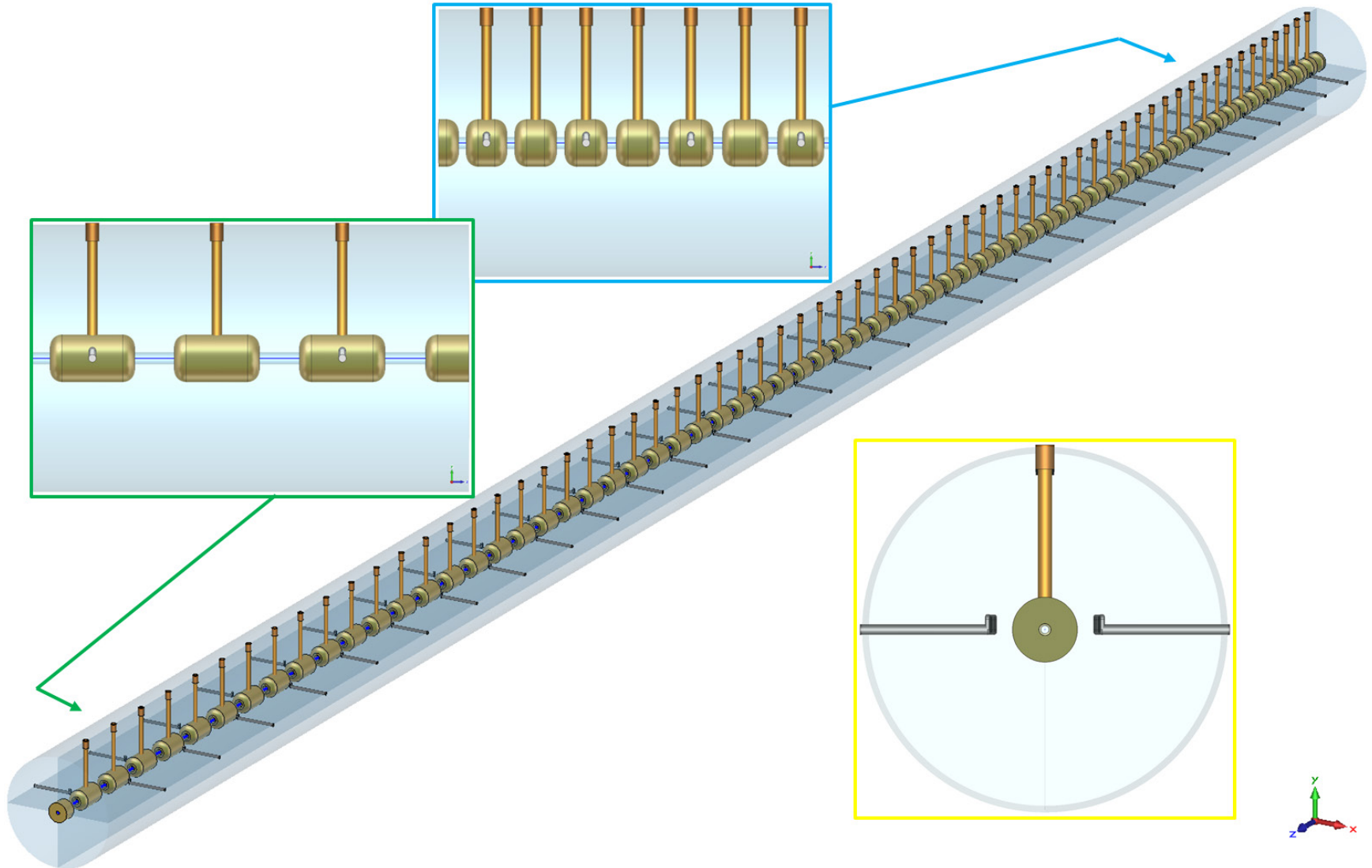
	Tank 1	Tank 2	Tank 3	Tank 4		
Cell number	1 to 31	32 to 59	60 to 97	98 to 135	136 to 165	
Energy in (MeV) $\beta$	0.75	0.04	5.39	0.107	41.33	72.72
Energy out (MeV) $\beta$	5.39	41.33	0.287	72.72	0.37	100.00
Energy gain (MeV)	4.64	35.94	31.39	27.28		
Tank length (cm)	326.0	1968.8	1875.0	1792.0		
Tank diameter (cm)	94.0	90.0	88.0	88.0		
Drift-tube diameter (cm)	18.0	16.0	16.0	16.0		
Drift-tube corner radius (cm)	2.0	4.0	4.0	4.0		
Bore radius (cm)	0.75	1.0	1.5	1.5	1.5	
Bore corner radius (cm)	0.5	1.0	1.0	1.0	1.0	
$g/L$	0.21–0.27	0.16–0.32	0.30–0.37	0.37–0.41		
Number of cells	31	66	38	30		
Number of quads	32	29	38	20	16	
Quad gradient (kG/cm)	8.34–2.46	2.44–1.89	1.01–0.87	0.90–0.84	0.84–0.83	
Quad length (cm)	2.62–7.88	7.88	16.29	16.29	16.29	
$E_0$ (MV/m)	1.60–2.30	2.40	2.40	2.50		
$\phi_s$ (°)	–26	–26	–26	–26		
Power (MW)	0.305	2.697	2.745	2.674		
Intertank space (cm)	15.90	85.62	110.95	–		
Transit-time factor, $T$	0.72–0.84	0.87–0.80	0.82–0.74	0.74–0.68		
Mean $ZT^2$ (M $\Omega$ /m)	26.8	30.1	23.7	19.2		

Total length including intertank spaces = 61.7 m

The best efficiency (higher effective shunt impedance) for DTL is achieved in the beam velocity range  $\beta = 0.1-0.3$ . At LANSCE it is used for wider range,  $\beta = 0.04-0.43$ .



# LANSCCE DTL tank models

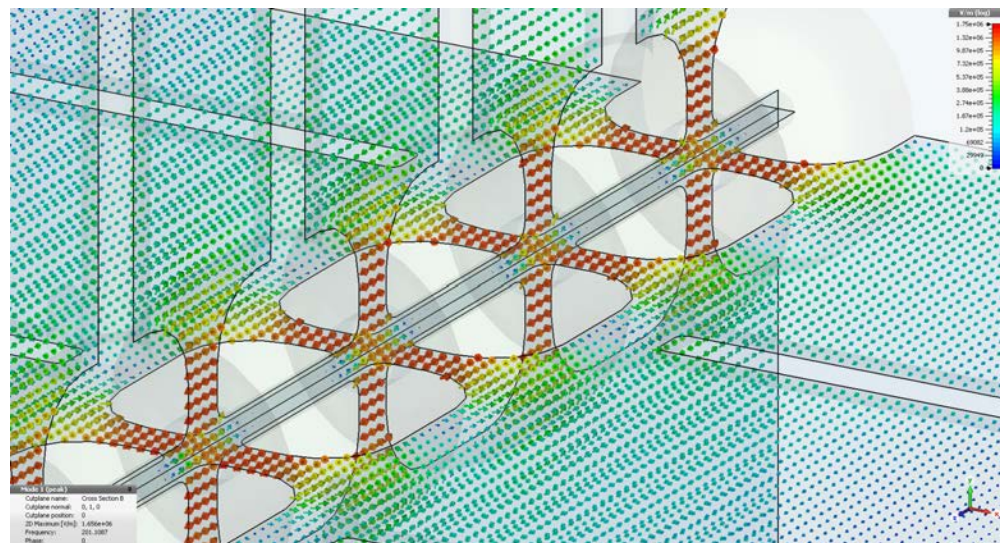


CST model of the LANSCE DTL tank 2: 66 cells, 19.68-m long,  $\beta = 0.107-0.287$

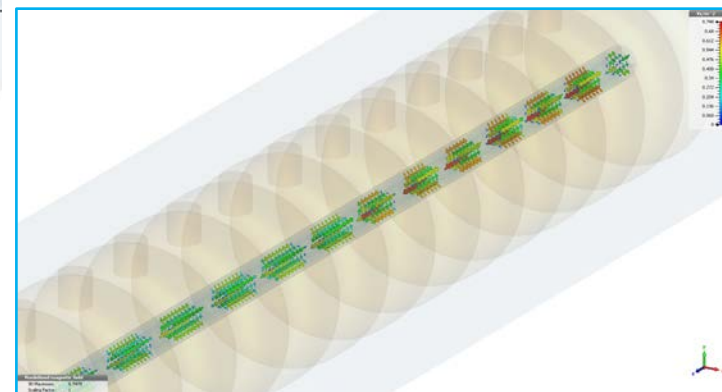
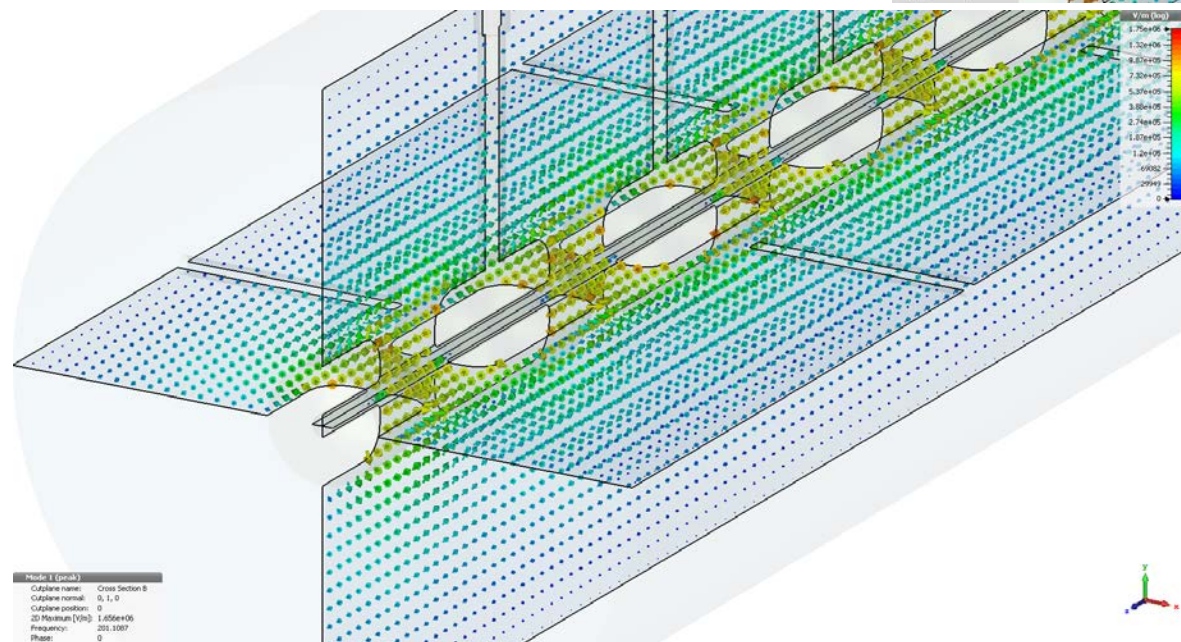


# Fields in DTL tanks

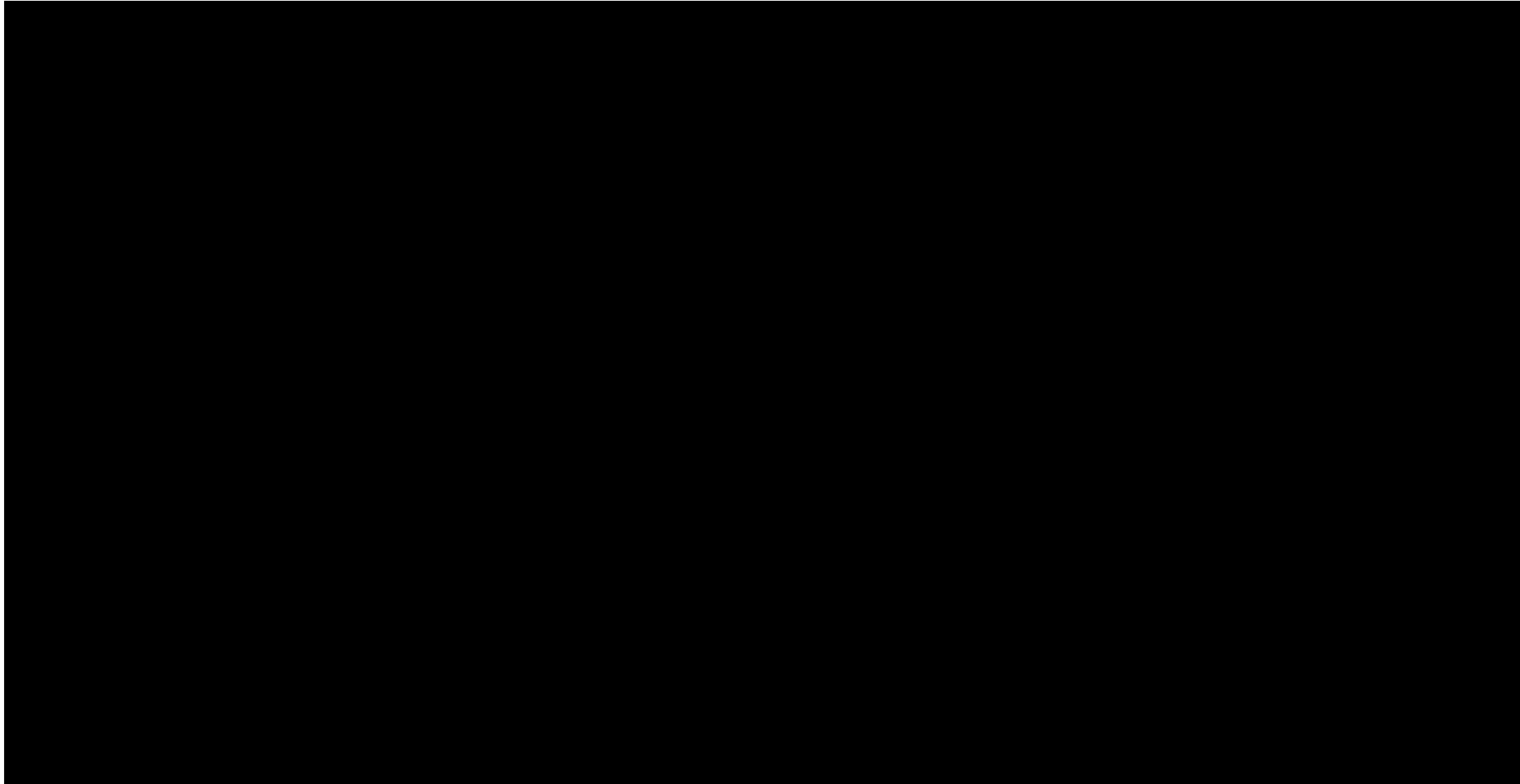
Electric field arrows (MWS norm.) in x & y-planes near the entrance (right) and exit (bottom) of DTL tank 2.



Magnetic fields of quadrupoles near the entrance of DTL tank 1 (imported in PS).



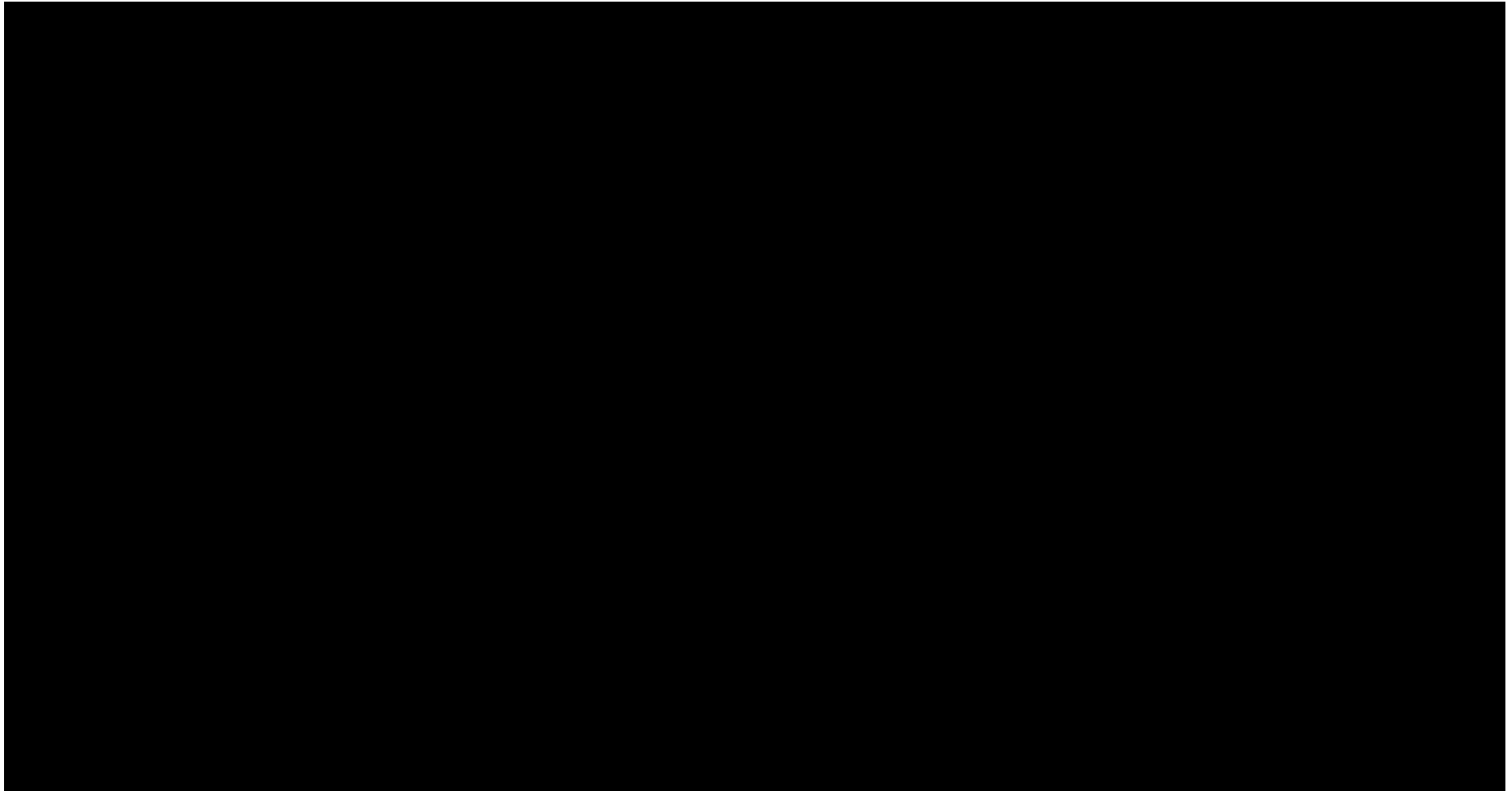
# DTL – PS simulations in LANSCE DTL tanks



Particle Studio simulations of 10 RF periods (10x10K) of 18-mA proton beam injected into DTL tank 1. Transmission 85% (80.6% in bunches, 4.4% in the tail).



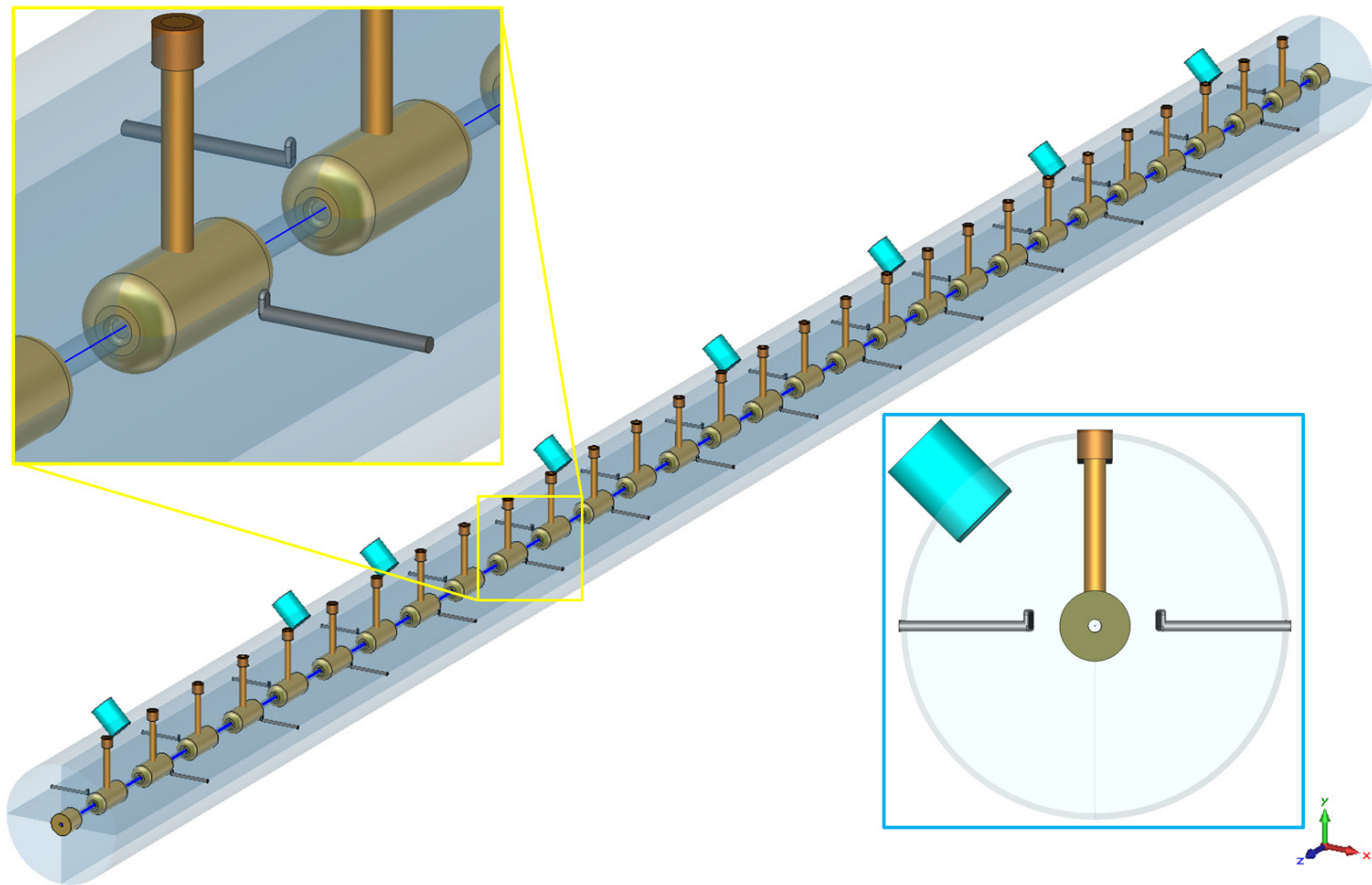
## DTL – PS simulations in LANSCE DTL tanks



Particle Studio simulations of 10 RF periods (10x10K) of 18-mA proton beam injected into DTL tank 1 – end-tank view. Transmission 85% (bunches 80.6%, tail 4.4%).



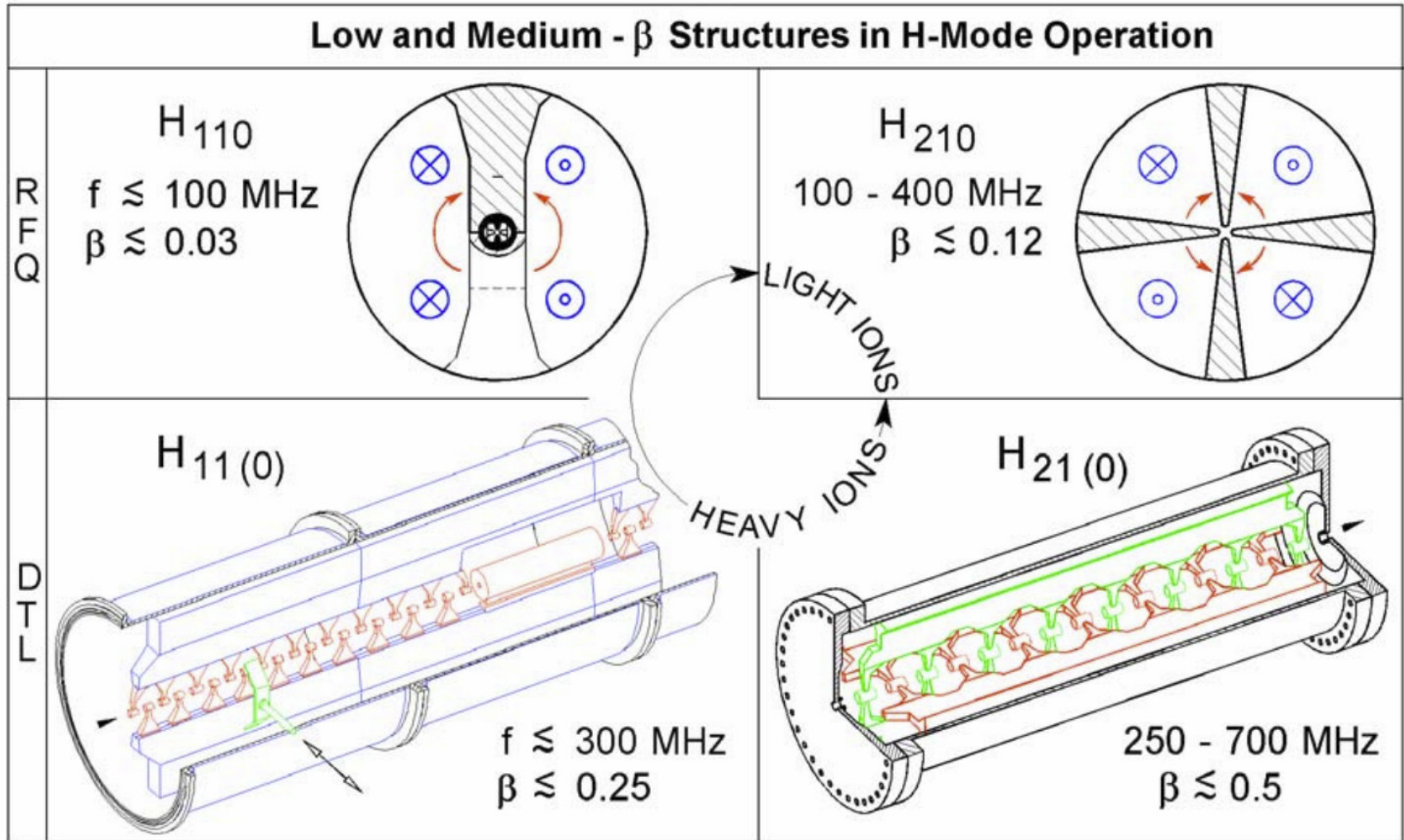
# DTL cavities: tuning



Frequency and field profile slug tuners in the DTL tank 4 model



# H-mode DTL – another type of DTL



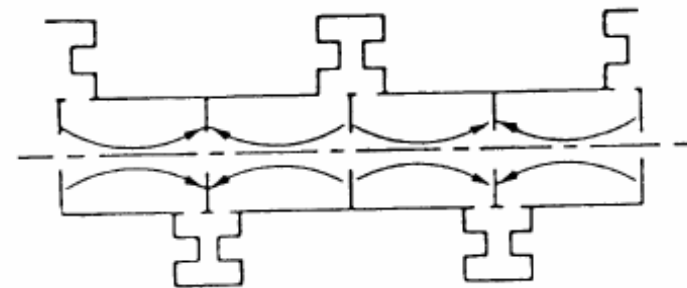
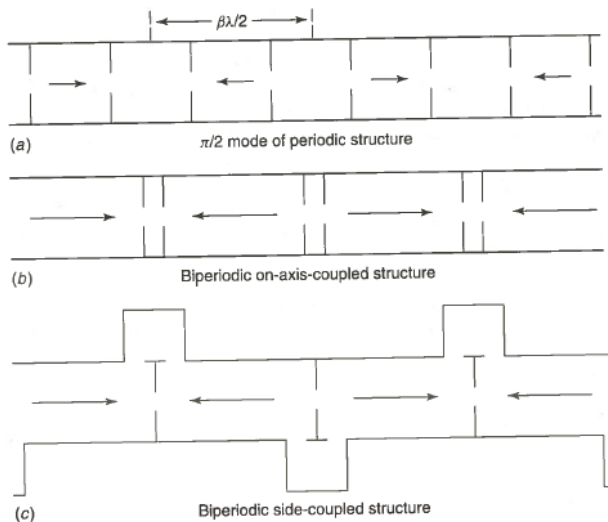
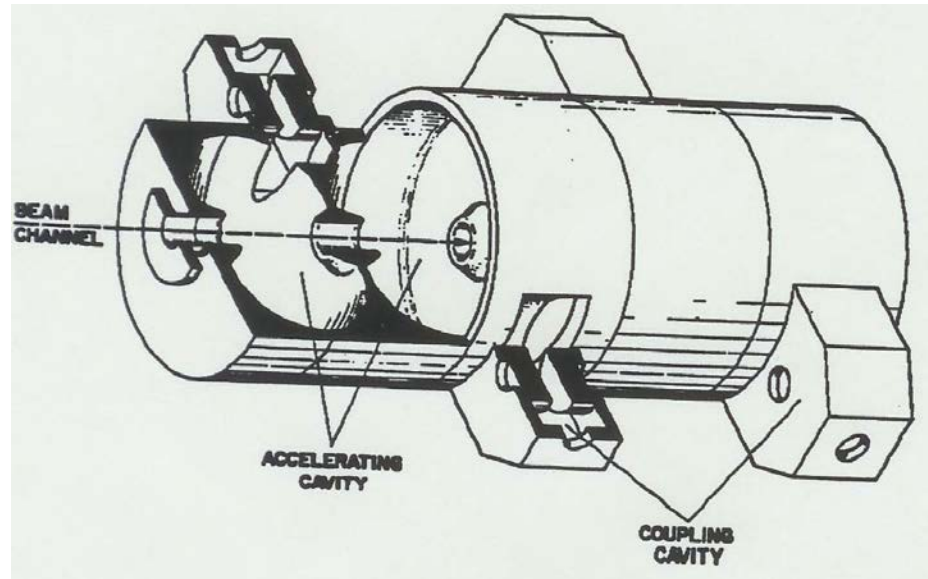
TE-mode DTL cavities: interdigital  $H_{110}$  (IH) and cross-bar  $H_{210}$  (CH)



# Coupled-Cavity Linac (CCL)

The coupling cells are not excited when the structure is tuned.

Various types of CCL (see below) are used at relatively high velocities, typically for  $\beta \geq 0.4$ .



Energy range 100-800 MeV  
High shunt impedance: up to 50 M $\Omega$ /m

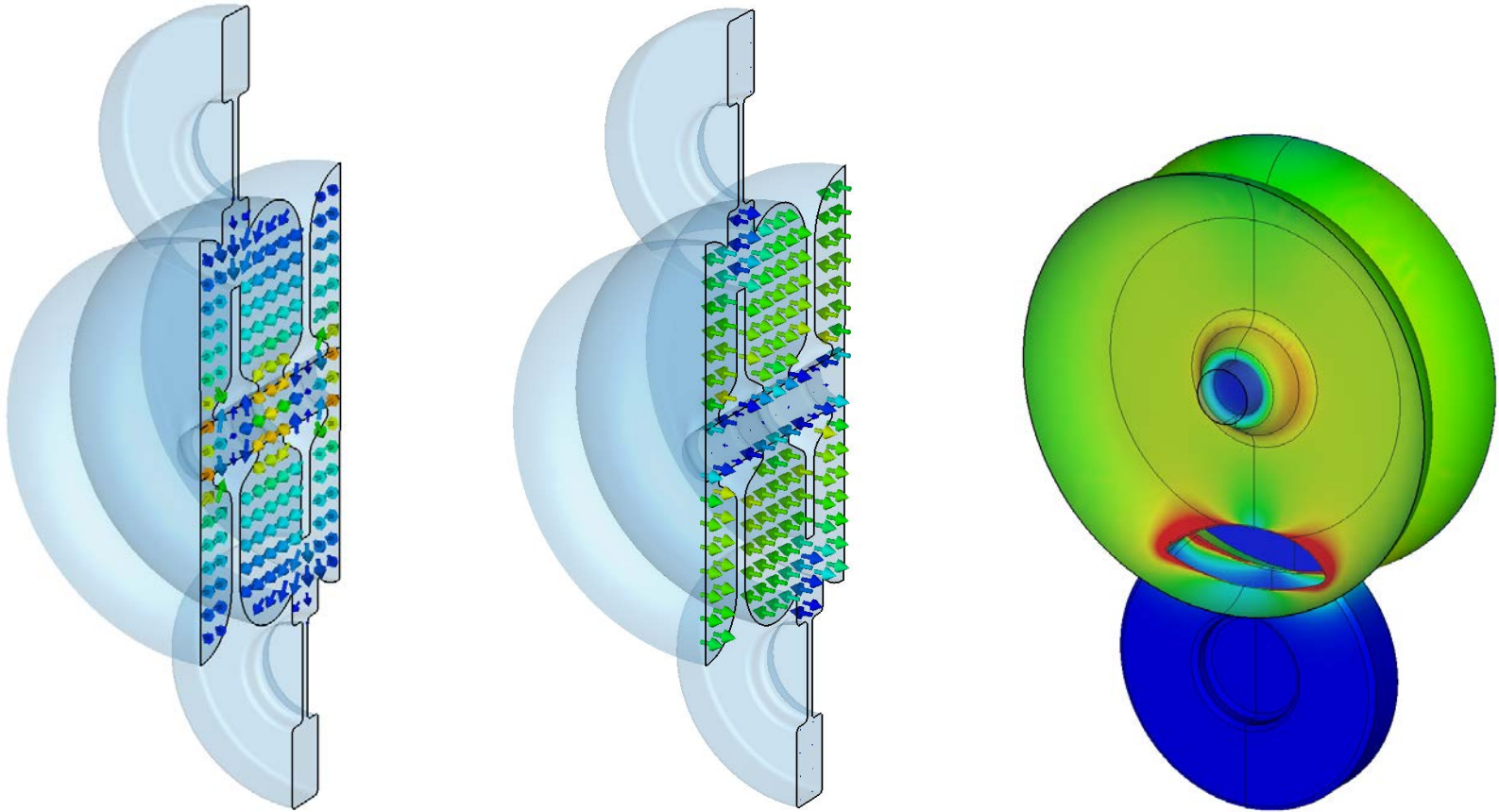
Los Alamos Side Coupled Structure (1968)





# LANSCE CCL – Module 5 Tank 1 (M5T1)

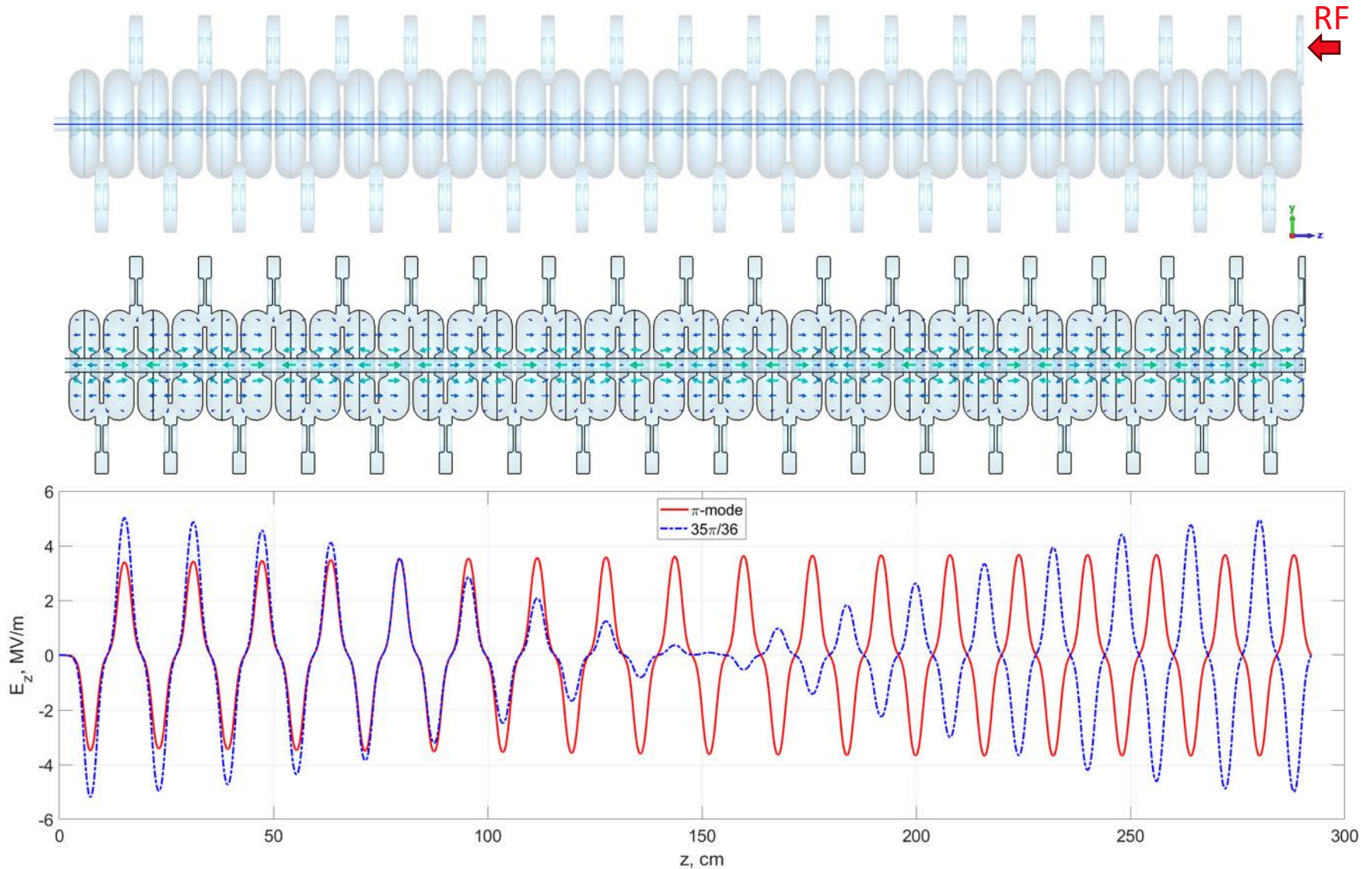
- M5T1:** 36 accelerating cells with 35 coupling cells (18 periods); length 2.89 m + 72-cm drift.
- Effective shunt impedance  $ZT^2 = 31.5 \text{ M}\Omega/\text{m}$ .
  - Energy in 100 MeV ( $\beta = 0.43$ ), out 103.4 MeV.



Electric (left) and magnetic (middle) fields and surface-current magnitude (right) in one period of M5T1



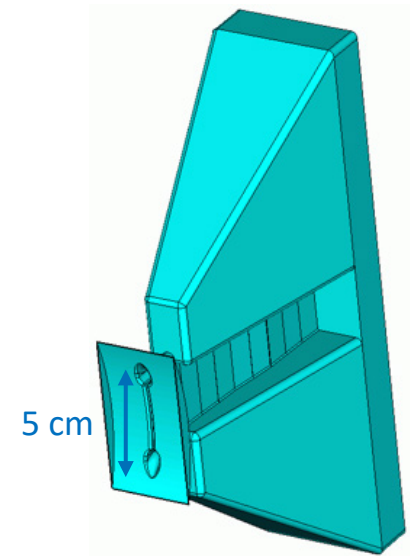
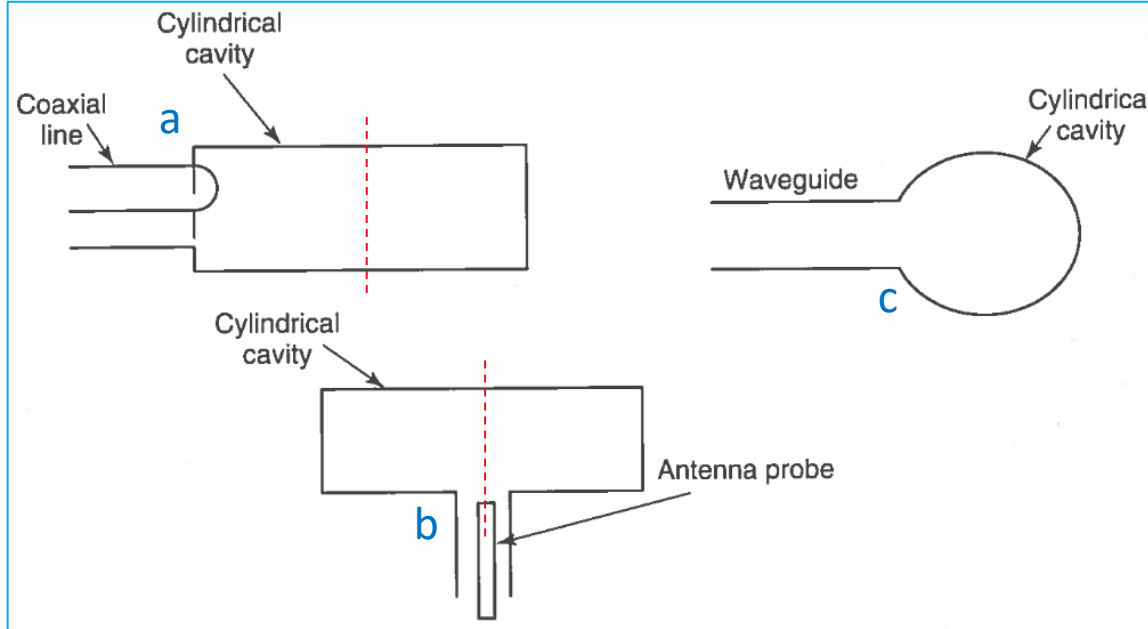
# LANSCCE CCL – Module 5 Tank 1



M5T1 cavity (top); electric field of the operating  $\pi$ -mode (middle); on-axis longitudinal electric fields of the two lowest modes:  $\pi$ -mode (red) and mode  $35/36 \pi$  per AC (blue dashed)



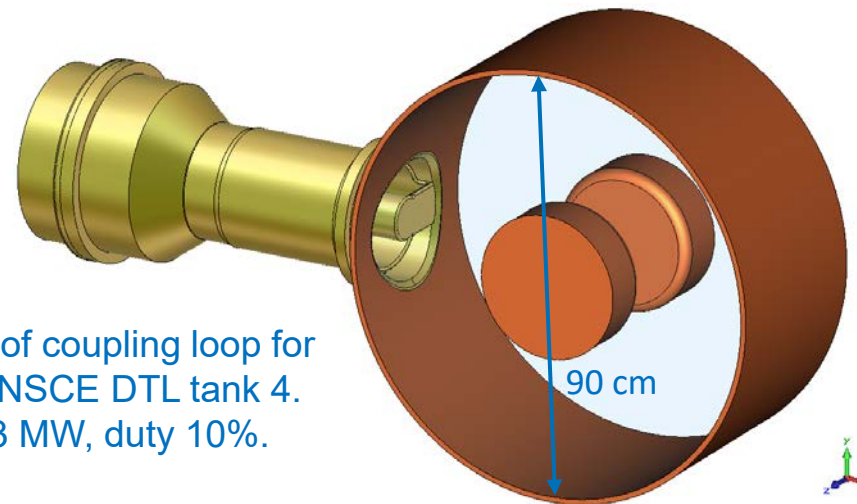
# Coupling RF power to cavities



“Dog-bone” coupling iris for high-power FEL photoinjector. Up to 0.5 MW at 100% duty.

Methods of coupling to RF cavities:

- (a) magnetic – current loop;
- (b) electric – antenna;
- (c) magnetic – iris WG-cavity



Model of coupling loop for the LANSCE DTL tank 4. Up to 3 MW, duty 10%.



## Summary 2

- RF cavities and some common accelerating structures (DTL, CCL) are reviewed.



# Figures of merit for accelerating structures

Quality factor (stored energy  $U$ , averaged power loss  $P$ )

$$Q = \frac{\omega U}{P}$$

Shunt impedance (total cavity voltage  $V_0$ )

$$R_{sh} = \frac{V_0^2}{P}$$

Effective shunt impedance (effective voltage  $V_0 T$ )

$$R_{eff} = R_{sh} T^2$$

Shunt impedance per unit length (voltage  $V_0 = E_0 L$ )

$$Z = \frac{E_0^2}{P / L}$$

Effective shunt impedance per unit length ( $Z_{eff}$ )

$$Z T^2 = \frac{(E_0 T)^2}{P / L}$$

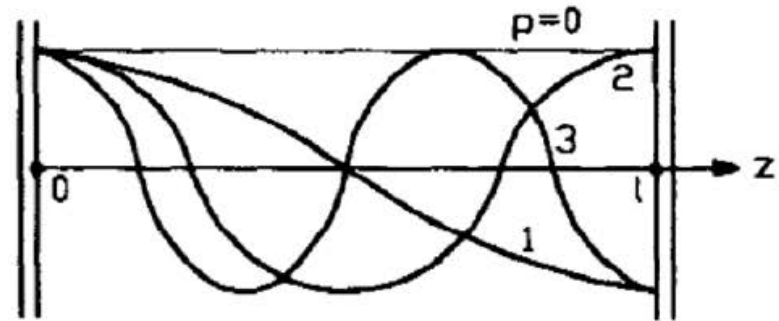
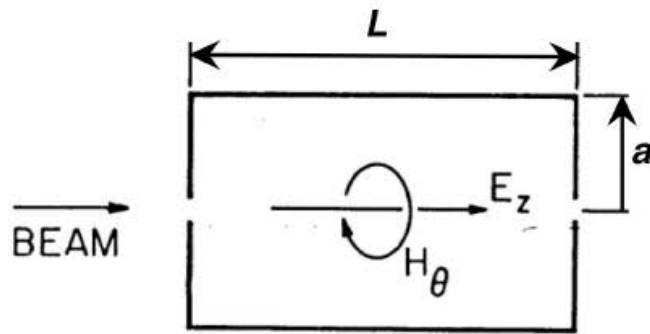
Ratio  $R_{eff}/Q$  is independent of surface losses and depends only on the cavity (structure) geometry

$$\frac{R_{eff}}{Q} = \frac{(V_0 T)^2}{\omega U}$$

Ratios  $E_{max}/E_{acc}$  ( $E_{acc} = E_0 T$ ) and  $B_{max}/E_{acc}$  – lower is better. The latter is very important for SC cavities.



# RF cavities: cylindrical resonator (pillbox)



Longitudinally integer number of half-variations can be excited

Transverse boundary condition:

$$k_z = \frac{\pi p}{L}$$

$$E_z(a) = 0 \quad J_n(k_r a) = 0 \quad k_r = \frac{v_{nm}}{a}$$

$$\frac{\omega_o^2}{c^2} - k_z^2 = \frac{v_{nm}^2}{a^2}$$

Frequency of oscillation mode is

$$\omega_o = c \sqrt{\frac{v_{nm}^2}{a^2} + \left(\frac{\pi p}{L}\right)^2}$$

Longitudinal component

$$E_z = E_o J_n\left(v_{nm} \frac{r}{a}\right) \cos n\theta \cos \frac{\pi p z}{L}$$

mode  $TM_{nmp}$



# Example: TM<sub>010</sub> mode

$$J'_1(x) = 0 \quad x_1 = 1.841 \quad J_1(x_1) = 0.5819$$

$$J_1(2.405) = 0.5191$$

Field components

$$E_z = E_o J_o(v_{01} \frac{r}{a}) \cos \omega_o t$$

$$B_\theta = -\frac{E_o}{c} J_1(v_{01} \frac{r}{a}) \sin \omega_o t$$

Boundary condition

$$E_z(a) = 0$$

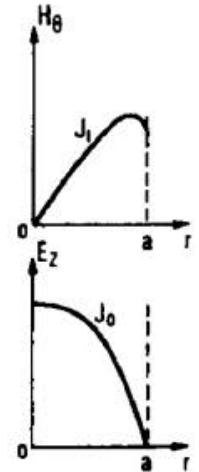
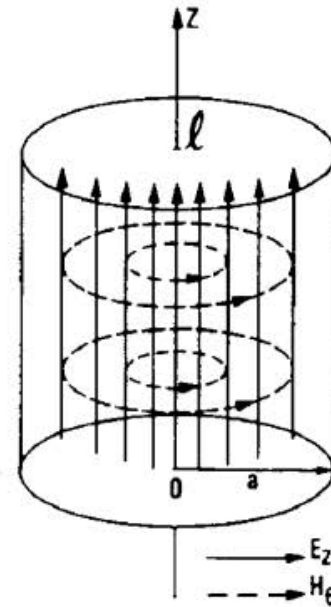
$$v_{01} = 2.405$$

Frequency of resonator

$$k_z = 0$$

$$\omega_o = 2\pi f = \frac{c v_{01}}{a}$$

$$f = \frac{2.405 c}{2\pi a}$$



Example: radius of resonator for  $f = 201.25$  MHz:

$$a = \frac{2.405 c}{2\pi f} = 0.57m$$

TM<sub>010</sub> mode in a pill-box cavity.

Note:

$$B = \mu_0 H; \quad [B] = T; [H] = A/m; Z_0 = \sqrt{\mu_0 / \epsilon_0} = 376.7 \Omega; \quad [E] = [Z_0 H] = V/m;$$

$$c = 1 / \sqrt{\mu_0 \epsilon_0}; \quad \mu_0 c = Z_0.$$



# Energy dissipation in resonator and Q factor

Dissipated power is a combination of power losses inside cavity and outside cavity

Energy stored in cavity

Quality factor

Q-factor is a combination of unloaded quality factor of cavity and external quality (loaded Q factor)

External quality factor

Losses in metal with surface resistance  $R_s$  [Ohm]

$$R_s = \frac{1}{\sigma\delta} = \sqrt{\frac{\mu_0\omega}{2\sigma}}, \text{ where } \sigma \text{ is the surface conductivity,}$$

$$\text{and } \delta \text{ is the skin depth } \delta = \sqrt{2 / (\mu_0\sigma\omega)}.$$

Unloaded quality factor

$$Q_o = \frac{\omega_o W_o}{P_o}$$

Physical meaning:  $Q = G \frac{V}{S\delta}$

$$P = P_o + P_{ext}$$

$$W_o = \frac{1}{2} \int_{V_o} \mu H_m^2 dV = \frac{1}{2} \int_{V_o} \epsilon E_m^2 dV$$

$$Q = \frac{\omega_o W_o}{P}$$

$$\frac{1}{Q} = \frac{1}{Q_o} + \frac{1}{Q_{ext}}$$

$$Q_{ext} = \frac{\omega_o W_o}{P_{ext}}$$

$$P_o = \frac{R_s}{2} \int_s H_m^2 dS$$

$$Q_o = \frac{\omega_o \int_{V_o} H_m^2 dV}{R_s \int_s H_m^2 dS}$$





# Quality factor of $TM_{010}$ cavity

Magnetic field

$$H_{m\theta} = -E_o \sqrt{\frac{\epsilon_o}{\mu_o}} J_1\left(\nu_{01} \frac{r}{a}\right) \quad \text{Amplitude}$$

Energy stored in cavity

$$W_o = \frac{1}{2} \int_{V_o} \mu_o H_{m\theta}^2 dV = \frac{\pi \epsilon_o E_o^2 L a^2 J_1^2(\nu_{01})}{2} = 0.135 \pi \epsilon_o L a^2 E_o^2$$

Loss power in cavity

$$P_o = \frac{R_s}{2} \int_S H_{m\theta}^2 dS = \pi a R_s E_o^2 \frac{\epsilon_o}{\mu_o} J_1^2(\nu_{01}) (L + a)$$

Unloaded quality factor

$$Q_o = \frac{\omega_o W_o}{P} = \frac{\nu_{01}^2}{2 R_s} \sqrt{\frac{\mu_o}{\epsilon_o}} \frac{1}{\left(1 + \frac{a}{L}\right)} = 1.2025 \frac{376.7 [\text{Ohm}]}{R_s} \frac{1}{\left(1 + \frac{a}{L}\right)}$$

For ideal copper surface  $\sigma = 5.8 \cdot 10^7$  Sm/m, so that  $R_s = 2.6 \cdot 10^{-4} \sqrt{f(\text{MHz})} \Omega$ . At 201.25 MHz,  $R_s = 3.7$  m $\Omega$ , and  $Q_o = 66500$  for  $a/L = 1$ . In practice, typically 10%-20% less.



# Surface conductivity in superconducting RF cavities

For RF cavities the power loss depends on the surface resistance: for normal-conducting

$$R_s = \frac{1}{\sigma\delta} = \sqrt{\frac{\mu_0\omega}{2\sigma}} \text{ scales with RF frequency as } \sqrt{f}.$$

In superconducting (SC) RF cavities the surface resistance is much lower; e.g., for Nb

$$R_s (\Omega) = 9 \cdot 10^{-5} \frac{f^2 (\text{GHz})}{T (\text{K})} \exp\left(-\alpha \frac{T_c}{T}\right) + R_{res},$$

where  $R_{res}$  is the residual resistance ( $\sim 1\text{-}10$  n $\Omega$ ),  $\alpha = 1.83$ , and  $T_c = 9.2$  K is the critical temperature.

SC  $R_s$  is  $\sim 10^{-5}$  of that in copper, and so are the cavity surface losses!



# RF cavity design

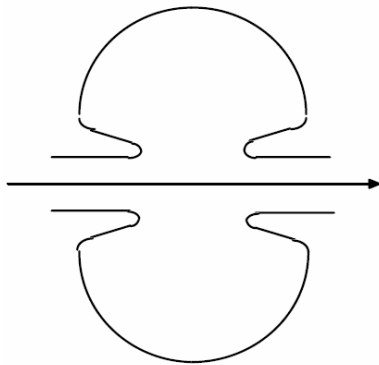
Cavity design goals depend on many factors including the cavity type and its application: maximize accelerating gradient, minimize losses (NC), minimize max surface fields, etc.

Frequency dependence of cavity parameters:  $a \sim 1/f$ ,

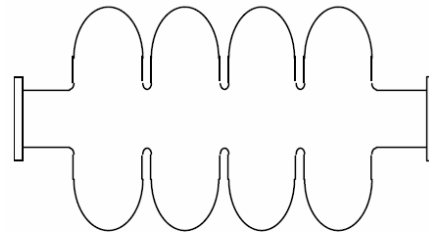
$$P \propto \begin{cases} f^{-1/2}, & \text{NC} \\ f, & \text{SC} \end{cases} \quad Q \propto \begin{cases} f^{-1/2}, & \text{NC} \\ f^{-2}, & \text{SC} \end{cases} \quad ZT^2 \propto \begin{cases} f^{1/2}, & \text{NC} \\ f^{-1}, & \text{SC} \end{cases}$$

Frequency choice also depends on available RF sources and beam parameters.

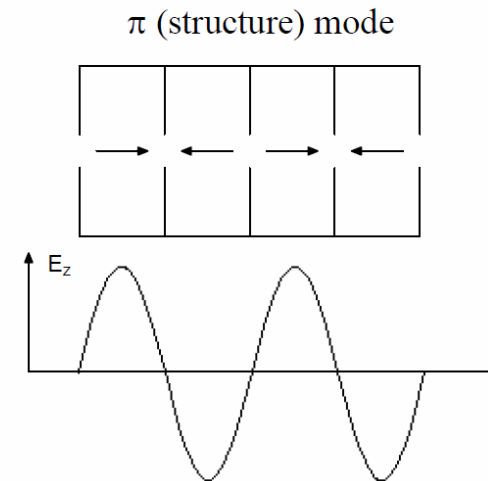
Changing cavity shape is the common way of achieving the design goals. Examples:



Nose-cone cavity



4-cell elliptical cavity (SC)



# RF cavity design codes

- Calculation of EM fields in the cavity: frequencies, modes, secondary parameters (losses,  $Q$ , shunt impedance, surface fields, ...)
- Calculation methods:
  - Analytical (simple cavity shapes) + perturbation theory
  - 2D codes (axisymmetric or flat structures): Superfish, URMEL, ...
  - 3D codes: CST, HFSS, Analyst, ACE-3P (Omega-3P), etc.



# Los Alamos Accelerator Code Group (LAACG)

Available at [laacg.lanl.gov/laacg/services/services.phtml](http://laacg.lanl.gov/laacg/services/services.phtml)

## Poisson / Superfish

- *collection of programs for calculating static magnetic and electric fields and radio-frequency electromagnetic fields in either 2-D Cartesian coordinates or axially symmetric cylindrical coordinates.*
- *triangular mesh*
- *includes plotting and post-processing*

## \* Poisson / Pandira

- *static electric and magnetic fields*

## \* Superfish

- *radio-frequency electromagnetic fields*

Windows PC – <C:\LANL> contains *programs & utilities; \Docs; \Examples; etc.*



The screenshot shows the LAACG website interface. At the top right, there are links for [LANL Home](#), [LANL Directory](#), and [Search LANL Web](#). Below this is the Los Alamos National Laboratory logo and the LAACG logo. A navigation bar contains links for [LANL](#), [About Us](#), [Beam Physics](#), [LANL ACE](#), [LAACG Codes](#), [General Resources](#), [LANL Accelerators](#), [Accelerator Physics](#), [Software/Methods](#), [Home](#), [News](#), and [Site Index](#). The main content area is titled "LAACG - Codes/Databases" and includes a sidebar menu with links like [->LAACG Codes](#), [->Poisson Superfish](#), [->Parmela](#), [->Parmila](#), [->Parmteq](#), [->Trace-2D/3D](#), [->Announcements](#), [->Access](#), [->LAACG Databases](#), [->Software](#), and [->Accelerators](#). The main content lists various code categories and design codes, such as "LAACG Design Codes" and "LAACG Databases - DISCONTINUED", with sub-links for each. At the bottom, there is a footer with the text: "This work is supported by the U. S. Department of Energy, Office of Science, Division of High Energy Physics."



# Superfish (SF)

Steps for running SF (from command window or with right click):

- create geo file (test.am);  $x \rightarrow z$ ,  $y \rightarrow r$  (cm); define BC and materials
- run Automesh on test.am > test.T35 with geo and mesh
- run Fish on test.T35 > test.T35 with fields
- double-click test.T35 to see field lines
- run post-processing of test.T35 > test.sfo to get cavity parameters

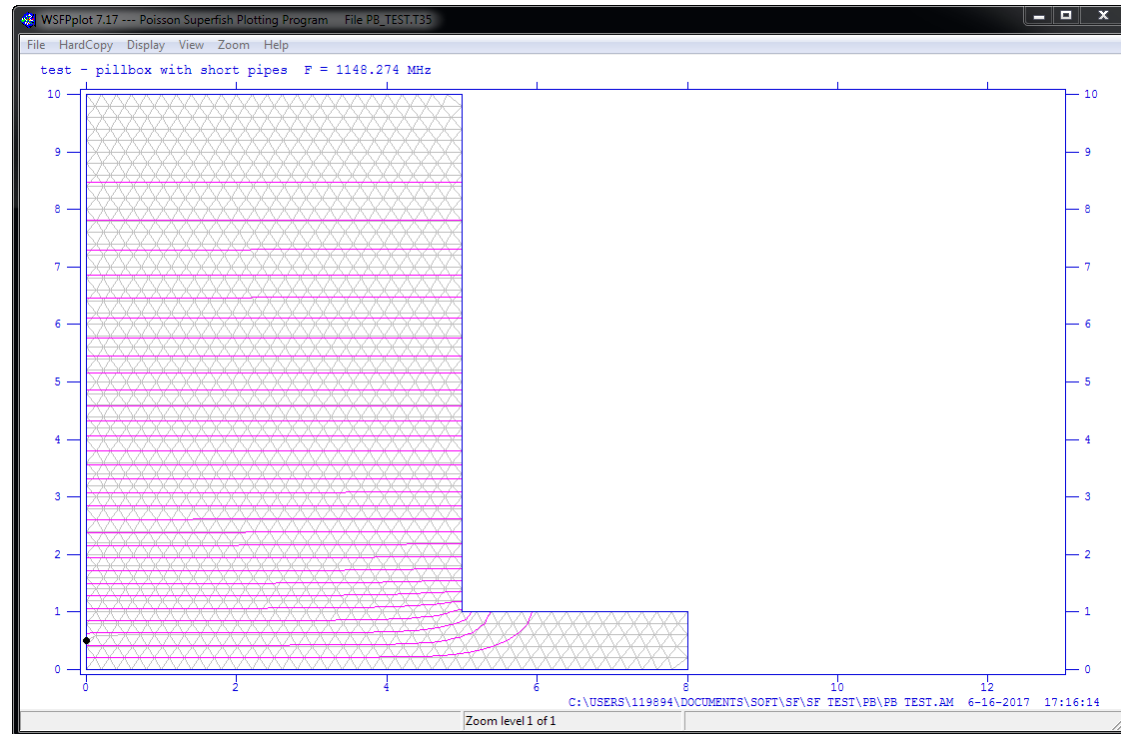
Alternative: run **Autofish** on test.am

pb\_test.am

```
test - pillbox with short pipes
```

```
&reg kprob=1,  
dx=0.2,dy=0.2,  
xdri=0.,ydri=0.5,freq=1500.00,dslope=-1,  
npoint=7 &
```

```
&po x= 0.0, y= 0.0 &  
&po x= 0.0, y= 10.0 &  
&po x= 5.0, y= 10.0 &  
&po x= 5.0, y= 1.0 &  
&po x= 8.0, y= 1.0 &  
&po x= 8.0, y= 0.0 &  
&po x= 0.0, y= 0.0 &
```



# Superfish input file

## SF input (\*.am or \*.af):

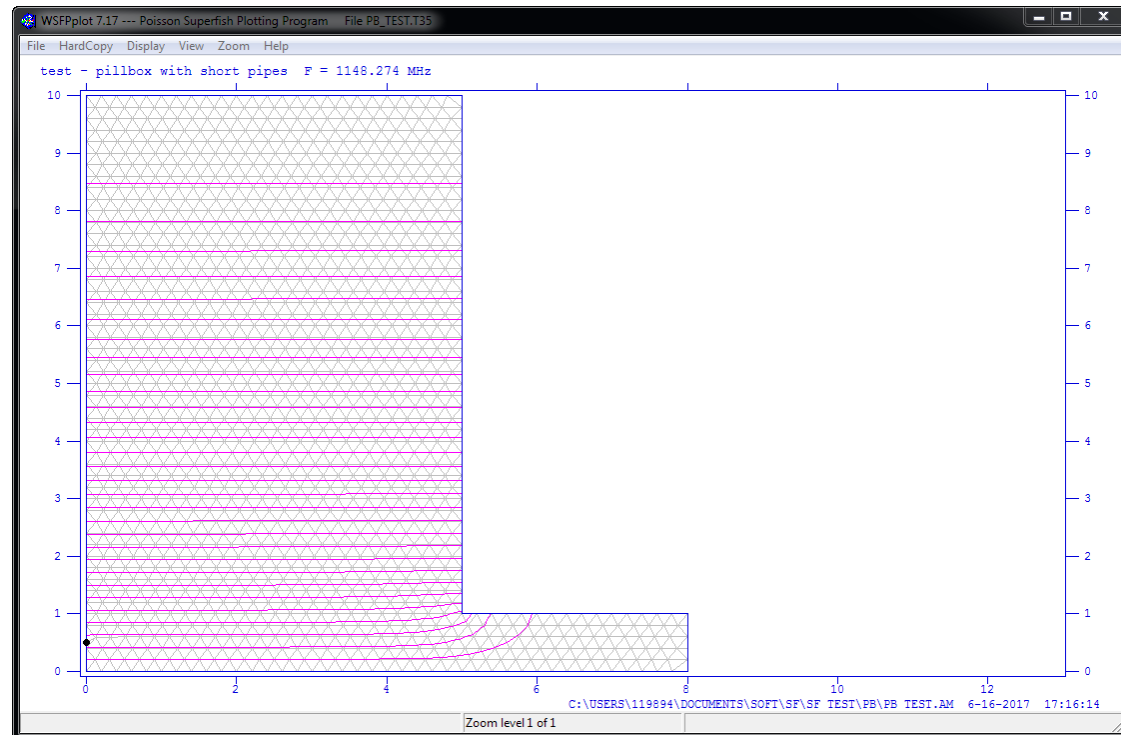
- First line is the problem title (< 80 char) followed by 3 namelists: REG, PO, MT (actually parsing). Delimiters: & or \$; comment: ; or !
- \$reg: kprob - problem type (1 – SF, 0 – Poisson) – in the 1<sup>st</sup> \$reg, symmetry: e.g., icylin=1 – cylindrical; BCs; approximate frequency (MHz); mat #.
- \$po: defines geometry; separate \$po list for each material. Note \$po ... \$.
- \$mt: mt=2, 3, ... - material table defines mat properties (epsilon, mu).

pb\_test.am

```
test - pillbox with short pipes
```

```
&reg kprob=1,  
dx=0.2,dy=0.2,  
xdri=0.,ydri=0.5,freq=1500.00,dslope=-1,  
npoint=7 &
```

```
&po x= 0.0,  y= 0.0 &  
&po x= 0.0,  y= 10.0 &  
&po x= 5.0,  y= 10.0 &  
&po x= 5.0,  y= 1.0 &  
&po x= 8.0,  y= 1.0 &  
&po x= 8.0,  y= 0.0 &  
&po x= 0.0,  y= 0.0 &
```



# Superfish problem 1. Pillbox cavity.

## Design $TM_{010}$ cavity for frequency 201.25 MHz

- Estimate radius  $R$ , choose length  $L$  (default units – cm); define BCs or use default BCs (SF: left – symmetry: Dirichlet BC).
- Create cavity geometry file, e.g., pb.am
- run Automesh on pb.am > pb.T35 with geo and mesh
- run Fish on pb.T35 > pb.T35 with fields
- double-click pb.T35 to see field lines
- run SFO post-processing of pb.T35 > pb.sfo

For  $TM_{nmp}$  modes in a cylindrical cavity of radius  $R$  and length  $L$ , the frequency

$$f_{nmp} = \frac{c}{2\pi} \sqrt{\left(\frac{j_{nm}}{R}\right)^2 + \left(\frac{\pi p}{L}\right)^2},$$

where  $j_{nm}$  are the roots of  $J_n(j_{nm}) = 0$ . The value of  $j_{01} = 2.4048$ .





# SF problems 1a & 1b. Pillbox cavity with beam pipe.

SF 1a: Design  $TM_{010}$  cavity for frequency 201.25 MHz with beam pipe.

- Add beam pipe to the pillbox cavity you already designed. Use pipe radius  $a \ll R$ , choose pipe length  $p > 2a$ .
- Will the cavity frequency increase or decrease when you add the pipe?

SF 1b:  $TM_{010}$  cavity with rounded edge of cavity-pipe connection: blend the sharp edge by introducing an arc:

Use  $\$po nt=2, x0=11.0, y0=3.5, r=1, theta=270 \$$  to make an arc.

Slater perturbation theorem relates the cavity frequency change with energy changes due to small deformations of cavity walls:

$$\frac{\Delta f}{f_0} = \frac{\Delta W_m - \Delta W_e}{2W_0}.$$

Sometimes it is useful to use  $L$ - $C$  circuit analogy for the cavity frequency:

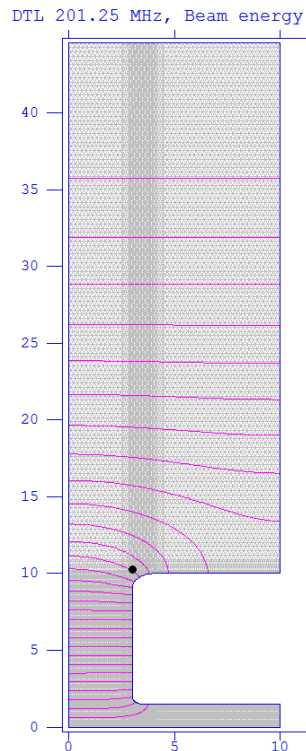
$$f = \frac{1}{2\pi\sqrt{LC}}.$$



# SF problem 2. Pillbox cavity with drift tube

Design  $TM_{010}$  cavity for frequency 201.25 MHz with a drift tube.

- Recommended  $g/L=0.3$ , DT outer radius 10 cm. How large is the frequency shift from 201.25 MHz when DT is inserted?
- Adjust cavity radius to get back to 201.25 MHz.



# DTL design using DTLfish

Tuning code DTLfish can design and tune a sequence of cells with some required parameters, e.g. frequency, in a given velocity range, e.g.  $\beta = 0.1-0.3$ .

```
DTL201.dtl x
; DTLfish control file
; Copyright 1998, by the University of California.

TITLE
DTL 201.25 MHz, Beam energy = 8.5 MeV
ENDTITLE

PARTICLE          H+
FILENAME_prefix   DTL
SEQUENCE_number   1
FREQUENCY         201.25
;BETA             0.135
G_OVER_Beta_lambda 0.3
LENGTH           20.
DIAMETER         90.
DRIFT_TUBE_Diameter 20.0
;GAP_Length      5.
E0_Normalization 1.0
CORNER_radius    1.
OUTER_nose_radius 1.
INNER_nose_radius 0.5
BORE_radius      1.5
FLAT_length      0
STEM_Diameter    1.905
STEM_Count       1
PHASE_length     180
DELTA_frequency  0.005
MESH_size        0.05
INCREMENT        2
START            2

ENDFILE
```

```
DTLfish_seq.txt x
...
START -2

; Start codes for DTLfish:
; 1 No tuning
; 2 Adjust tank diameter
; 3 Adjust drift tube diameter (not recommended)
; 4 Adjust gap
; 5 Adjust face angle

SEQUENCE_number 2 ; Problem 2
BETA            0.1
LENGTH         7.053940188235
DIAMETER       PREVIOUS
G_OVER_Beta_lambda 0.2042467589655
GAP_Length     1.440744421384
START          -4

SEQUENCE_number 3 ; Problem 3
BETA            0.15
DIAMETER       PREVIOUS
START          -4
```



# SF problem 3. DTL design using DTLfish.

Design DTL cells for frequency 201.25 MHz for  $\beta = 0.135$ .

- Recommended  $g/L=0.3$ , DT outer radius 10 cm. **Note:** \*.dtl
- DTLfish can tune the cavity parameters, e.g. cavity radius or gap, to get the required frequency, 201.25 MHz.

```
DTL201.dtl x
; DTLfish control file
; Copyright 1998, by the University of California.

TITLE
DTL 201.25 MHz, Beam energy = 8.5 MeV
ENDTITLE

PARTICLE          H+
FILEName_prefix  DTL
SEQuence_number   1
FREQuency         201.25
;BETA             0.135
G_OVER_Beta_lambda 0.3
LENGTh           20.
DIAMeter         90.
DRIFT_TUBE_Diameter 20.0
;GAP_Length      5.
E0_Normalization 1.0
CORNER_radius    1.
OUTER_nose_radius 1.
INNER_nose_radius 0.5
BORE_radius      1.5
FLAT_length      0
STEM_Diameter    1.905
STEM_Count       1
PHASE_length     180
DELTA_frequency  0.005
MESH_size        0.05
INCRement        2
START            2

ENDFILE
```

